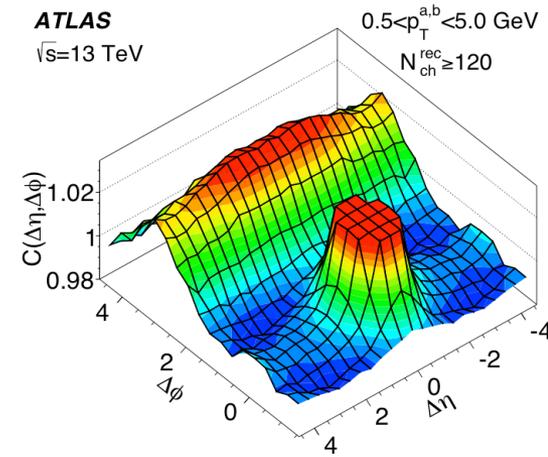
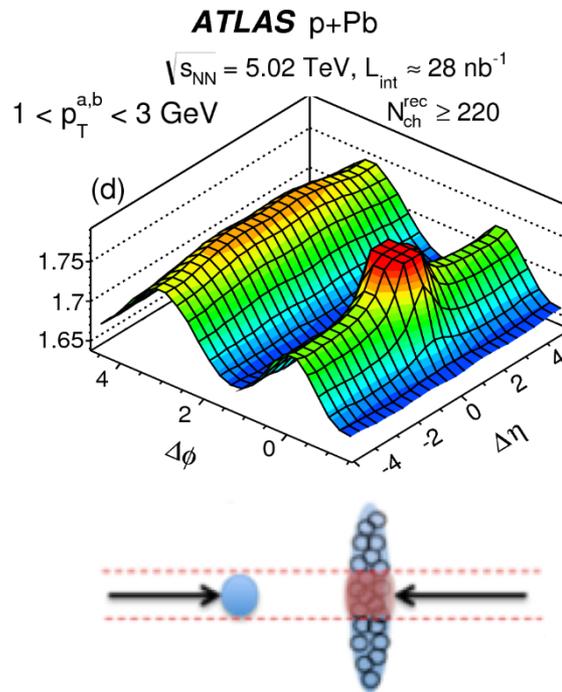
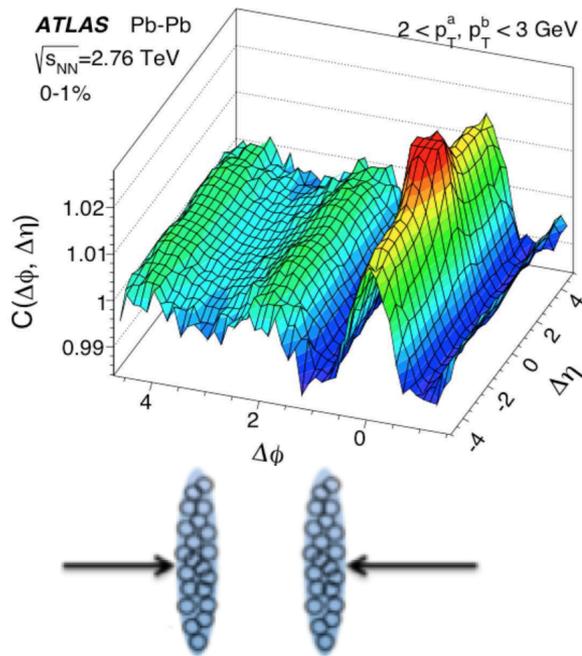


The role of longitudinal correlations and fluctuations :Exp

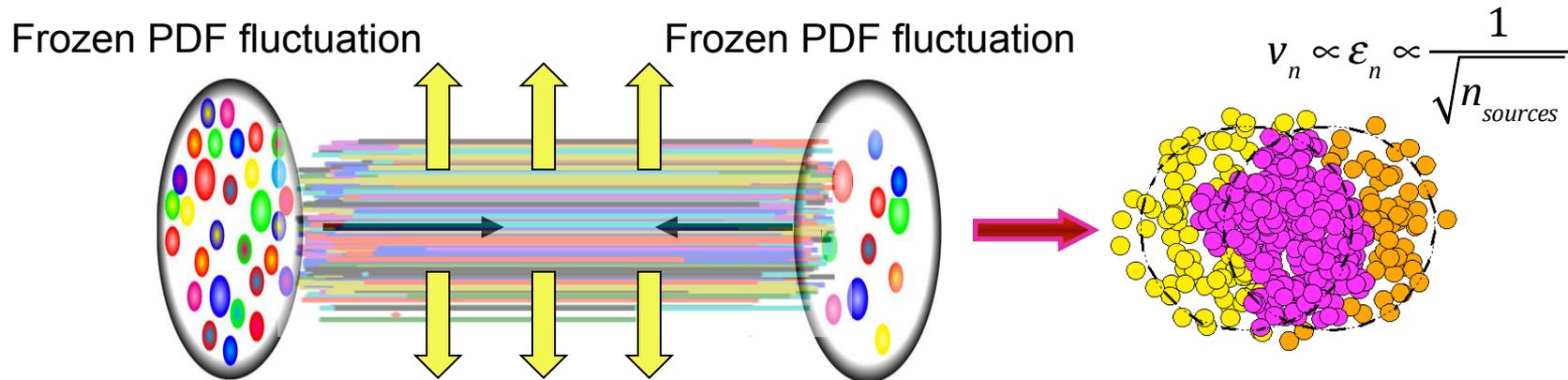
Jiangyong Jia

Stony Brook University & Brookhaven National Laboratory

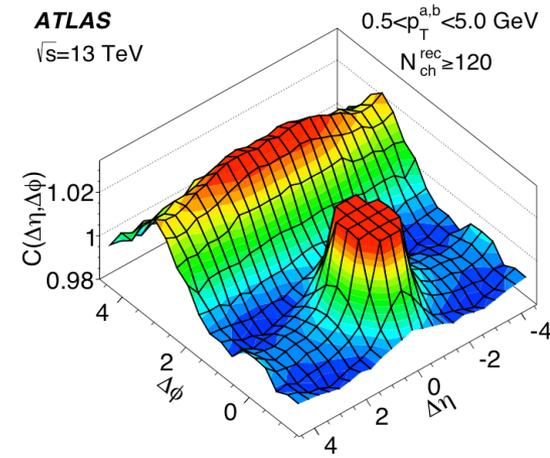
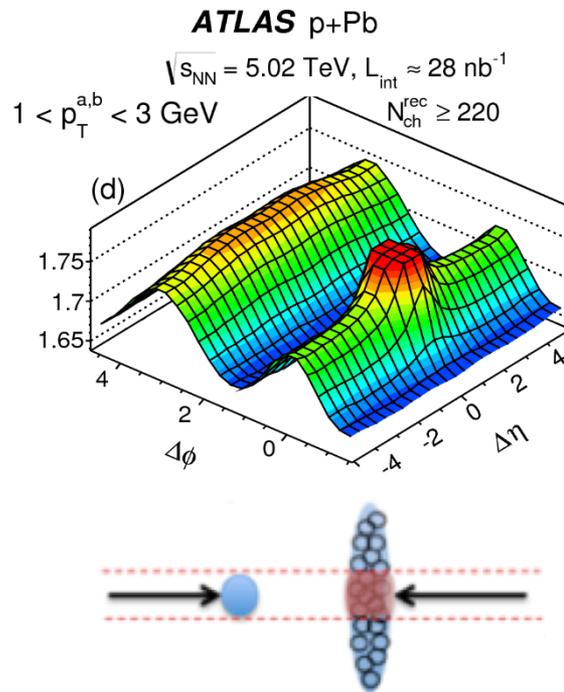
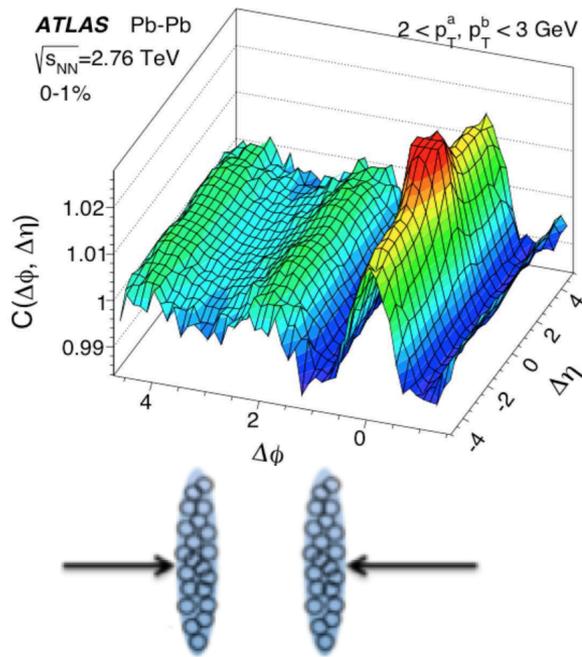
Initial Stages 2016



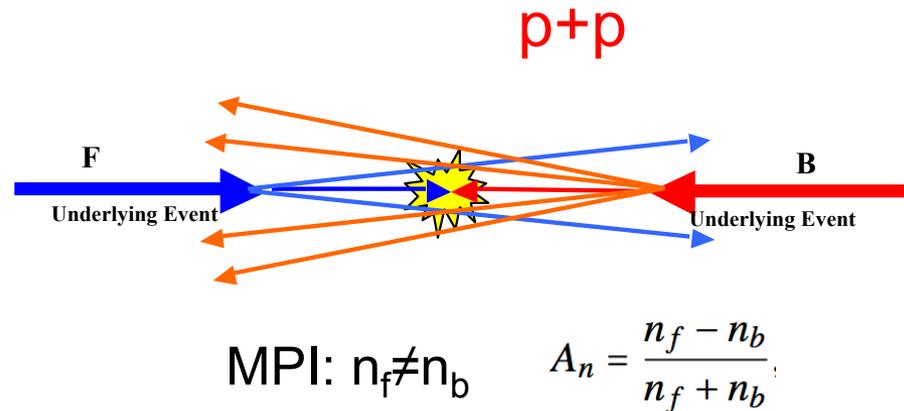
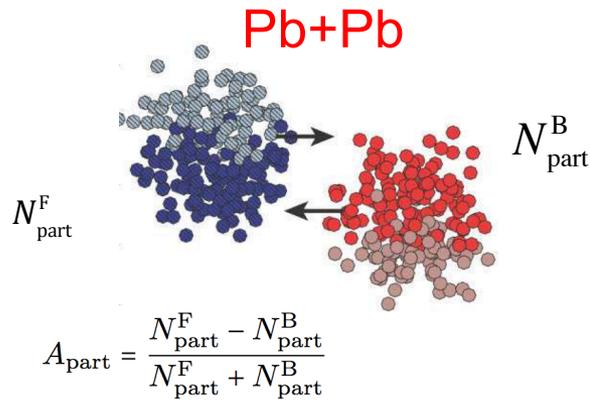
Nature of sources seeding these long-range collective ridges?



**How many sources, their sizes & transverse distribution?
 they transport in rapidity?**



Nature of sources seeding these long-range collective ridges?

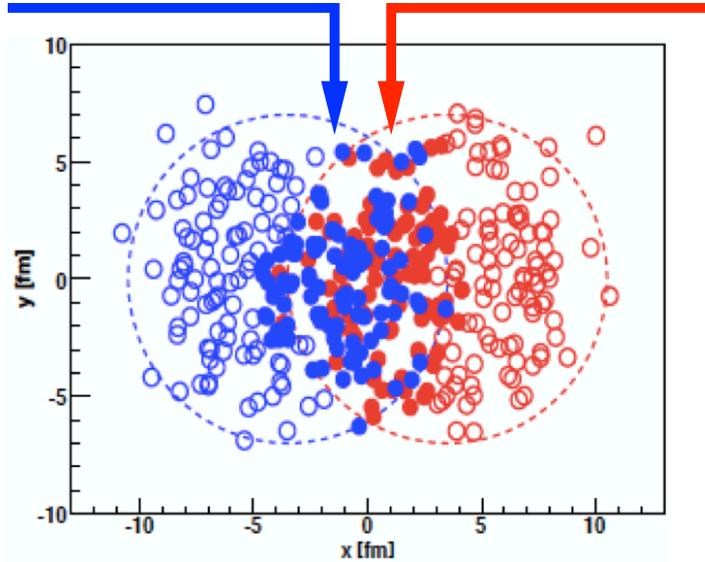


Forward-backward flow/multiplicity correlations provide a handle

Three types of longitudinal correlations

Fluctuation of sources in two nuclei \rightarrow fluc. of size and transverse-shape

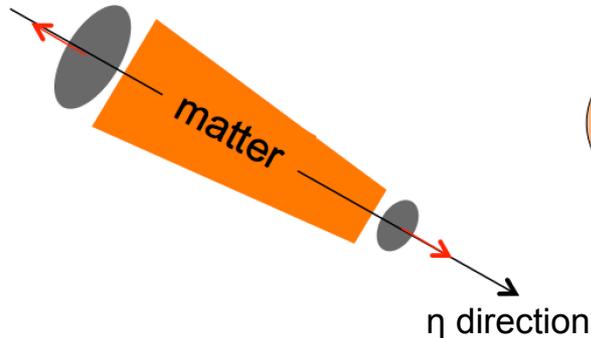
$$N_{\text{part}}^F \quad \varepsilon_n^F e^{in\Psi_n^F}$$



$$N_{\text{part}}^B \quad \varepsilon_n^B e^{in\Psi_n^B}$$

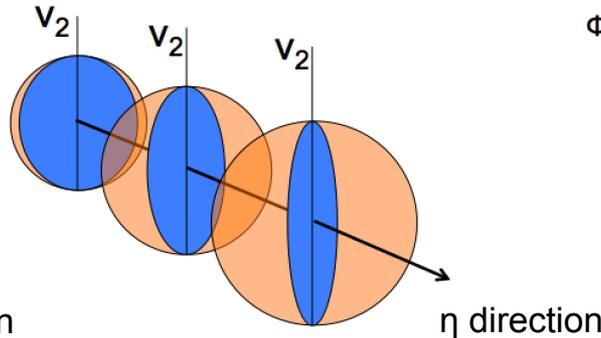
Consequences:

(a) $N_{\text{part}}^F \neq N_{\text{part}}^B$



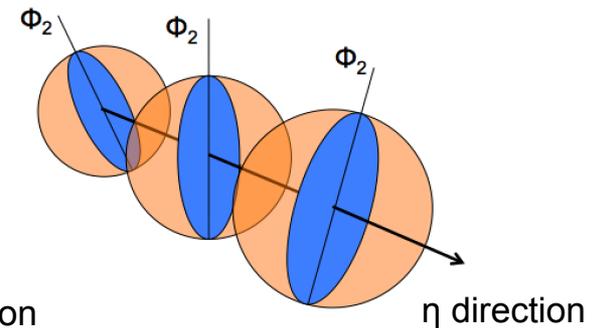
Asymmetry in multiplicity

(b) $\varepsilon_2^F \neq \varepsilon_2^B$



**Asymmetry in flow magnitude
not a de-correlation**

(c) $\Psi_2^F \neq \Psi_2^B$

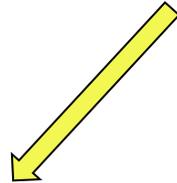


Torque/twist of flow plane

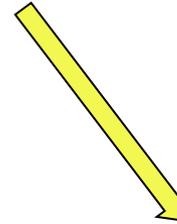
Two-particle correlation observables

Most general form in angular space: $C(\eta_1, \eta_2, \Delta\phi)$

$$C(\eta_1, \eta_2, \Delta\phi) = \underline{C_N(\eta_1, \eta_2)} \left[1 + 2 \sum_n \underline{V_{n\Delta}(\eta_1, \eta_2)} \cos n\Delta\phi \right]$$



FB Multiplicity fluctuation



FB flow fluctuation

$$C_N(\eta_1, \eta_2) = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle}$$

ATLAS observable

Driven by N_{part} asymmetry

$$V_{n\Delta}(\eta_1, \eta_2) = \langle v_n(\eta_1)v_n(\eta_2) \cos n[\Phi_n(\eta_1) - \Phi_n(\eta_2)] \rangle$$

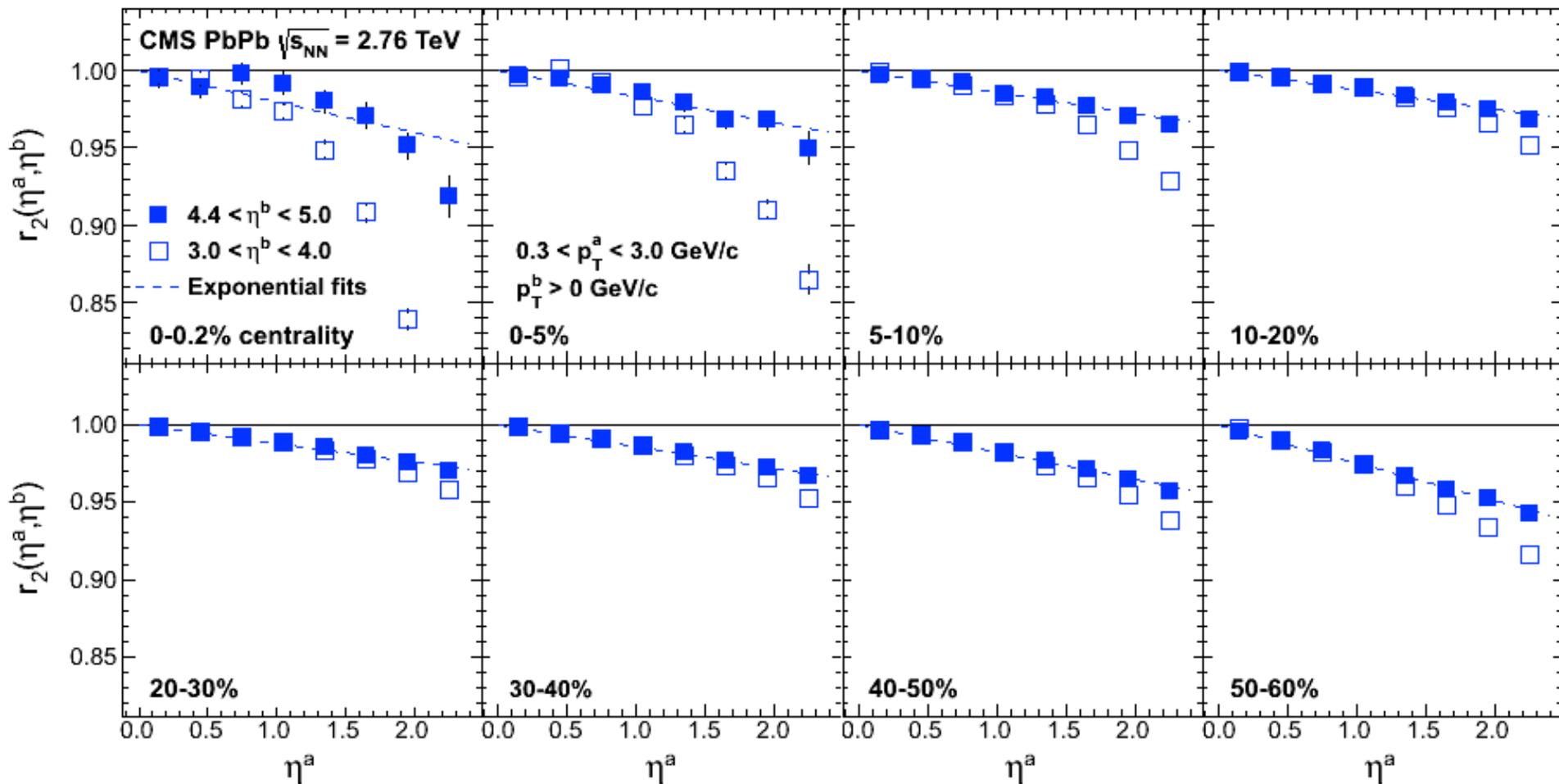
$$\text{CMS observable: } r(\eta, \eta_{\text{ref}}) = \frac{V_{n\Delta}(-\eta, \eta_{\text{ref}})}{V_{n\Delta}(\eta, \eta_{\text{ref}})}$$

Driven by twist & asymmetry of ε_n

2nd-order flow in PbPb

$$r_n(\eta^a, \eta^b) \equiv \frac{V_{n\Delta}(-\eta^a, \eta^b)}{V_{n\Delta}(\eta^a, \eta^b)}$$

6

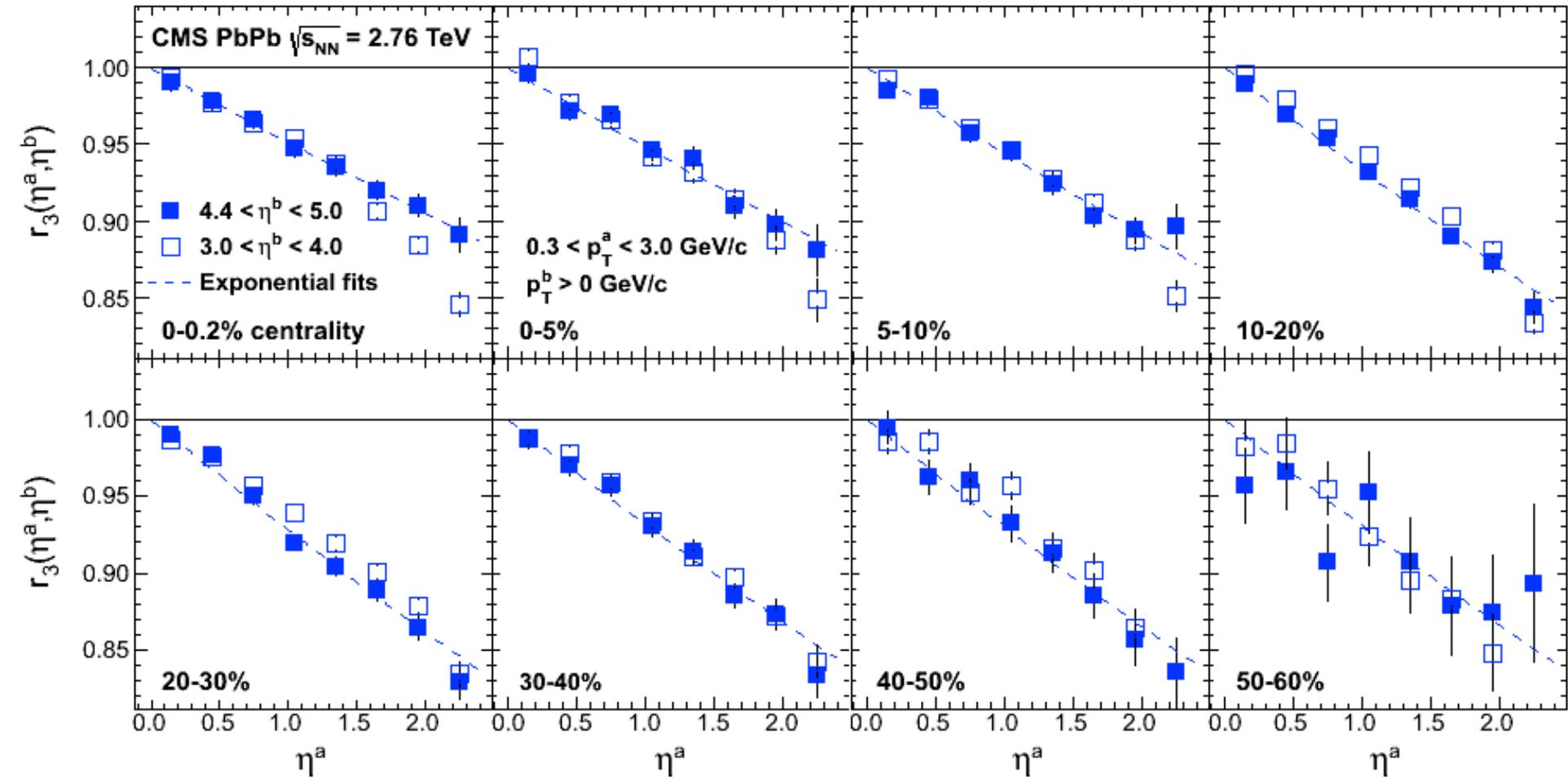


- Linear function except in most central collisions
- Slope decreases then increases from central to peripheral

3rd-order flow in PbPb

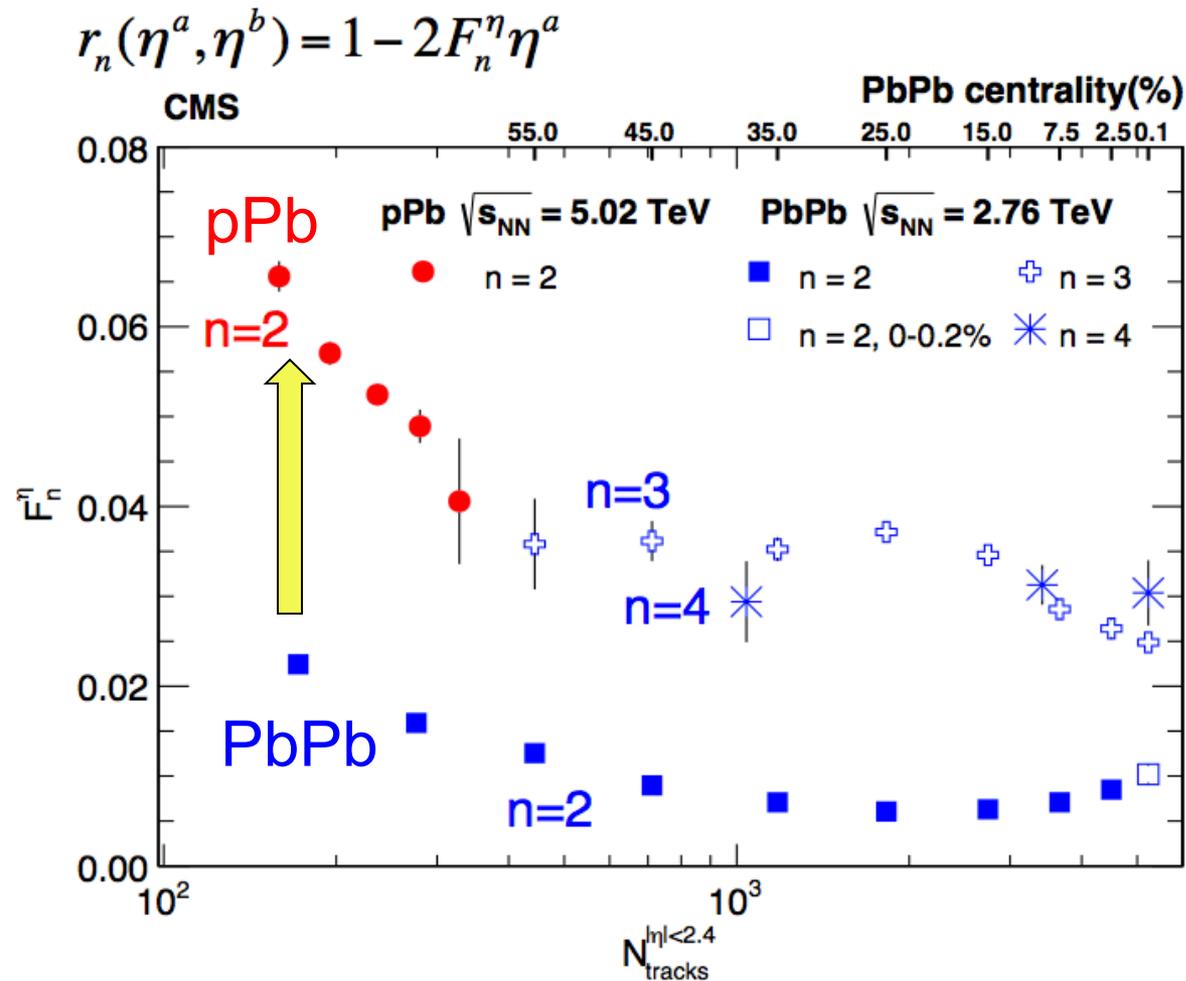
$$r_n(\eta^a, \eta^b) \equiv \frac{V_{n\Delta}(-\eta^a, \eta^b)}{V_{n\Delta}(\eta^a, \eta^b)}$$

7



■ Slope \sim independent of centrality

Compared PbPb with pPb

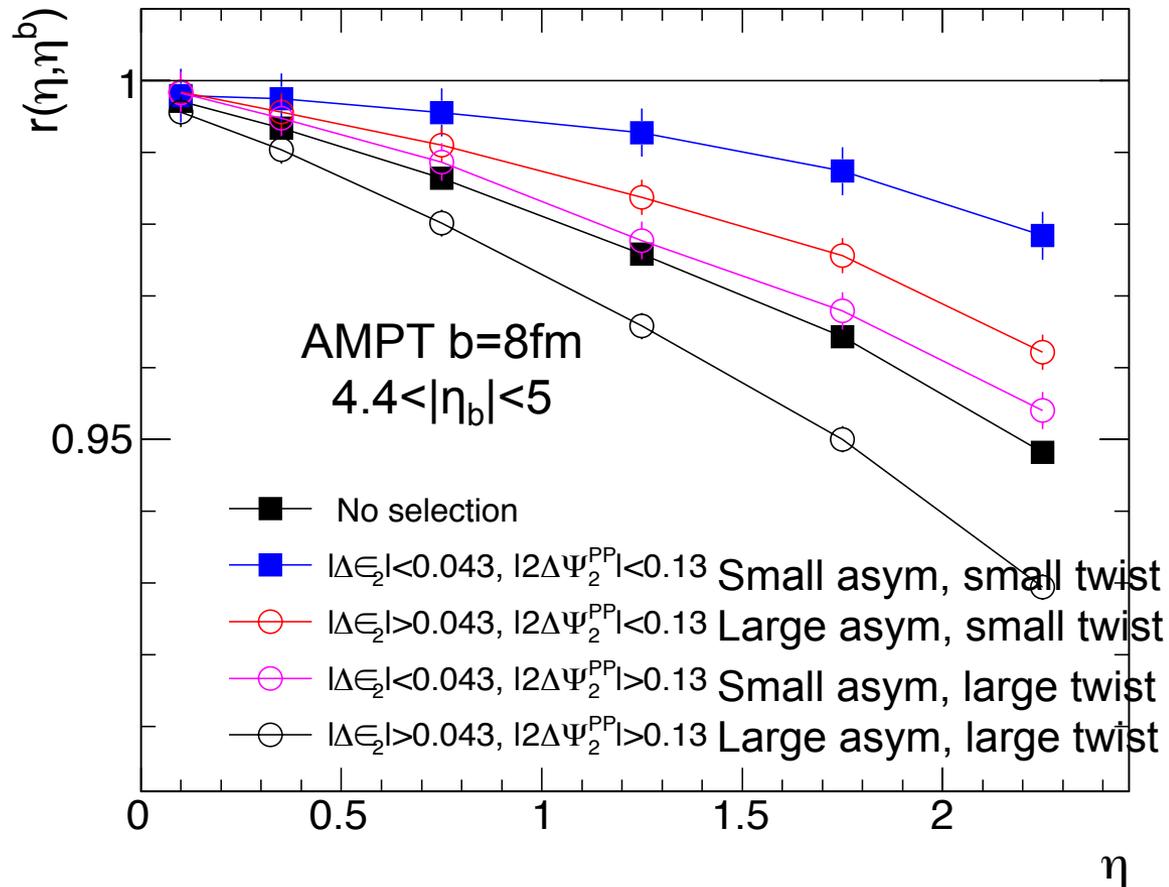


Stronger effect in pPb! require sub-nucleonic dof.

What about HM pp?

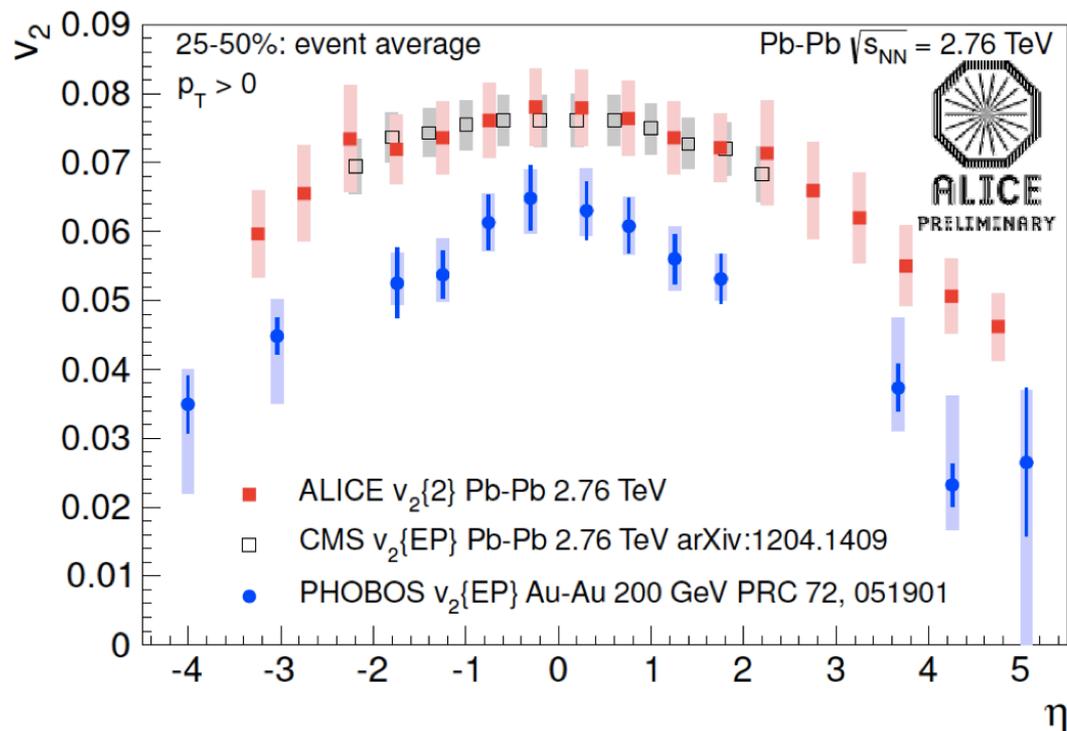
Separate asymmetry and twist contributions

- Select asymmetry and twist based on eccentricity vector in AMPT
 - Cut on asymmetry : $\Delta\varepsilon_2 = \varepsilon_2^F - \varepsilon_2^B$, cut on twist: $\Delta\Psi_2 = \Psi_2^F - \Psi_2^B$



asymmetry contribution $> 50\%$ of the twist contribution.

Revisit the $v_n(\eta)$ measurement



- Relies on 2PC & factorization assumption: $V_{n\Delta}(\eta_1, \eta_2) = v_n(\eta_1)v_n(\eta_2)$.

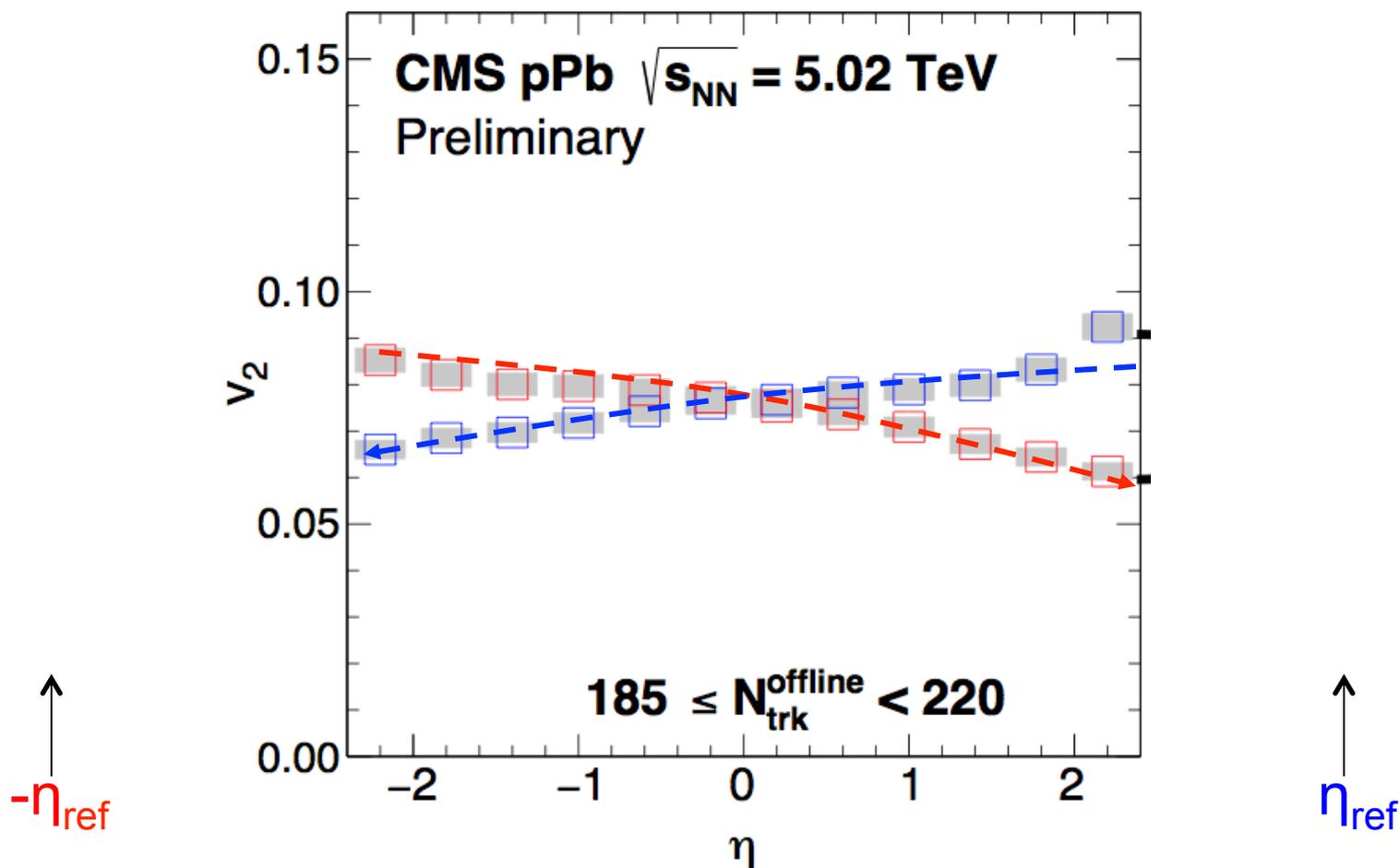
- When quoting $v_n(\eta)$, don't forget the reference particle, e.g. in SP method:

- Distinguish different components of η dependence $v_n(\eta) \equiv \sqrt{\frac{V_{n\Delta}(\eta, \eta_{ref})}{V_{n\Delta}(\eta_{ref}, -\eta_{ref})}}$

- Intrinsic $v_n(\eta)$
- Relative fluct. between $v_n(\eta_1)$ and $v_n(\eta_2)$
- Event-plane decorrelation, $\Psi_n(\eta_1) \neq \Psi_n(\eta_2)$

Hydro calc need to include these effects

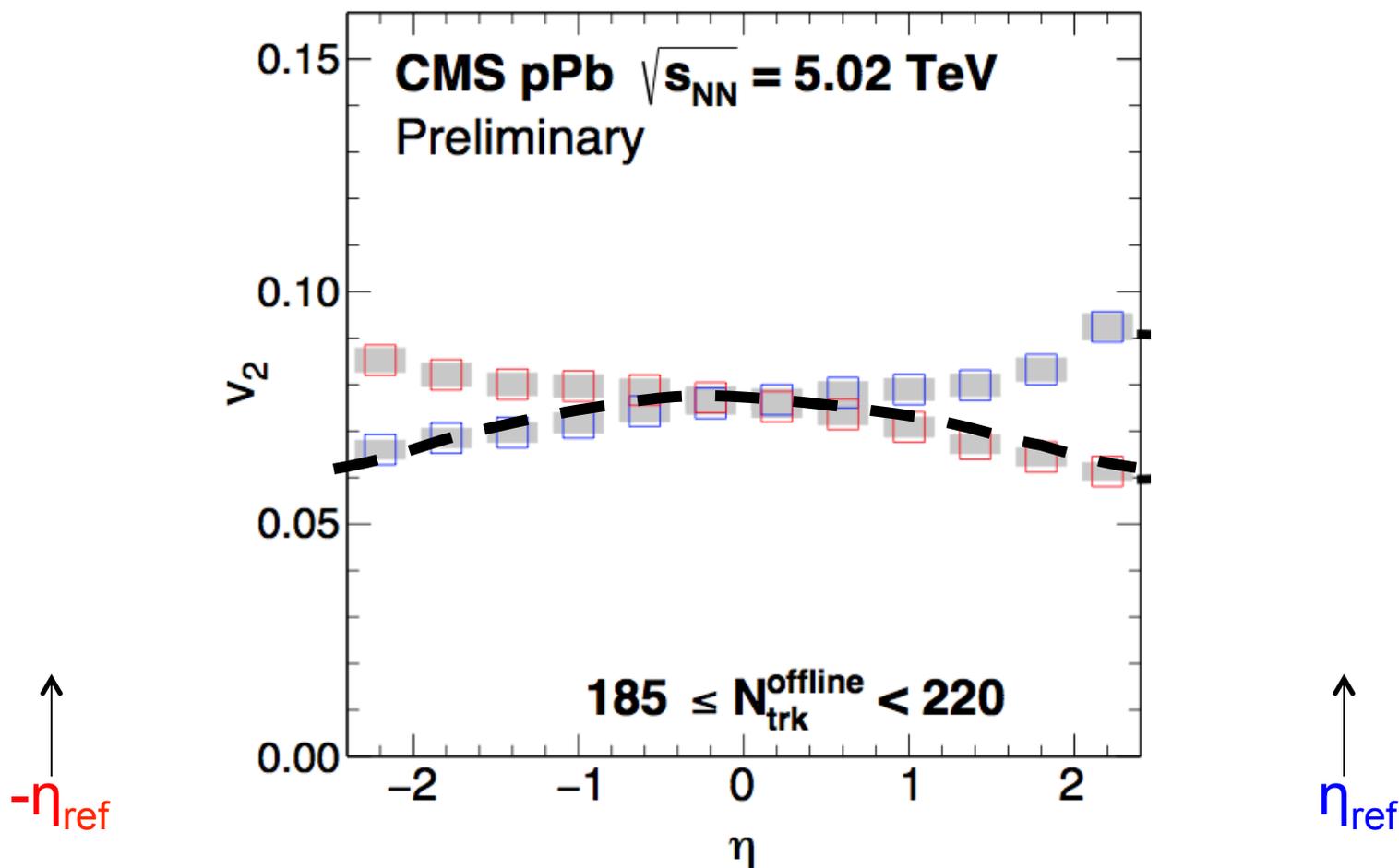
The fallacy of factorization assumption in η



Observation: v_n always decreases away from reference particle

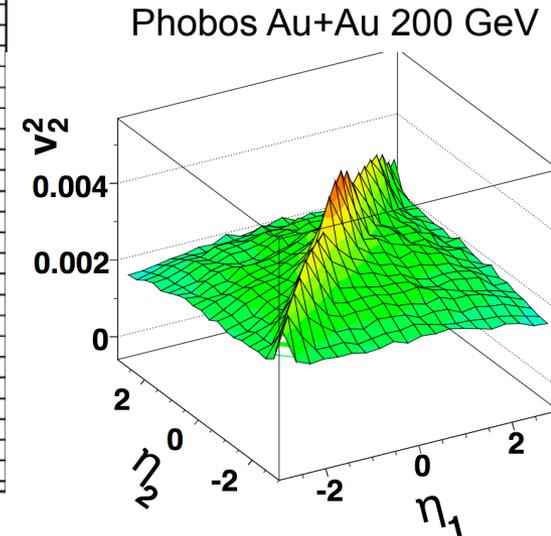
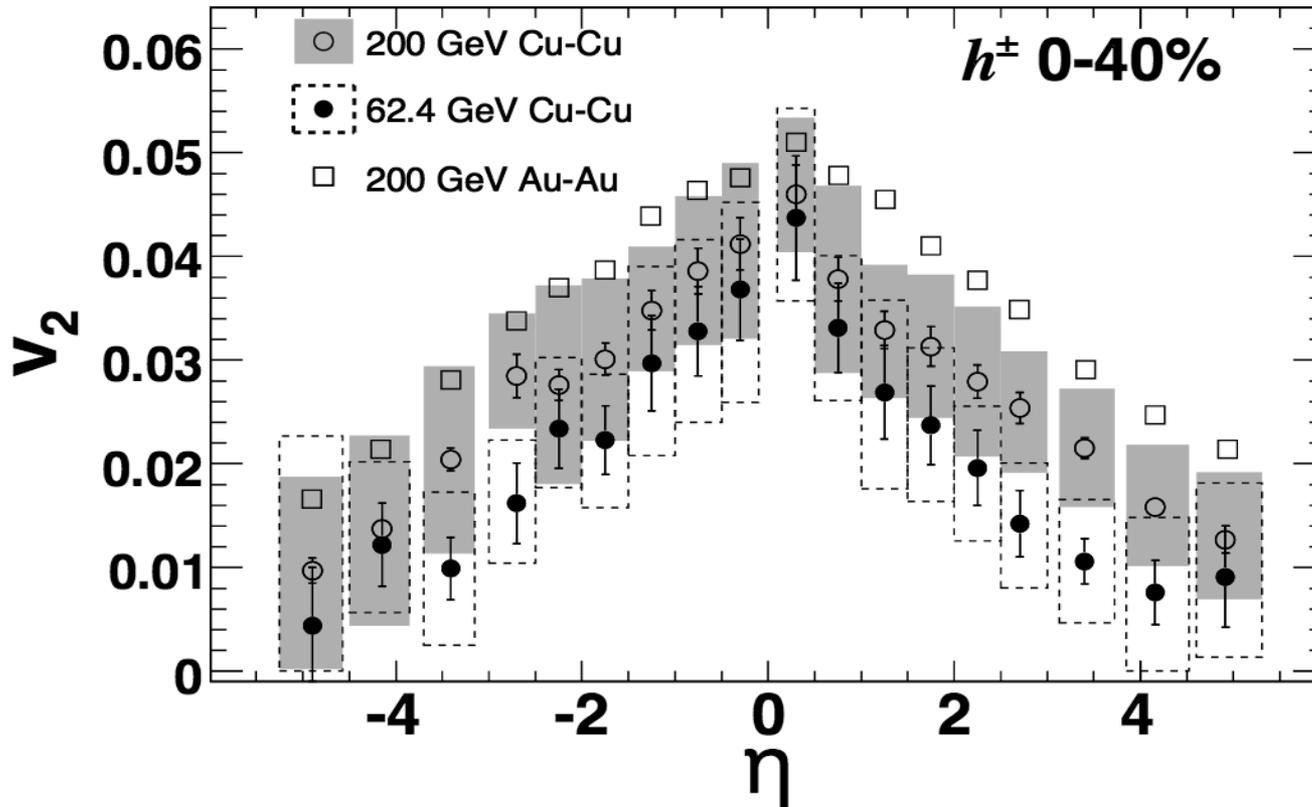
The fallacy of factorization assumption in η

12



Observation: v_n always decreases away from reference particle
symmetrized result is smaller than truth

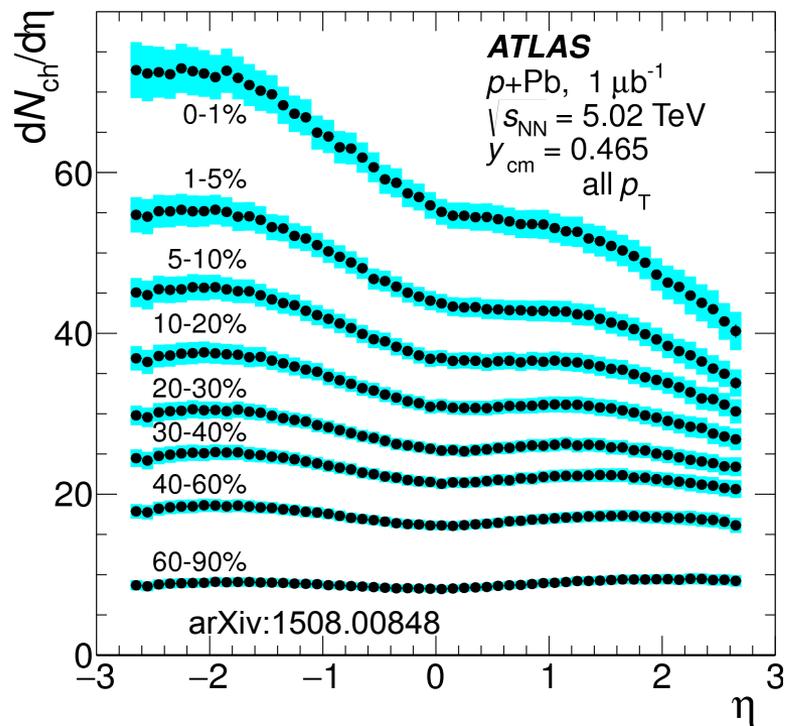
Stronger bias at RHIC



- Measure $V_{n\Delta}(\eta_1, \eta_2)$ instead of only the factorized form!
 - Systematic separation of the short-range and various components of flow.
 - Complete information on collectivity in 3+1D.

0th-order: FB multiplicity asymmetry

- $dN/d\eta$ shape in pPb reflects asymmetry in num. of F-B sources

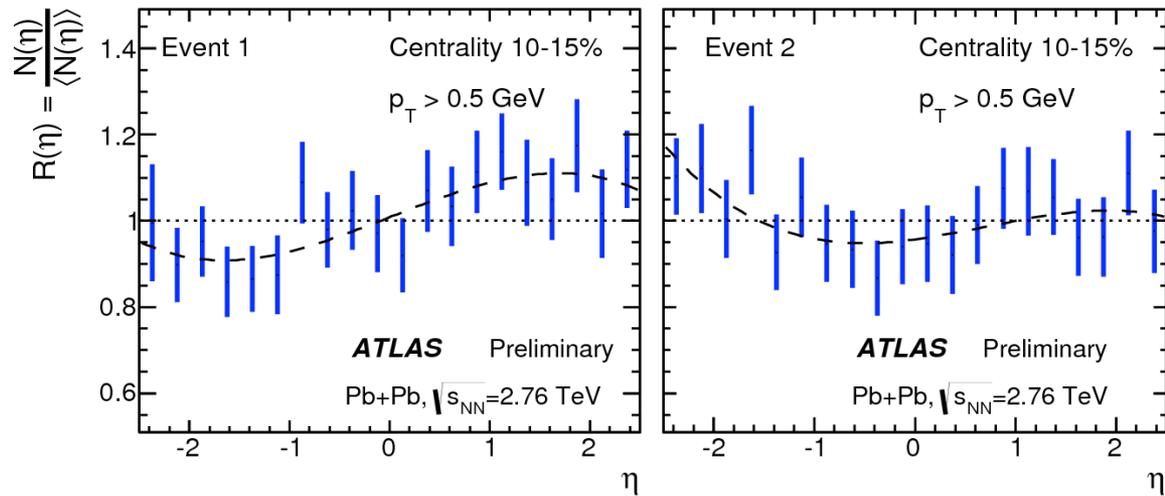


Measure FB asymmetry fluctuation event-by-event?

Pseudorapidity correlation function

Single particle distribution

$$R_S(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle}$$



$$C = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} = \langle R_S(\eta_1)R_S(\eta_2) \rangle_{events}$$

\swarrow \nearrow
 Mixed events

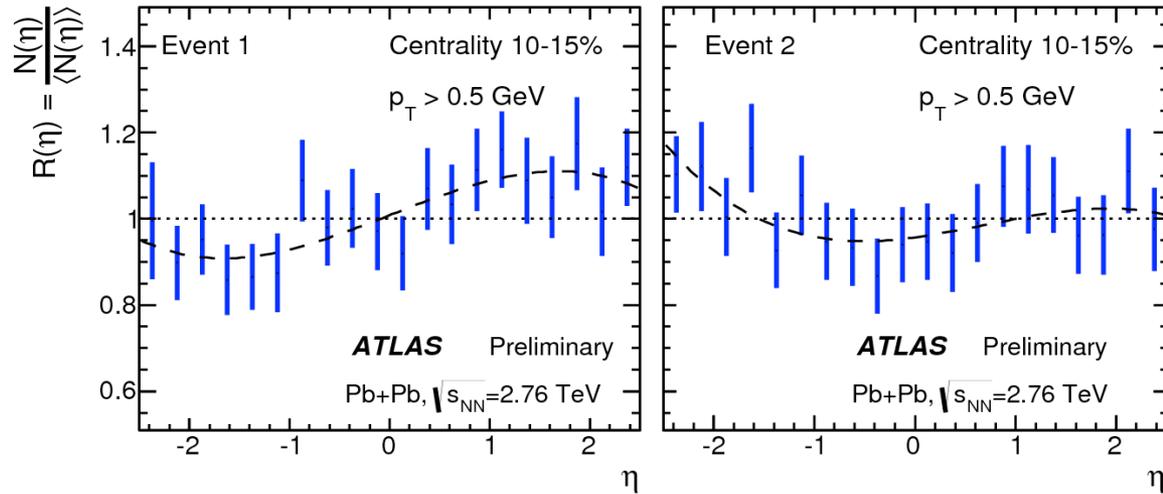
Disentangles **statistical** fluctuation from **dynamical** fluctuation

Can also do multi-particle correlations: Bzdak, Bozek, Broniowski 1509.02967, 1509.04124

Leading-order contribution

Single particle distribution

$$R_S(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle} \approx 1 + a_1 \eta$$

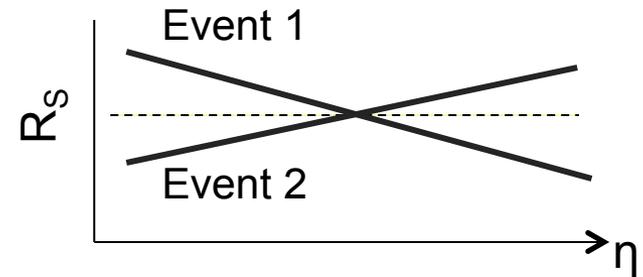


$$C = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} = \langle R_S(\eta_1)R_S(\eta_2) \rangle_{events}$$

Mixed events

$$\approx 1 + \langle a_1 \eta_1 a_1 \eta_2 \rangle$$

$$= 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$



Disentangles **statistical** fluctuation from **dynamical** fluctuation

Can also do multi-particle correlations: Bzdak, Bozek, Broniowski 1509.02967, 1509.04124

Properties of multiplicity correlation

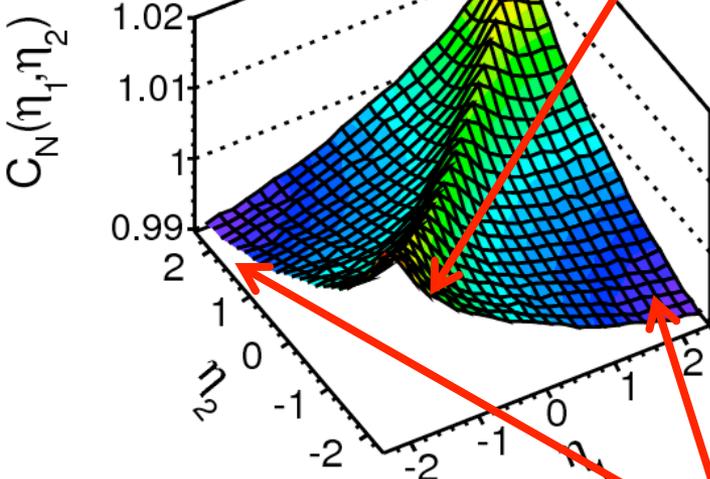
$$C_N = 1 + \delta_{SRC} + \delta_{LRC}$$

$$p_T > 0.2 \text{ GeV}$$

$$100 \leq N_{ch}^{rec} < 120$$

ATLAS Preliminary

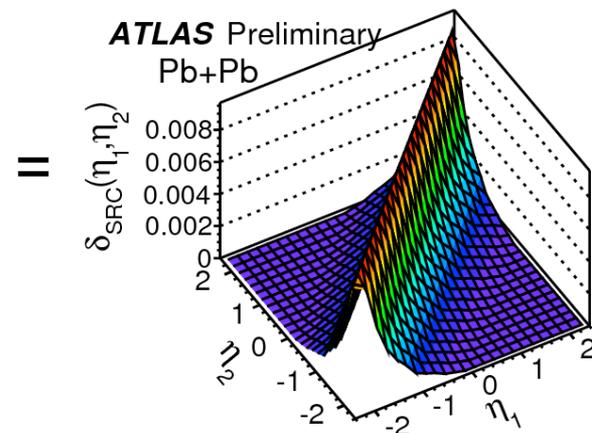
Pb+Pb



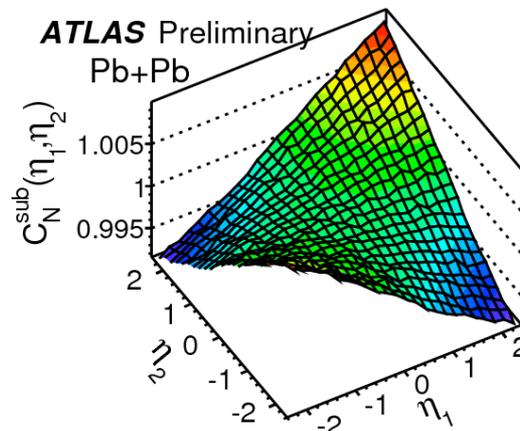
Short-range correlation δ_{SRC}

$$\Delta\eta = \eta_1 - \eta_2 \sim 0$$

Long range correlation δ_{LRC}

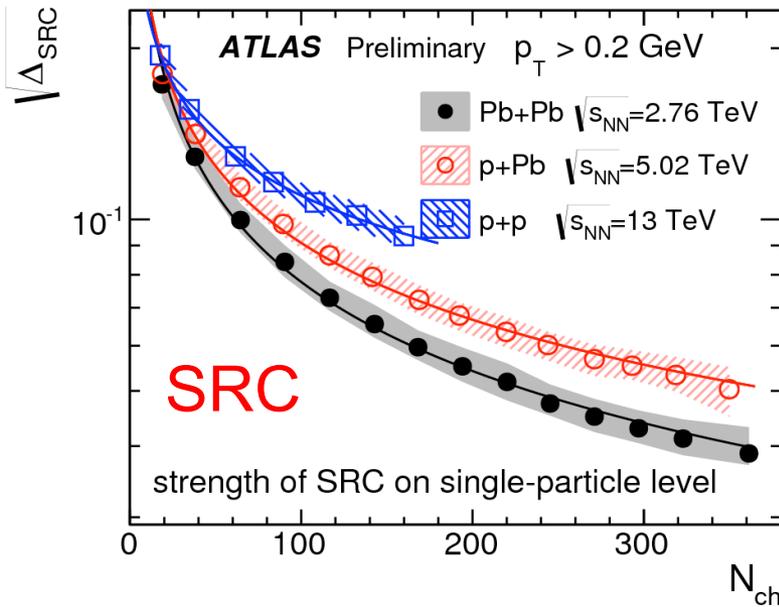


$$\Delta_{SRC} = \frac{\int \delta_{SRC}(\eta_1, \eta_2) d\eta_1 d\eta_2}{4Y^2}$$



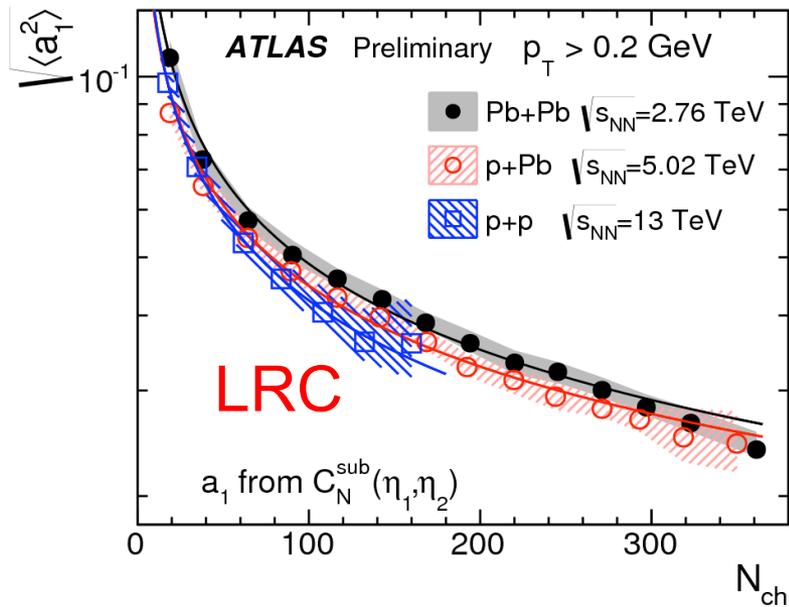
See Mingliang Zhou's talk

Consistent with $\approx 1 + \langle a_1^2 \rangle \eta_1 \eta_2$



SRC controlled by num. of sources

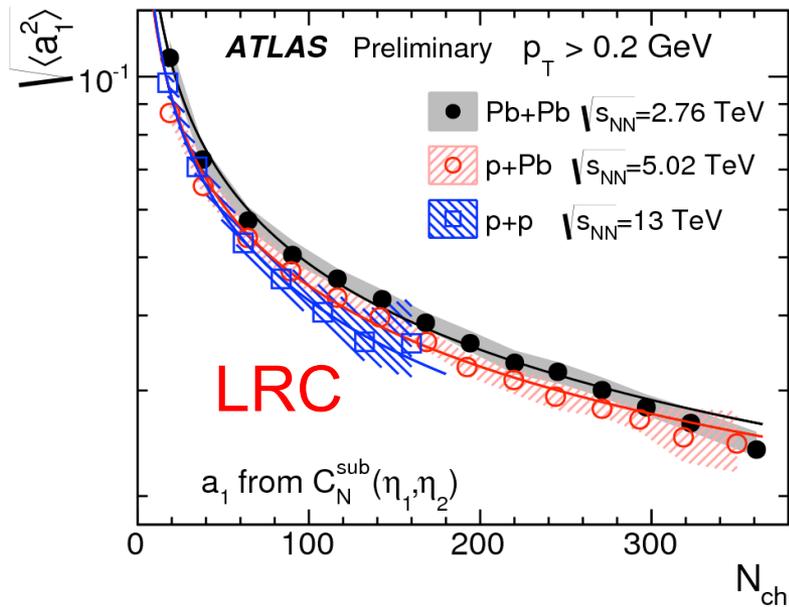
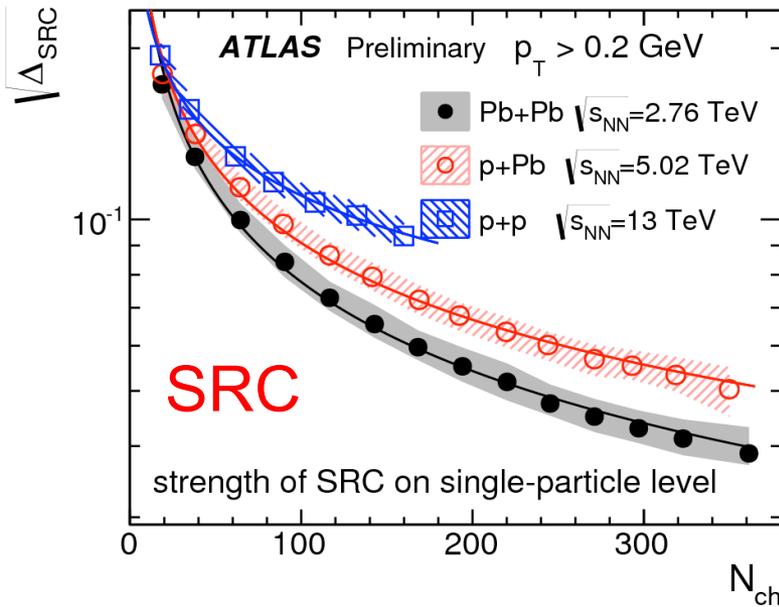
$$n = n_f + n_b \propto N_{ch}$$



LRC controlled by FB asymmetry of sources

$$A_n = \frac{n_f - n_b}{n_f + n_b} \quad \langle a_1^2 \rangle \propto \langle A_n^2 \rangle$$

Expect $1/\sqrt{N}$ for independent-source emission



SRC controlled by num. of sources

$$n = n_f + n_b \propto N_{ch}$$

LRC controlled by FB asymmetry of sources

$$A_n = \frac{n_f - n_b}{n_f + n_b} \quad \langle a_1^2 \rangle \propto \langle A_n^2 \rangle$$

Expect $1/\sqrt{N}$ for independent-source emission

■ Fit with c/N_{ch}^α

	Pb+Pb	p+Pb	pp
α for $\sqrt{\Delta_{SRC}}$	0.505 ± 0.011	0.450 ± 0.010	0.365 ± 0.014
α for $\sqrt{\langle a_1^2 \rangle}$	0.454 ± 0.011	0.433 ± 0.014	0.465 ± 0.018

- SRC: more pair/source for smaller system
- LRC: $1/\sqrt{N}$ behavior independent of collision system

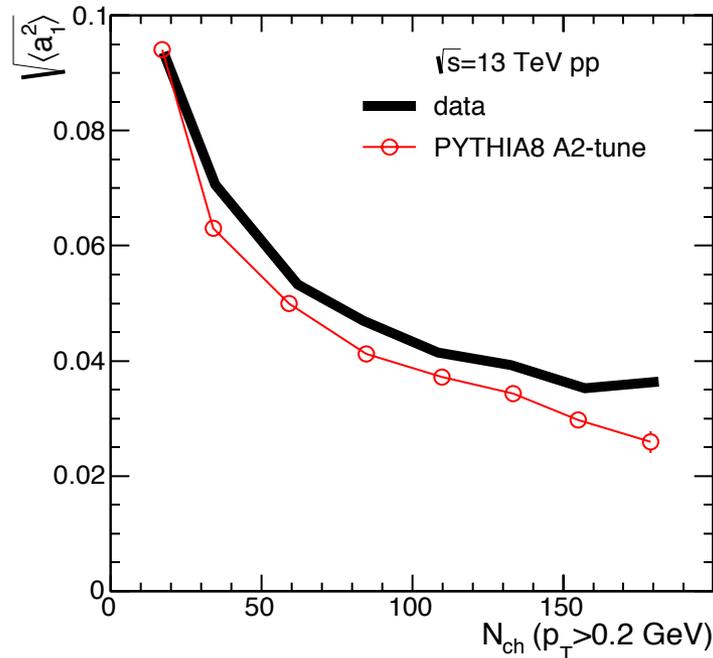
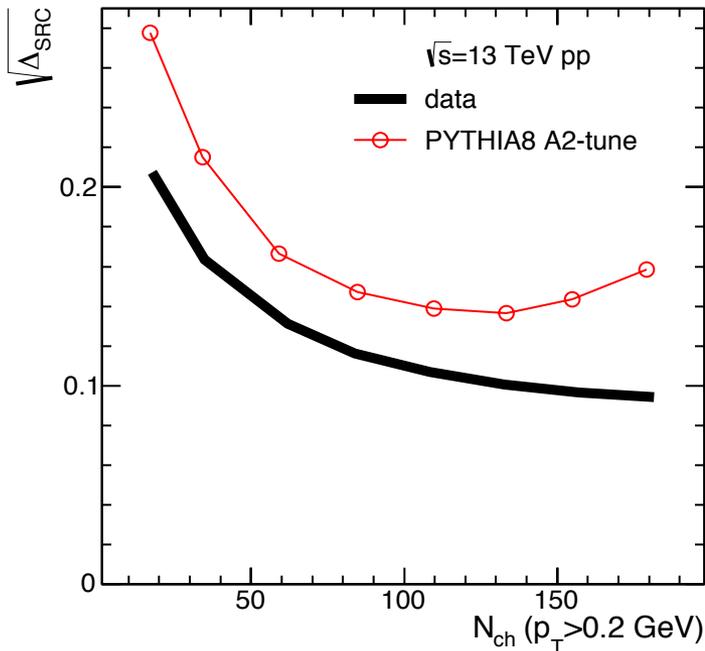
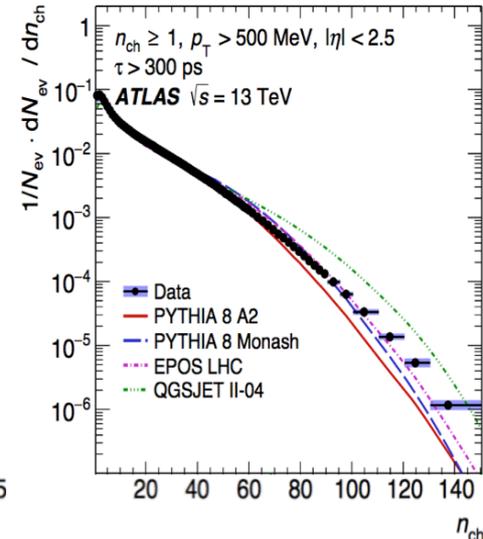
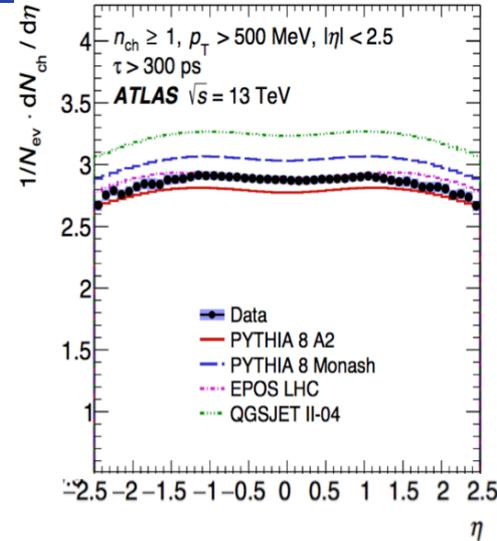
Compare with PYTHIA8 and EPOS-LHC

- Tuned to $dN/d\eta$ and N_{ch} distribution via MPI



Models:

- Over-estimate the SRC
- Under-estimate the LRC

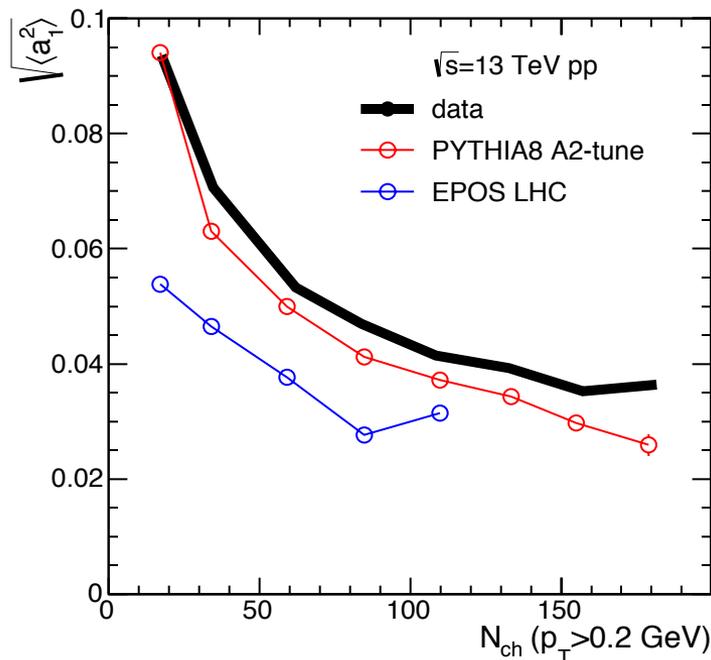
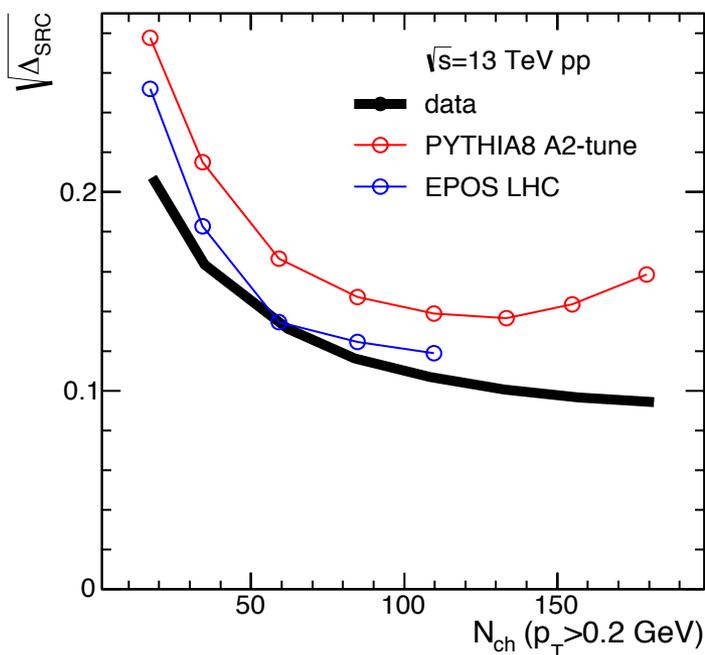
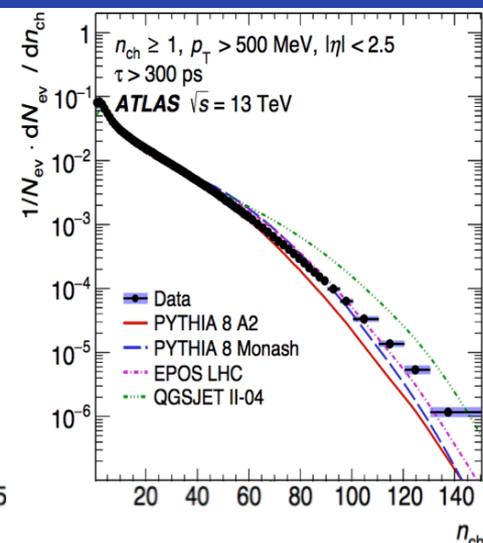
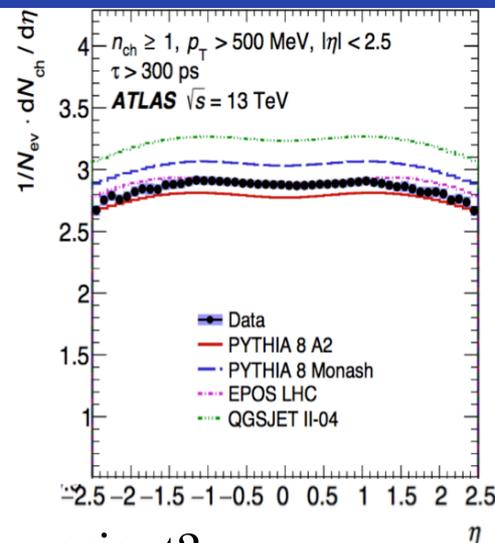


Compare with PYTHIA8 and EPOS-LHC

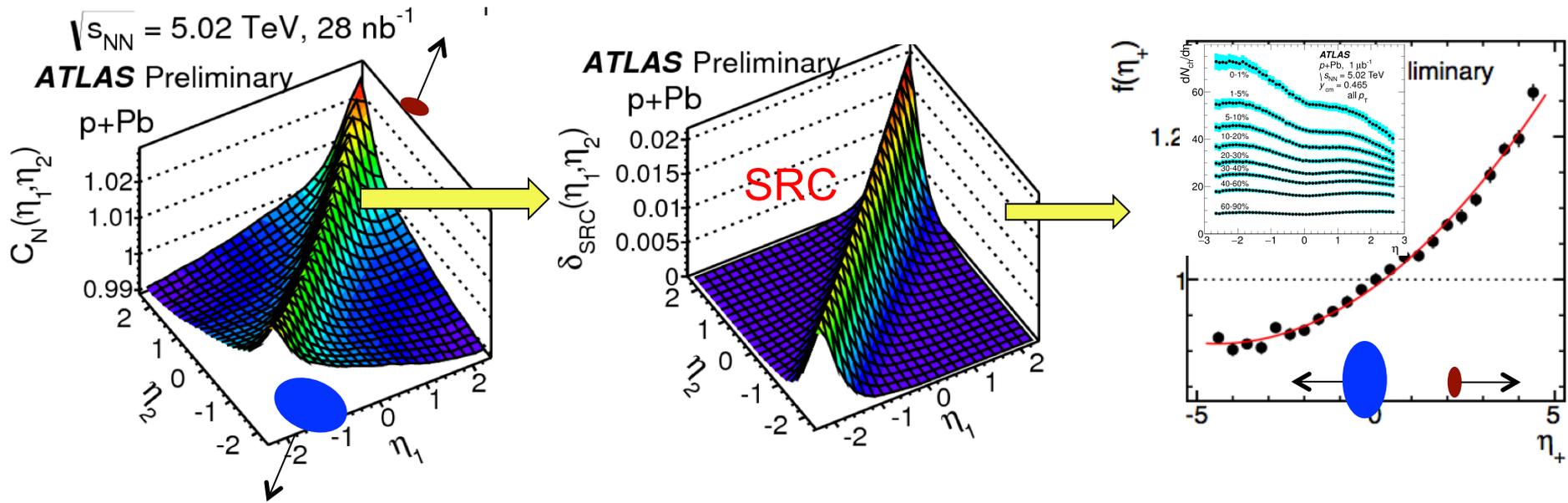
- Tuned to $dN/d\eta$ and N_{ch} distribution via MPI 

Models:

- Over-estimate the SRC
- Under-estimate the LRC
- LRC in EPOS is very small, boost invariant?

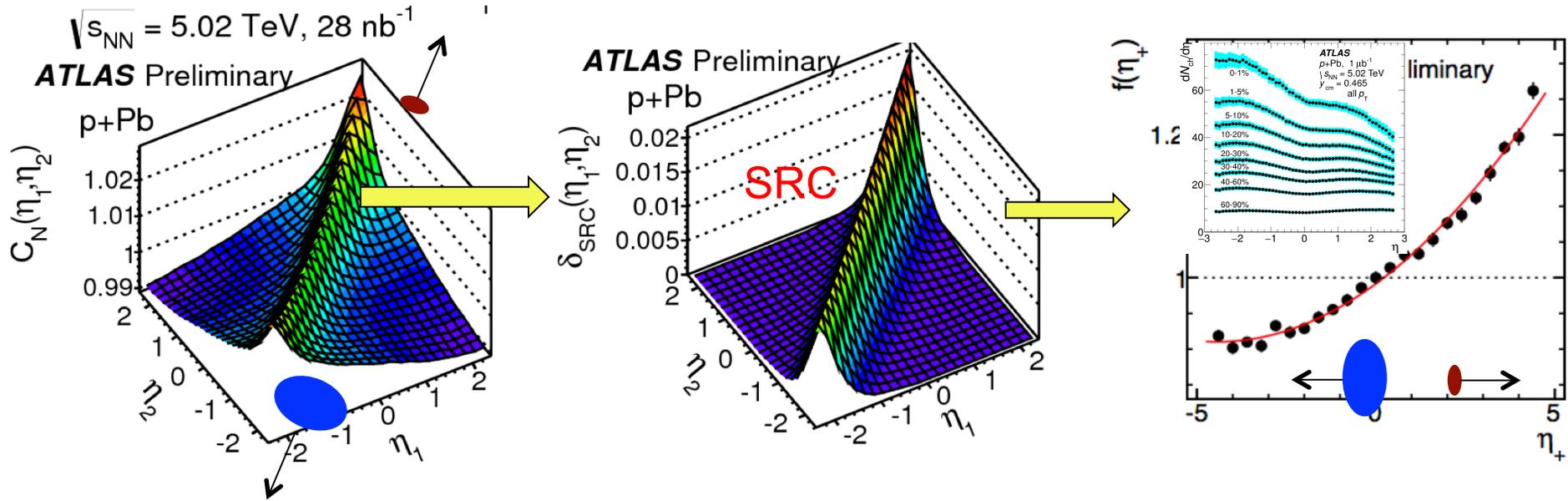


SRC and $dN/d\eta$



Asymmetry entirely due to SRC \rightarrow larger on proton-going side!

SRC and $dN/d\eta$



Asymmetry entirely due to SRC → larger on proton-going side!

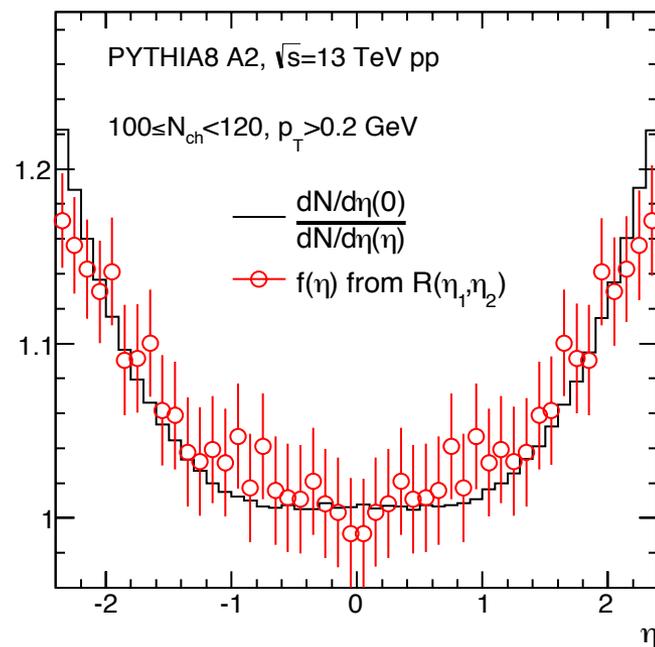
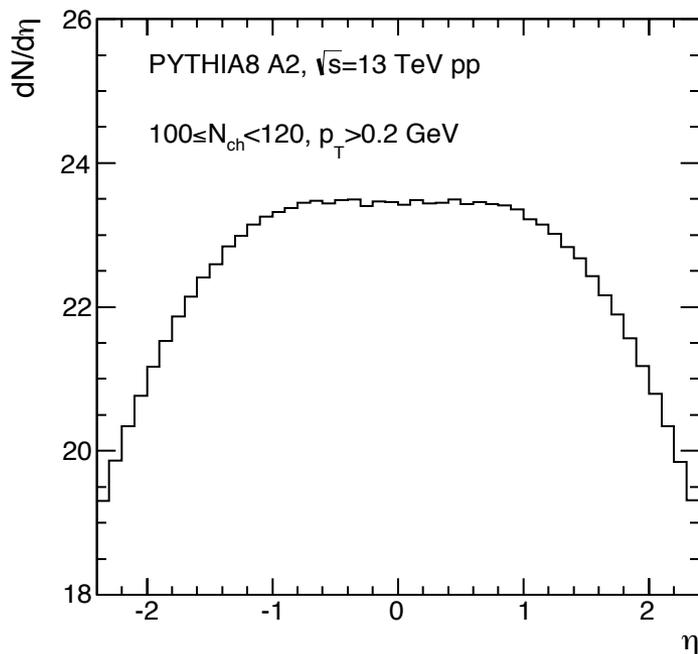
Assume n_s sources at η , each source produce m particles,

$$\text{SRC at given } \eta \text{ scale as } \approx \frac{n_s m^2}{(n_s m)^2} = \frac{1}{n_s} \propto \frac{1}{dN/d\eta}$$

Can use SRC to infer $dN/d\eta$ shape!

Verify the idea with PYTHIA

- Calculate the $f(\eta)$ from CF and compare to actual $dN/d\eta(0)/dN/d\eta(\eta)$
 - Reproducing the $dN/d\eta$ shape
 - Can use 2PC method to measure $dN/d\eta$ -shape, small experimental systematics, albeit with assumption that cluster size independent of η .



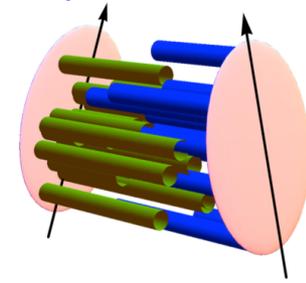
- Longitudinal correlations provide info on non-boost-invariant initial conditions & rapidity transports in pp, pA and AA collisions
- Longitudinal flow correlations
 - Consistent with rapidity-dependent mixing of initial condition controlled by projectile and target sources.
 - Important to separate different components of flow
 - They need to be properly included in all 3+1D ebye hydro models
- Longitudinal multiplicity correlations
 - Long-range correlations scale as $c/\sqrt{N_{\text{ch}}}$ in dependent of collision system
 - Information on the particle production sources?

See Mingliang's talk for more experimental details

Outlook I

■ Measure $V_{n\Delta}(\eta_1, \eta_2) = \langle v_n(\eta_1)v_n(\eta_2)\cos n[\Phi_n(\eta_1) - \Phi_n(\eta_2)] \rangle$ in “full” η space

- Carry the same measurement in HM pp, pPb
- Systematic separation of SRC and components of flow.
- Clarify the longitudinal structures of the initial condition.



Bozek et al., arXiv:1011.3354

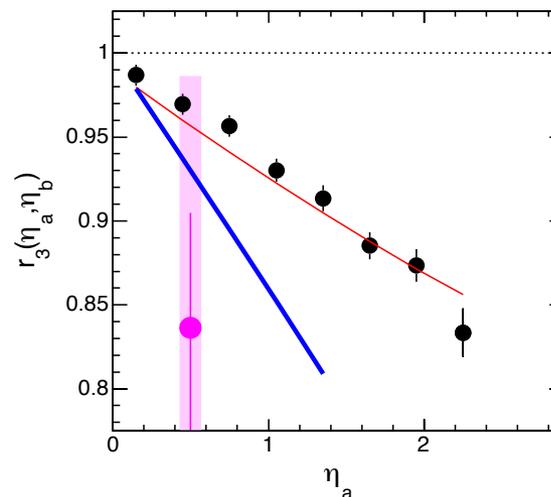
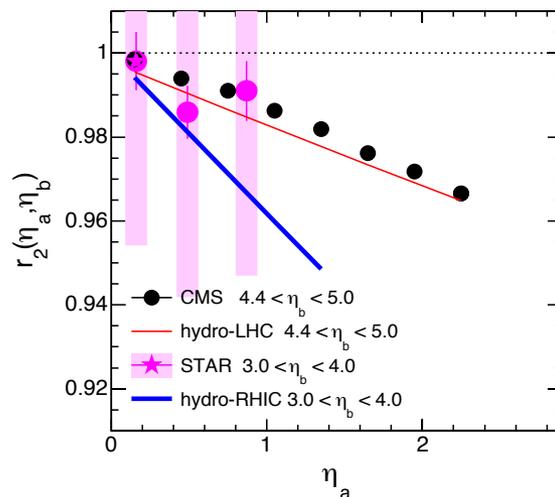
■ Multiplicity correlation $C(\eta_1, \eta_2)$ via identified particles

- probe transport of conserved quantities in η : charge, net baryon, strangeness..
- Others, e.g. $\langle p_T \rangle(\eta_1)$, $\langle p_T \rangle(\eta_2)$ correlations nucl-th/0606061, 1106.4334

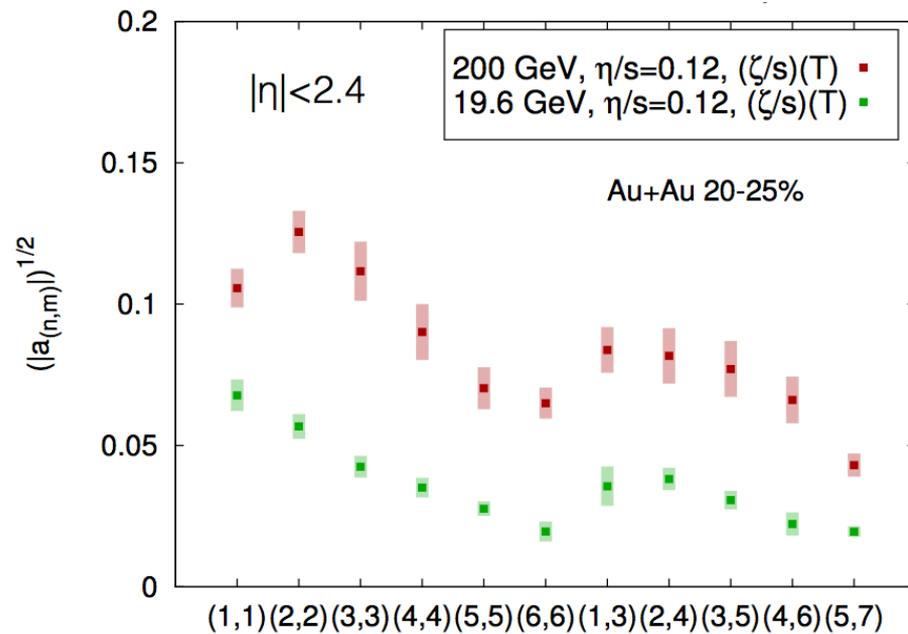
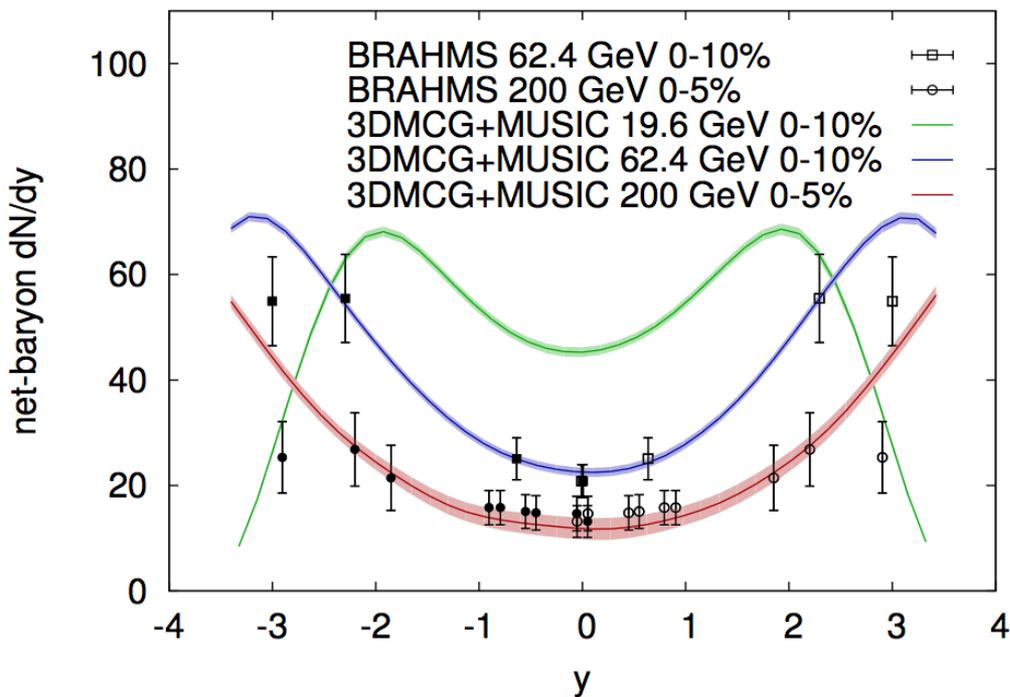
■ Perform similar measurements at RHIC

L.G.Pang, et.al EPJA52 (2016) 97

- FB asymmetry & decorrelation should be larger due to compressed η profile.
- \sqrt{s} dependence of number of sources, their η -length and length fluctuations.



EbyE baryon transport via FB net-proton correlation

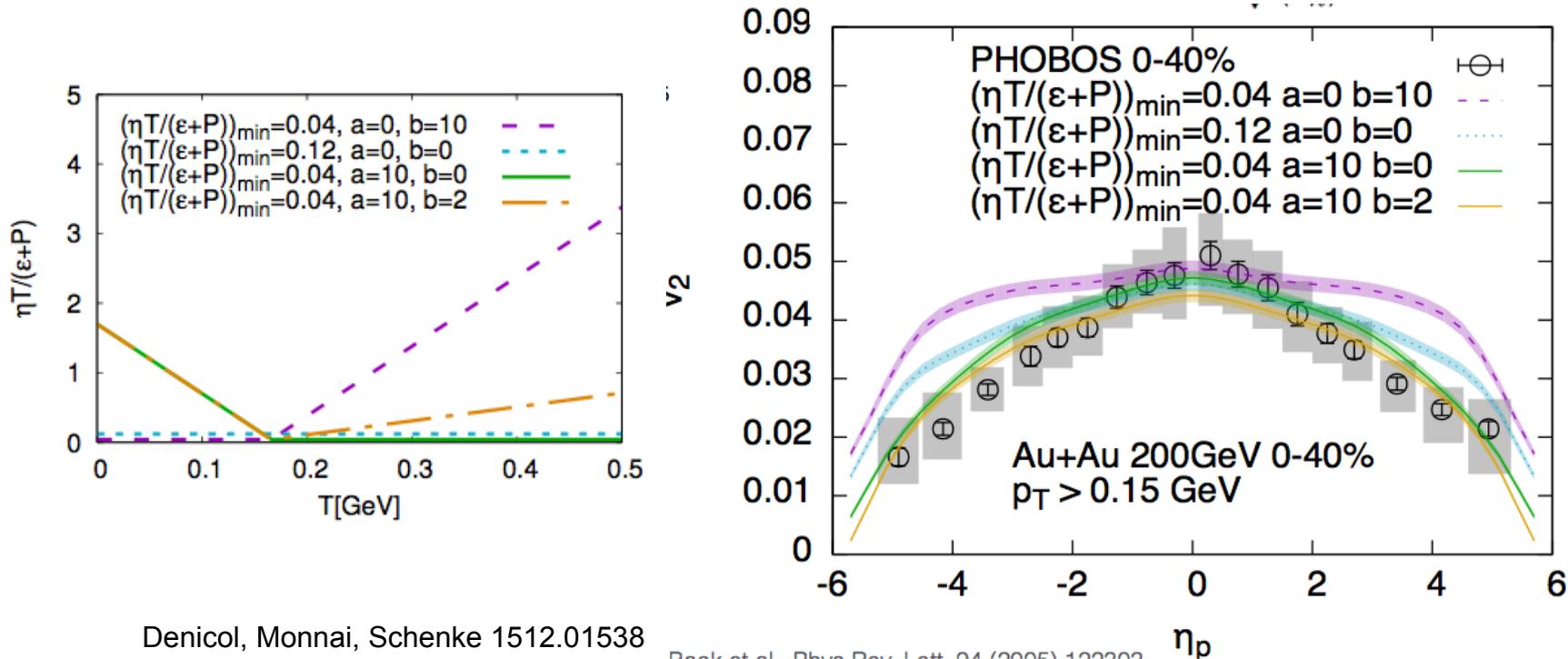
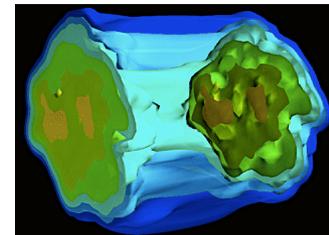


B. Schenke QM2015

Very important in the context of BES-II at RHIC

Outlook II

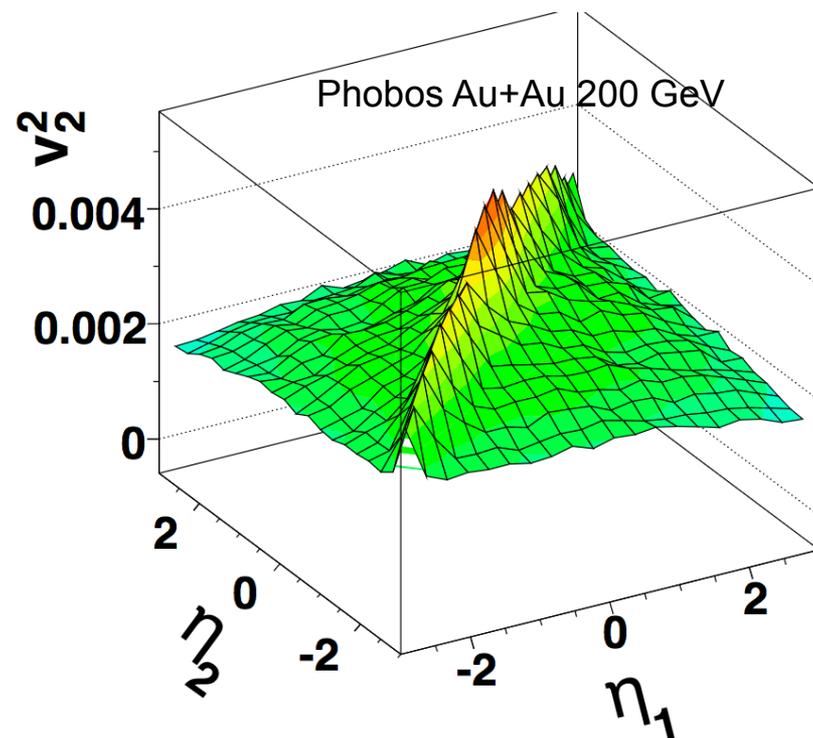
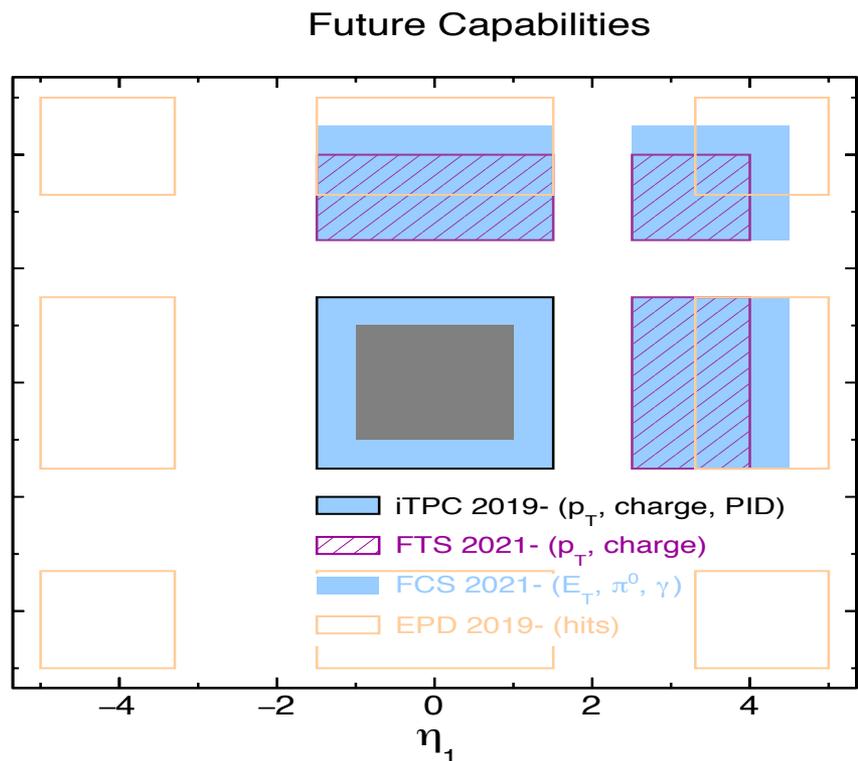
- Differential information on spectra and flow in forward η
 - Map the EbyE fluc & improve full EbyE 3+1D hydrodynamics.
 - Longitudinal pressure, isotropization, hydrodynamic noise....



forward high- μ at large $\sqrt{s} \neq$ mid-rapidity high- μ at small \sqrt{s}

Outlook III

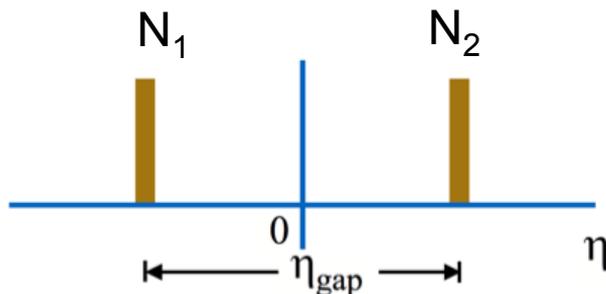
- LHC: LS2 upgrade extend tracking from $|\eta| < 2.5$ to 4 @ATLAS/CMS
- RHIC: possible STAR forward upgrade, iTPC+FTS+FCS & sPHENIX?



What level of precision we need for the longitudinal dynamics in comparison to the transverse dynamics?

Backup

Traditional observable



$$b = \frac{\langle N_1 N_2 \rangle - \langle N_1 \rangle \langle N_2 \rangle}{\sigma_{N_1} \sigma_{N_2}}$$

$$\approx (C(\eta_1, \eta_2) - 1) \frac{1}{\sqrt{\langle N_2 \rangle} \sqrt{\langle N_2 \rangle}}$$



Undesirable, e.g. value of b reduces by factor of two if one uses only half of the particles in each rapidity, although physics clearly should remain the same.

Statistical artifacts everywhere!

