Electromagnetic Observables and Hydrodynamics



Figure: K. Reygers (2014)



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Sources & EM emissivity: Rates •Modelling the evolving system: 3D viscous hydro Fluctuating initial states • How are the photon yield and v_2 dependent on the dynamics? • Photons as a characterization tool: Temperature (& shear viscosity) Status of our interpretation of the data

Why study photons and dileptons in relativistic nuclear collisions?

- •Penetrating probes: negligible final state effects (α)
- Real and virtual photons are complementary, and they supplement hadronic observables
 Thermal photon emission rate favours hotter
- zones of the colliding system
- ^oEmitted throughout the collision history
- ^oLow emission rates
- •Procedure: Calculate thermal emission rates & use hydrodynamics to model the evolution. Integrate rates over whole history







Sources of photons in a relativistic nuclear collision:

Hard direct photons. pQCD with shadowing Non-thermal

Fragmentation photons. pQCD with shadowing Non-thermal

Thermal photons Thermal



Jet-plasma photons Thermal

Jet in-medium bremsstrahlung Thermal







INFO CARRIED BY THE THERMAL RADIATION

$$dR = -\frac{g^{\mu\nu}}{2\omega} \frac{d^3k}{(2\pi)^3} \frac{1}{Z} \sum_{i} e^{-\beta K_i} \sum_{f} (2\pi)^4 \delta(p_i - p_f - k)$$
$$\times \langle j | J_{\mu} | i \rangle \langle i | J_{\nu} | j \rangle$$

Thermal ensemble average of the current-current correlator

Emission rates:

$$\omega \frac{d^{3}R}{d^{3}k} = -\frac{g^{\mu\nu}}{(2\pi)^{3}} \operatorname{Im}\Pi^{R}_{\mu\nu}(\omega,k) \frac{1}{e^{\beta\omega} - 1} \qquad \text{(photons)}$$

$$E_{+}E_{-}\frac{d^{6}R}{d^{3}p_{+}d^{3}p_{-}} = \frac{2e^{2}}{(2\pi)^{6}} \frac{1}{k^{4}} L^{\mu\nu} \operatorname{Im}\Pi^{R}_{\mu\nu}(\omega,k) \frac{1}{e^{\beta\omega} - 1} \qquad \text{(dileptons)}$$

Feinberg (76), McLerran, Toimela (85) Weldon (90), Gale, Kapusta (91)



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(FOR DILEPTONS:)

 $\operatorname{Im} < J_{\mu}J_{\nu} >_{T} \Rightarrow \operatorname{Im} < \rho_{\mu}\rho_{\nu} >_{T} \Rightarrow \operatorname{Im} D_{\mu\nu}^{T} \Rightarrow \operatorname{Vector spectral density}$



Thermal Photons from hot QCD: HTL program (Klimov (1981), Weldon (1982), Braaten & Pisarski (1990); Frenkel & Taylor (1990))

$$\int \int R_{R\mu} dr$$

$$\int_{R\mu}^{\mu} \sim \ln\left(\frac{\varpi T}{\left(m_{th}\left(\sim gT\right)\right)^{2}}\right)$$

Kapusta, Lichard, Seibert (1991) Baier, Nakkagawa, Niegawa, Redlich (1992)

Going to two loops: Aurenche, Kobes, Gélis, Petitgirard (1996) Aurenche, Gélis, Kobes, Zaraket (1998)



Co-linear singularities: $\alpha_s^2 \left(\frac{1}{m_{th}^2}\right) \sim \alpha_s$

2001: Results complete at $O(\alpha_{s})$

Arnold, Moore, and Yaffe JHEP 12, 009 (2001); JHEP 11, 057 (2001) Incorporate LPM; Inclusive treatment of collinear enhancement, photon and gluon emission



 \sim



Going beyond LO AMY rates?

•Approach is LO, but

 $\alpha_{s} \sim 0.2 - 0.3$

• Integral equation can be written in terms of a Dyson-Schwinger type iteration...



which contains a scattering kernel:

 $C(q_{\perp})|_{\rm LO} = g^2 C_R T \frac{m_D^2}{q_{\perp}^2 (q_{\perp}^2 + m_D^2)}$

Aurenche, Gélis, Zaraket (2002)

The techniques used to derive this - and all results in perturbative, finite-temperature field theory - rely on the scale separation:

$$gT \ll T$$

soft \ll hard



The LO-NLO scattering kernel(s)

Clue that NLO effects might be important: Heavy quark diffusion

 $C(q_{\perp})\Big|_{\rm LO} \rightarrow C(q_{\perp})\Big|_{\rm NLO}$

Simon Caron-Huot PRD (2009)



Possible large effects on photon production!?



The LO-NLO scattering kernels

Ghiglieri, Hong, et al., JHEP (2013)

The two main contributions:



ELECTROMAGNETIC RADIATION FROM HADRONS

Chiral, Massive Yang-Mills: O. Kaymakcalan, S. Rajeev, J. Schechter, PRD 30, 594 (1984)

$$\mathcal{L} = \frac{1}{8} F_{\pi}^{2} \operatorname{Tr} D_{\mu} U D^{\mu} U^{\dagger} + \frac{1}{8} F_{\pi}^{2} \operatorname{Tr} M \left(U + U^{\dagger} \right)$$
$$- \frac{1}{2} \operatorname{Tr} \left(F_{\mu\nu}^{L} F^{L\mu\nu} + F_{\mu\nu}^{R} F^{R\mu\nu} \right) + m_{0}^{2} \operatorname{Tr} \left(A_{\mu}^{L} A^{L\mu} + A_{\mu}^{R} A^{R\mu} \right)$$
$$+ \text{ non-minimal terms}$$

Parameters and form factors are constrained by hadronic phenomenology:

•Masses & strong decay widths

- •Electromagnetic decay widths
- •Other hadronic observables:
 - •e.g. $a_1 \rightarrow \pi \rho \quad D/S$

(See also, Lichard and Vojik, Nucl. Phys. (2010); Lichard and Juran, PRD (2008)) 10



EM emissivities computed: Turbide, Rapp, Gale, PRC (2004); Turbide, McGill PhD (2006)



ELECTROMAGNETIC RADIATION FROM HADRONS

All allowed s-, t-, and u- Born graphs of the reactions:

 $X + Y \longrightarrow Z + \gamma$ $\rho \to Y + Z + \gamma$ $K^* \to Y + Z + \gamma$ > X,Y,Z $\in \{\rho, \pi, K^*, K\}$



Turbide, Rapp, and Gale, PRC (2004)



COMPARING RATES



Turbide, Rapp, and Gale, PRC (2004)





PHOTONS @ RHIC: RATES ARE INTEGRATED USING "STANDARD" RELATIVISTIC HYDRODYNAMIC MODELLING



- At low p_T, spectrum dominated by thermal components (HG, QGP)
- At high p_T, spectrum dominated by pQCD
- Window for jet-QPG contributions at midрт?

• All hydro calculations undershoot low p_T photons



ONE OF THE USES OF PHOTONS: CHARACTERIZING THE HOT MATTER CREATED AT RHIC



$$T_{\rm excess} = 221 \pm 19 \pm 19 \,\mathrm{MeV}$$



van Hees, Gale Rapp,PRC (2011)Shen, Heinz, Paquet, Gale, PRC (2014)



BEYOND SIMPLE SPECTRA: FLOW AND CORRELATIONS





Soft photons will go with the flow Jet-plasma photons: a negative v₂ <u>Details will matter</u>: flow, T(t). . .

Turbide, Gale, Fries PRL (2006) Low p_T : Chatterjee *et al.*, PRL (2006) All p_T : Turbide *et al.*, PRC (2008)









THE EFFECTS OF SHEAR VISCOSITY ON BULK DYNAMICS

$$\begin{split} T_{\text{ideal}}^{\mu\nu} &= (\mathcal{E} + P) u^{\mu} u^{\nu} - P g^{\mu\nu} \\ T^{\mu\nu} &= T_{\text{ideal}}^{\mu\nu} + \pi^{\mu\nu} \\ \partial_{\mu} (s u^{\mu}) &\propto \eta \end{split} \text{ Israël & Stewart, Ann. Phys. (1979), Baier et al., \\ JHEP (2008), Luzum and Romatschke, PRC (2008) \\ \end{split}$$



THE EFFECTS OF SHEAR VISCOSITY ON THE PHOTON DISTRIBUTION

In-medium **hadrons**:

$$f_{0}(u^{\mu}p_{\mu}) = \frac{1}{(2\pi)^{3}} \frac{1}{\exp[(u^{\mu}p_{\mu} - \mu)/T] \pm 1}$$

$$f \to f_{0} + \delta f, \quad \delta f = f_{0}(1 \pm (2\pi)^{3}f_{0})p^{\alpha}p^{\beta}\pi_{\alpha\beta}\frac{1}{2(\varepsilon + P)T^{2}}$$

$$q_{0}\frac{d^{3}R}{d^{3}q} = \int \frac{d^{3}p_{1}}{2(2\pi)^{3}E_{1}}\frac{d^{3}p_{2}}{2(2\pi)^{3}E_{2}}\frac{d^{3}p_{3}}{2(2\pi)^{3}E_{3}}(2\pi)^{4}|M|^{2}\delta^{4}(...)\frac{f(E_{1})f(E_{2})[1 \pm f(E_{3})]}{2(2\pi)^{3}}$$

One considers all the reaction and radiative decay channels of external state combinations of:

 $\{\pi, K, \rho, K^*, a_1\}$ With hadronic form factors

+ QGP Photons



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- •Large at early times
- Small at later times: viscosity corrections to the distribution functions will also vanish





The Net thermal photon yield & V₂



- •Viscous corrections make the spectrum harder, ≈100% at p_T = 4 GeV.
- Increase in the slope of
 ≈15% at p_T = 2 GeV.
- Once pQCD photons are included: a few % effect from viscosity
- •The net elliptic flow is a weighted average. A larger QGP yield will yield a smaller v₂.

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INITIAL STATE FLUCTUATIONS: A PARADIGM SHIFT IN HEAVY ION ANALYSES





MOVING INTO THE "CHARACTERIZATION" PHASE ...



ALL TOGETHER NOW: FICS + VISCOSITY



0.12

- Combined with viscous corrections, FIC yield an enhancement by ≈5 @ 4 GeV, and ≈2 @ 2 GeV
- •Temperature estimated by slopes can vary considerably
- •A combination of hot spots and blue shift hardens spectra
- •FICs enhance v₂ in this centrality class (0-20%), as for hadrons
- •Net v₂ is comparable in size to that with ideal medium, in this centrality class



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PHOTON V2 DATA?



RHIC

Chatterjee et al. (2013) Dion et al. (2011)

ABORATORY

•Data is higher than calculation, even with e-b-e initial state fluctuations, and ideal hydro

•Size comparable with HG v₂

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PHOTON V2 DATA?

Pb+Pb, 2.76 TeV 0-40%



Paquet et al., (2014)



SOME FACTS AND SOME LEADS

- FICs are here to stay. "Initial temperature" is ill-defined.
- Some room to explore systematically hydro initialization and parameters. This requires consistency with the hadronic data.
- Making the QGP signal **larger** will *decrease* the v₂. The T=0 photons, *decrease* v₂. Suppose 2 sources:

$$\frac{v_2 = \int d\phi \frac{dN}{d\phi} \cos\left(2(\phi - \psi)\right)}{\int d\phi \frac{dN}{d\phi}} = \frac{\int d\phi \frac{dN^1}{d\phi} \cos\left(2(\phi - \psi)\right)}{\int d\phi \frac{dN}{d\phi}} + \frac{\int d\phi \frac{dN^2}{d\phi} \cos\left(2(\phi - \psi)\right)}{\int d\phi \frac{dN}{d\phi}}$$

• For each source:

$$\frac{v_2^i = \int d\phi \frac{dN^i}{d\phi} \cos\left(2(\phi - \psi)\right)}{\int d\phi \frac{dN^i}{d\phi}}, \qquad \therefore \quad v_2 = \frac{\sum_i N^i v_2^i}{\sum_i N^i}$$

Tension between rates and elliptic flow for QGP signal
Missing strength in the hadronic sector(?)





SOME FACTS AND SOME LEADS

- Can we improve on the hadronic rates? Baryons? Baryons +mesons? How important is bremsstrahlung?
- Early-times magnetic field effects? (Basar, Kharzeev, Skokov, PRL (2012); Basar, Kharzeev, Shuryak, arXiv: 1402.2286)
- Non-perturbative effects? Glasma effects (McLerran, Schenke, arXiv:1403.7462). See L. McLerran's talk. Semi-QGP: see S. Lin's talk.
- Is the large photon elliptic flow telling us about the dynamics?
- •Non-zero initial shear tensor? Primordial flow? Can we improve on the hydro initial states?
- Can we improve on the hydrodynamic evolution? Is the pQCD contribution really well-known?





THE "PQCD PHOTONS"



ELLIPTIC FLOW AND SPACE-TIME DYNAMICS

- In a thermal fireball picture, the net photon yield is sensitive to the value of the acceleration parameter, and to details of the initial state. The photons **do** report on the details of the dynamics.
- How uniquely determined are these? How unique is the entire evolution?



van Hees, Gale, Rapp, PRC (2011)

• Smooth fireball, Primordial flow, a slightly different set of resonances, baryons



See H. van Hees' talk

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BEYOND GLAUBER: IP-GLASMA + MUSIC EFFECT ON HADRONIC OBSERVABLES Flow harmonics reproduced up to v₅ at RHIC and LHC Distributions of v_n at LHC:





- •IP-Glasma + MUSIC provides consistent flow systematics at RHIC & LHC
- •Contains an initial flow: Investigating the effects on EM variables

Gale, Jeon, Schenke, Tribedy, Venugopalan PRL (2013)



Is the hydrodynamic modelling complete?

 In the last ~5-8 years, relativistic hydrodynamics has undergone a revolution

• 3D

- 3D Shear viscosity
- 3D Shear viscosity Fluctuating initial conditions
- 3D Shear viscosity Fluctuating initial conditions also in y
 What's left?

$$T^{\mu\nu} = -Pg^{\mu\nu} + \omega u^{\mu}u^{\nu} + \Delta T^{\mu\nu}$$

The dissipative terms:

$$\Delta T^{\mu\nu} = \eta \Big(\Delta^{\mu} u^{\nu} + \Delta^{\nu} u^{\mu} \Big) + \Big(\frac{2}{3} \eta - \zeta \Big) H^{\mu\nu} \partial_{\rho} u^{\rho} - \chi (H^{\mu\alpha} u^{\nu} + H^{\nu\alpha} u^{\nu}) Q_{\alpha}$$

No simulation incorporates all of these



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BULK VISCOSITY?

S. Weinberg, Ap. J (1971)



A. Buchel, Phys. Lett. (2008)

G. Denicol et al., PRC (2014)

Bulk viscosity vanishes in conformal fluids. QCD is only very approximately conformal:



BULK VISCOSITY EFFECTS ON PHOTONS?

Ideal photon $v_2(q_T)$

Viscous photon $v_2(q_T)$



•
$$\frac{\zeta}{s}(T)$$
 etc..

• Bulk visc. is consistent with hadronic data

J.-B. Rose, MSc 2014 (McGill)

100

X^2



0.3

0.25

0.2

MORE ON THE HYDRO MODELLING AND PHOTON PRODUCTION

$$\tau_{\pi}\dot{\pi}^{\langle\mu\nu\rangle} + \pi^{\mu\nu} == 2\eta\sigma^{\mu\nu} - \frac{4}{3}\tau_{\pi}\pi^{\mu\nu}\theta$$

- •Can the relaxation time be changed? Does this affect anything?
- •What about $\pi_0^{\mu\nu}$?



MORE ON THE HYDRO MODELLING AND PHOTON PRODUCTION, PART II



* Photons are sensitive to early time dynamics; hadrons less so

* Those extra dimensions are not typically explored in hydro

Vujanovic et al., arXiv:1404.3714



See G. Vujanovićs talk



THERMAL PHOTONS AS A THERMOMETER

Suppose a static source at temperature T:



Read off the temperature from the exponent





Suppose an expanding source at local temperature T:





 $< E \frac{d^3 n}{d^3 p} \approx E e^{-\beta \gamma E + \beta \gamma v E}$

Side view



The effective temperature (deduced from the slope) is <u>not</u> the true temperature



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STUDYING THE DIFFERENTIAL TEMPERATURE DISTRIBUTION WITH A REALISTIC FLUID-DYNAMICAL CALCULATION



WITH A FLUID-DIMMAMICAL CALCULATION

DISTRIBU

4

VING THE



THERMAL PHOTONS AS A VISCOMETER

 $\omega \frac{dR}{d^3 q} = \Gamma_0 + \frac{\pi^{\mu\nu}}{2(\epsilon + P)} \Gamma_{\mu\nu}(p,T) \qquad \text{Shen, Heinz, Paquet, Kozlov, Gale, arXiv 1308.2111}$





MAXIMIZING THE EFFECT



- * Slope of ratio vs centrality grows with viscosity
- * The ratio has stronger centrality dependence than for hadrons: photons access earlier times with larger viscous tensor
- This ratio is insensitive to sources
 with a vanishing v_n such as pre equilibrium & pQCD







WHAT ABOUT DILEPTONS?

- OAdditional degree of freedom: M and pT may be varied independently
- ^oSame approach as for photons: integrate rates with hydro



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THERMAL DILEPTON SOURCES, QGP

•HTL at zero momentum: Braaten, Pisarski and Yuan, PRL (1990)

•2-loop, p=0, E>>T: Majumder and Gale, PRC (2002)

•HTL, *M~gT*, *E>T*: Aurenche, Gélis, Moore, Zaraket, JHEP (2008)

•HTL at finite momentum:

• Non-perturbative calculation:



No single calculation covers the entire dilepton kinematical phase space

M. Laine, JHEP **11**, 120 (2013) $M^2 \gtrsim (\pi T)^2, p \neq 0$

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THERMAL DILEPTON SOURCES, HG

- HG contribution: calculate the in-medium vector spectral density:
 - Many-Body approach with hadronic effective Lagrangians
 Rapp and Wambach, ANP (2000)
 - Empirical evaluation of the vector mesons forwardscattering amplitudes

$$\Pi_{ab}(E,p) = -4\pi \int \frac{d^3k}{(2\pi)^3} n_b(\omega) \frac{\sqrt{s}}{\omega} f_{ab}^{\text{c.m.}}(s)$$

- E. Shuryak, NPA (1991)
 Eletsky, Ioffe, Kapusta (1999)
 Vujanovic, Gale (2009)
- Chiral Reduction formulae
 Yamagishi, Zahed (1996)

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DILEPTONS, THE STORY AS OF A FEW YEARS AGO





Dileptons, some recent results from STAR

STAR



THERMAL DILEPTON V₂ WITH VISCOUS EFFECTS DILEPTON V₂? [R. CHATTERJEE ET AL., PRC (2007)]



G. Vujanovic et al.,PRC (2014)



CONCLUSIONS

- The status of EM rates and their integration in fluid dynamical models is still in flux
- The fluid dynamical paradigm is not yet established
- Photon v₂ is sensitive to the EOS, and to various hydro parameters such as viscosity, and initial conditions (time and FICs). One must be consistent with hadronic data
- Photons and dileptons are sensitive to non-equilibrium effects (in addition to shear viscosity)
- Current v_2 data: new physics? Measuring photon $v_{3,}\,v_n$ at RHIC and LHC will help complete this picture
- Physics in dilepton vn
- Jet-plasma photons need to be included: MARTINI
- Known unknowns: pre-equilibrium radiation





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