Correlations and fluctuations in high-energy nuclear collisions

-- a "flow" centric review

Jiangyong Jia

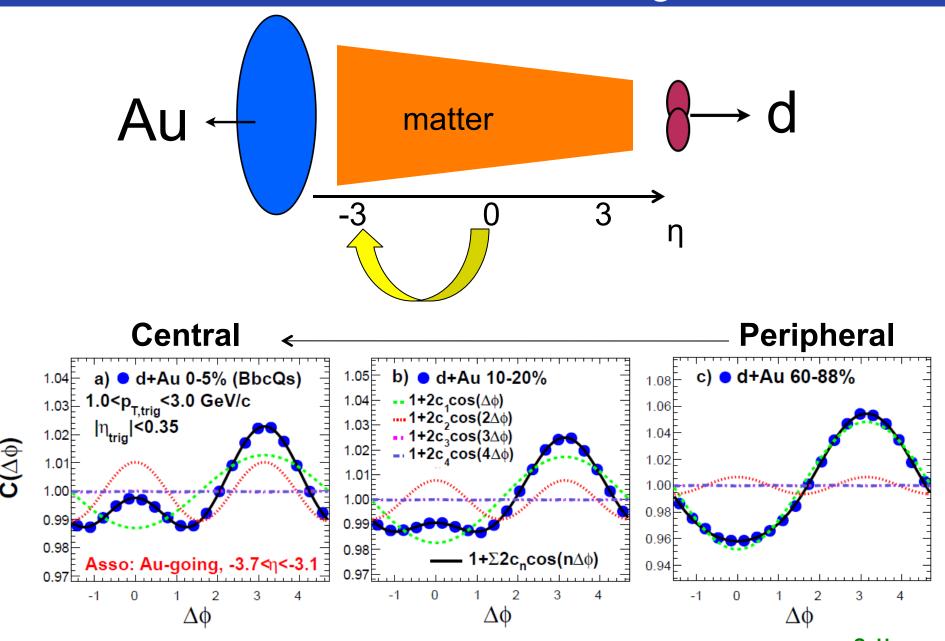
- Ridge in small systems
- Collective phenomena in A+A



Refer to Alex Shmah for other topics

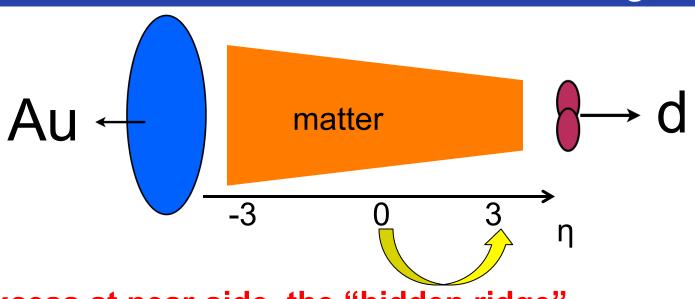


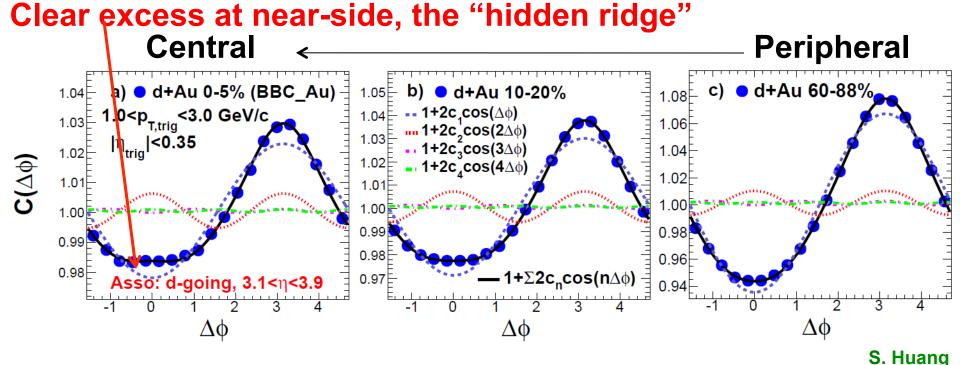
The PHENIX d+Au ridge



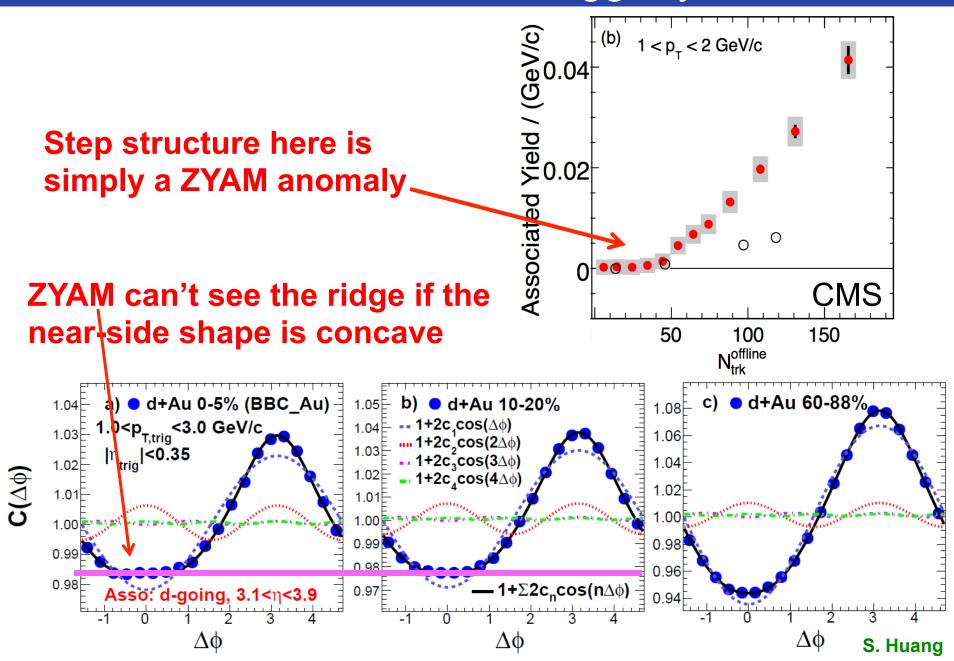
S. Huang

The PHENIX "hidden" d+Au ridge

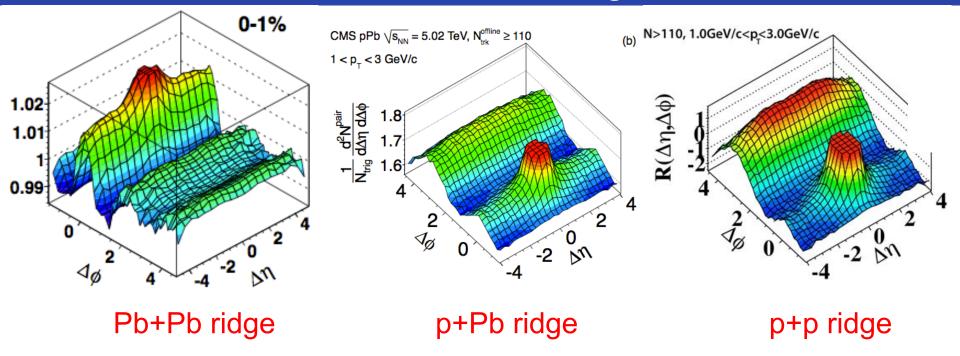




Be careful about Per-trigger yield...

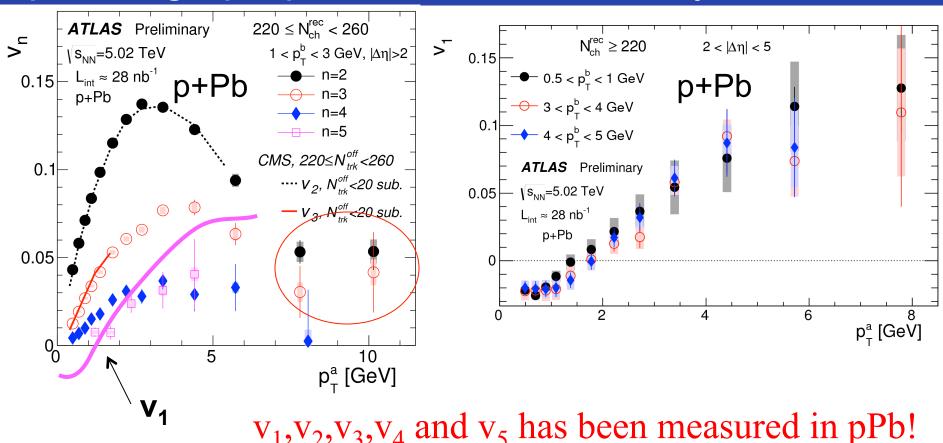


The tale of three ridges....

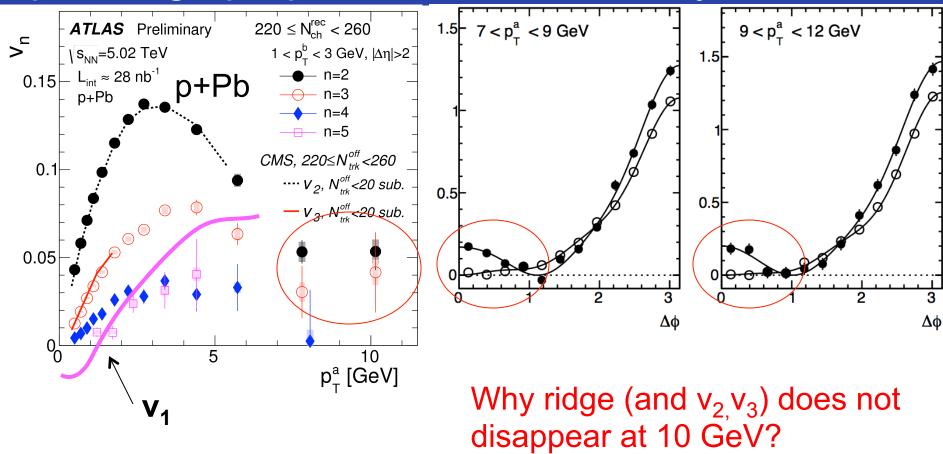


- Manifestation of QCD in different high density systems
- But is there an effective mechanism that rules them all? Is it initial state effect, final state effect or both?
- What is its detailed p_T , η , and centrality dependence? How these dependences compare between different systems?

pPb ridge properties summarized by harmonics

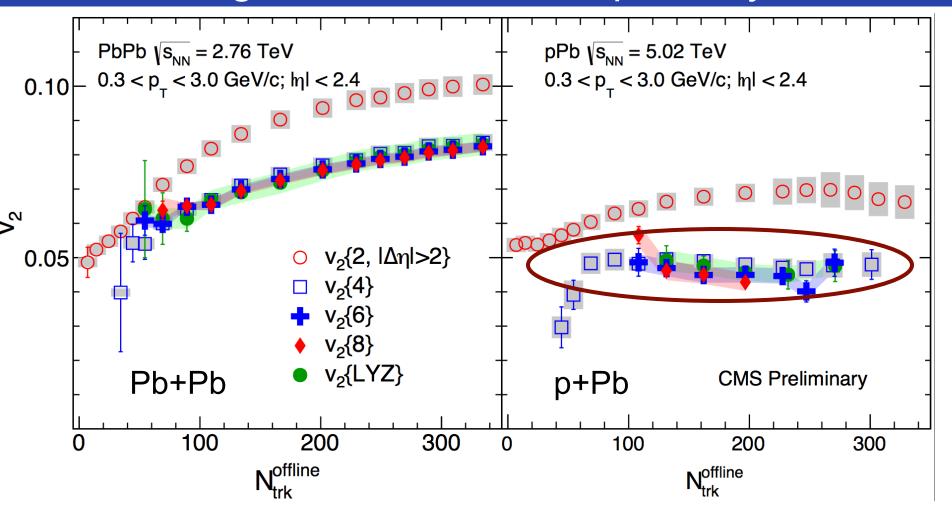


- v_1, v_2, v_3, v_4 and v_5 , made possible with recoil subtraction
 - v_2 , v_3 out to 10 GeV, remain 3-5%, small jet modifications?
 - v_n decrease with n for n=2-5
 - Significant v_1 comparable with v_3 at 4 GeV.



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Is there global correlation in p+Pb system?

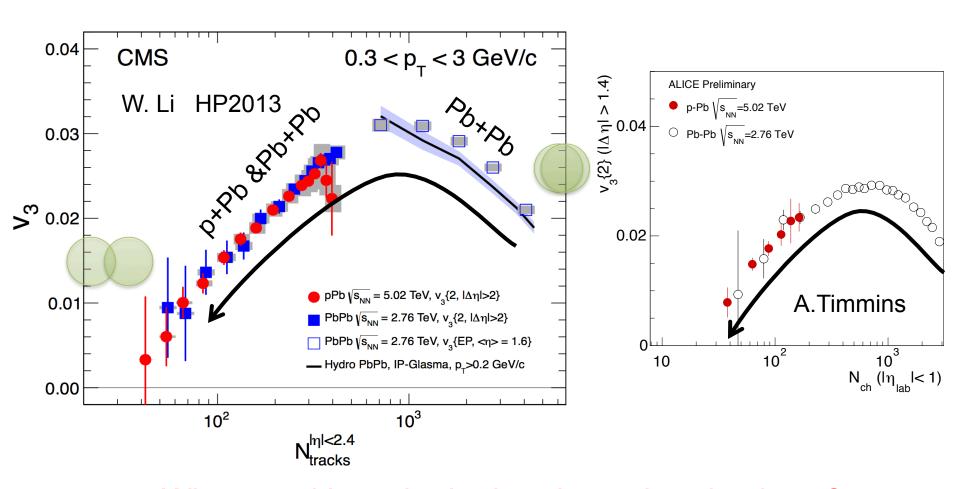


Multi-particle and all particle correlation signal remain remarkably large in high-multiplicity events!!

Collective behavior!

Comparison p+Pb with Pb+Pb

Collectivity increase and decrease with system size.



Where and how the hydro-picture breaks down? What is the correct effective theory? CGC+transport?

Comparison of p+Pb with Pb+Pb

 Why extrapolation of hydro prediction works so well? e.g. conformal scaling

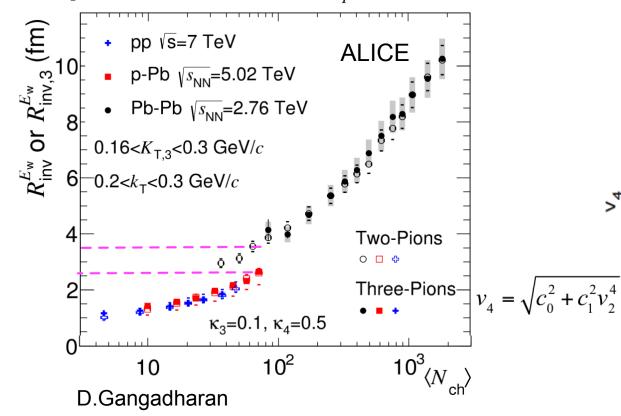
G. Basar & Teaney

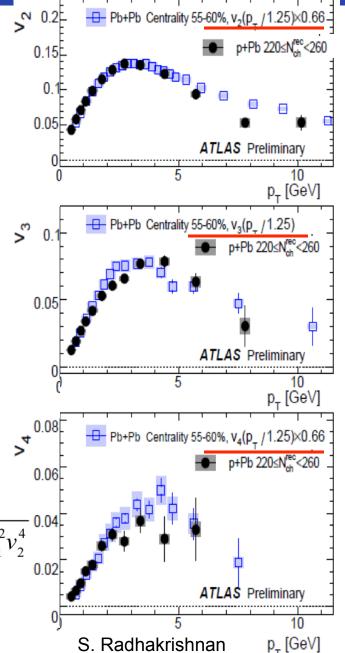
• From the confomal analysis

$$\frac{L_{AA}}{L_{pA}} = \frac{\langle p_T \rangle_{pA}}{\langle p_T \rangle_{AA}} = 1.3$$

• Find:

$$\frac{R_{AA}}{R_{pA}} = \frac{3.5}{2.6} = 1.35$$





Comparison of p+Pb with Pb+Pb

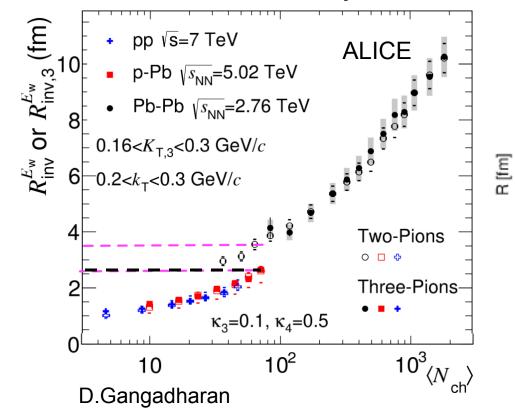
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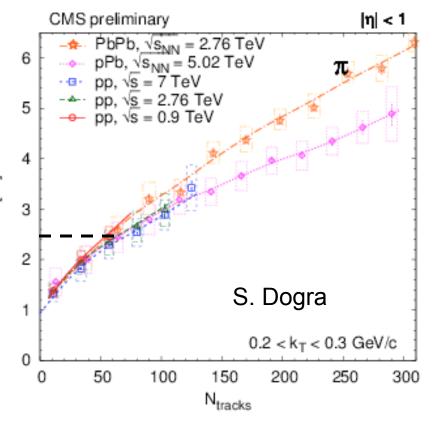
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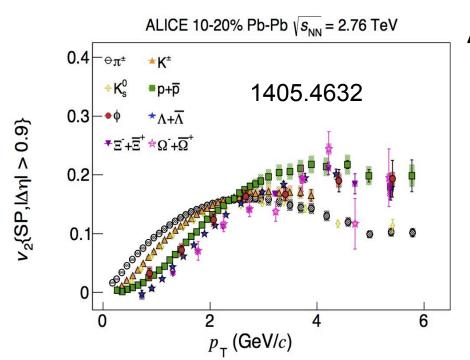
Detailed comparison between experiments are needed

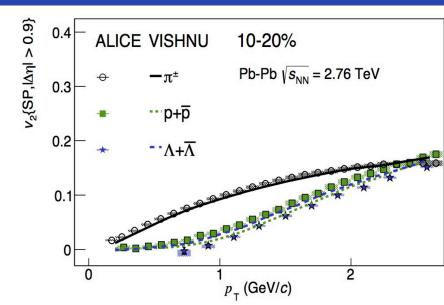


A few observations/comments about flow in A+A collisions

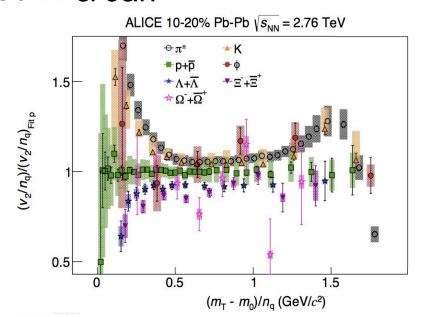
PID v₂ at LHC

- Compare to RHIC results,
 - Stronger radial flow and importance of hadronic rescattering.
 - Poorer NCQ scaling.
- • flow like a baryon (central) and meson (mid-central)
 - Combination of mass and crosssection effects?

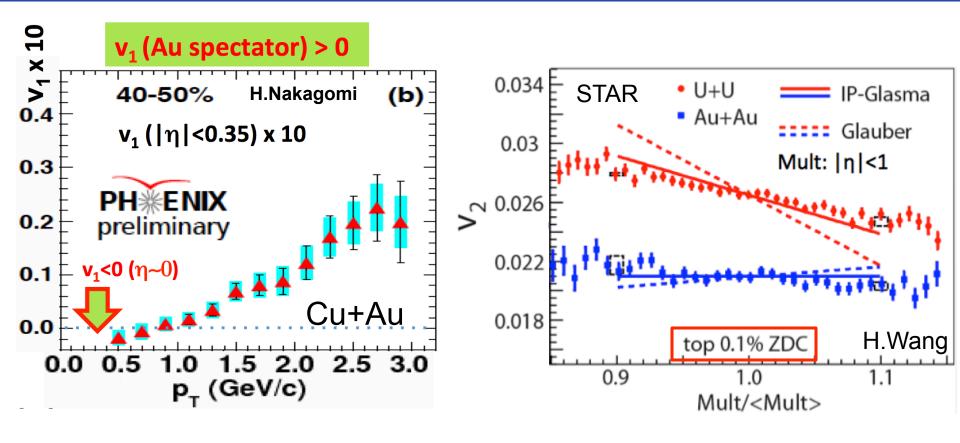




A. Dobrin & Jan



Cu+Au and U+U



- Cu+Au v₁ from average dipolar geometry
- U+U: see some sensitivity to the initial state geometry.

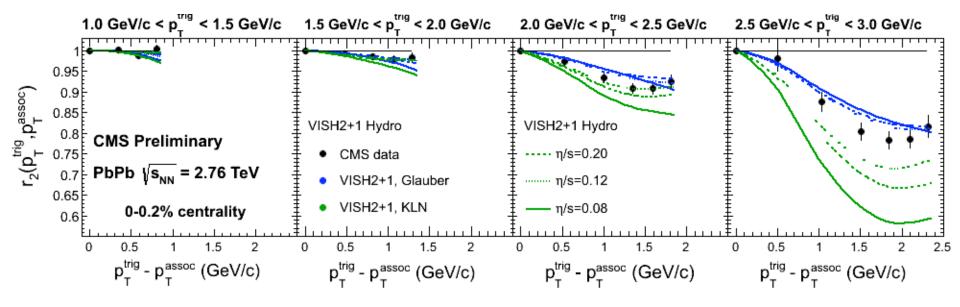
Each collision system introduces its own uncertainty in geometry!

Intra-event flow fluctuation and factorization

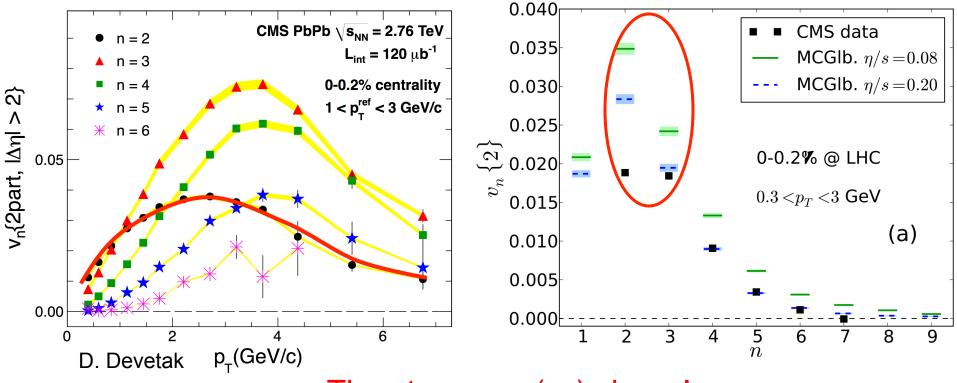
• Flow angle and amplitude fluctuates in p_T (and η) Ollitrault QM2012

$$ilde{r}_n(p_{T1},p_{T2}) := rac{\langle v_n(p_{T1})v_n(p_{T2}) ext{cos}[n(\Psi_n(p_{T1})-\Psi_n(p_{T2}))]
angle}{\langle v_n(p_{T1})v_n(p_{T2})
angle}$$

- Breaking is largest for v₂ in ultra-central Pb+Pb collisions
 - Much smaller for other harmonics and in other centralities (ALICE/ATLAS/CMS)
- Breaking of factorization p+Pb at a few % level D. Devetak also Y. Zhou



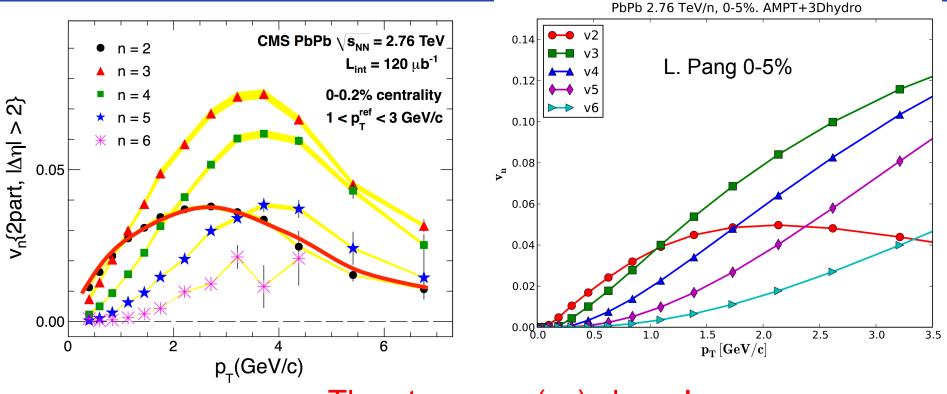
Ultra-central collisions



The strange v₂(p_T) shape!

- Linear response dominates: $v_n \propto \varepsilon_n$ for all n
- Models have difficulty explain $v_2 \approx v_3$
 - Importance of nucleon-nucleon correlation and bulk viscosity? G.Denicol

Ultra-central collisions

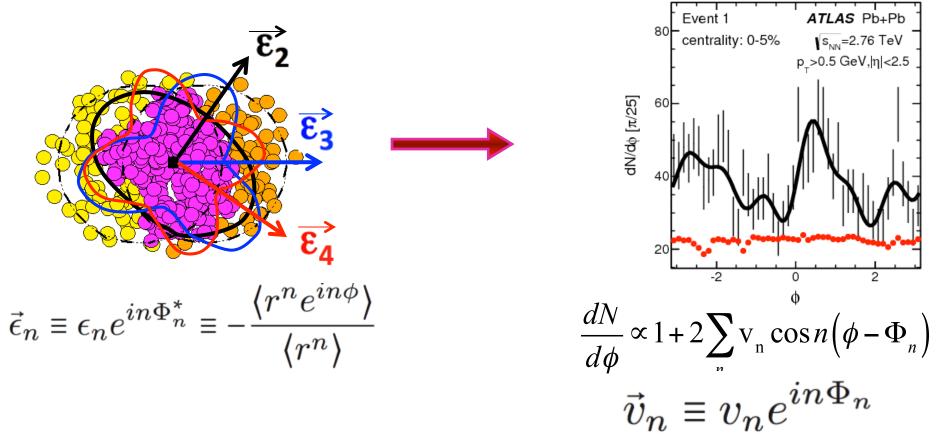


The strange $v_2(p_T)$ shape!

- Linear response dominates: $v_n \propto \varepsilon_n$ for all n
- Models have difficulty explain $v_2 \approx v_3$
 - Importance of nucleon-nucleon correlation and bulk viscosity? G.Denicol

Event-by-Event fluctuations

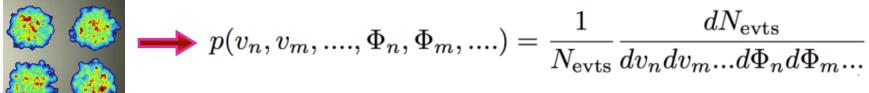
Geometry and harmonic flow



- How $(\varepsilon_n, \Phi_n^*)$ are transferred to (v_n, Φ_n) ?
- What is the nature of final state (non-linear) dynamics?

Experimental observables

Many little bangs



Angular component captured by cosines

$$\frac{dN_{\text{evts}}}{d\Phi_1 d\Phi_2 ... d\Phi_l} \propto \sum_{c_n = -\infty}^{\infty} a_{c_1, c_2, ..., c_l} \cos(c_1 \Phi_1 + c_2 \Phi_2 ... + c_l \Phi_l)$$

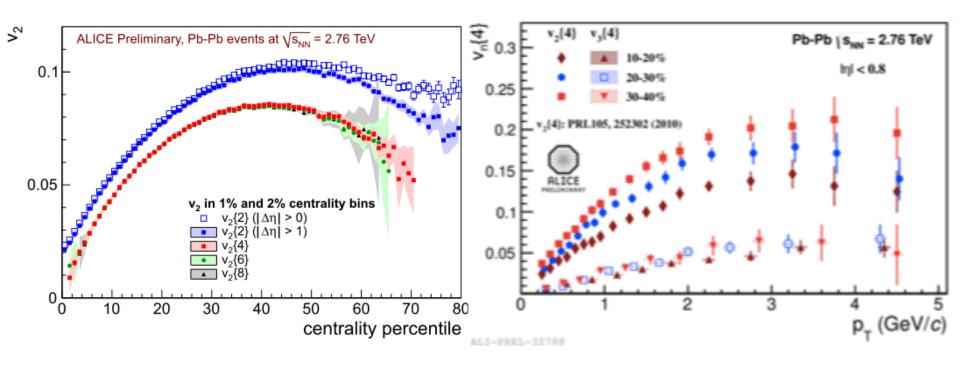
$$a_{c_1, c_2, ..., c_l} = \langle \cos(c_1 \Phi_1 + c_2 \Phi_2 + ... + c_l \Phi_l) \rangle$$

$$\langle \cos(c_1 \Phi_1 + 2c_2 \Phi_2 ... + lc_l \Phi_l) \rangle, c_1 + 2c_2 ... + lc_l = 0.$$

1104.4740, 1209.2323, 1203.5095 ,1312.3572

| | Probability distribution | Cumulants |
|-------------------------|--------------------------|--|
| Flow amplitudes | $p(v_n), p(v_n, v_m)$ | $v_n\{2k\}, \langle v_n^2 v_m^2 \rangle - \langle v_n^2 \rangle \langle v_m^2 \rangle$ |
| Event-plane correlation | $p(\Phi_n,\Phi_m,)$ | $\langle \vec{v}_n \vec{v}_m \rangle$ or |
| | | $\langle \cos(c_1\Phi_1++lc_l\Phi_l) \rangle$ |

v_n{2k} in Pb+Pb collisions

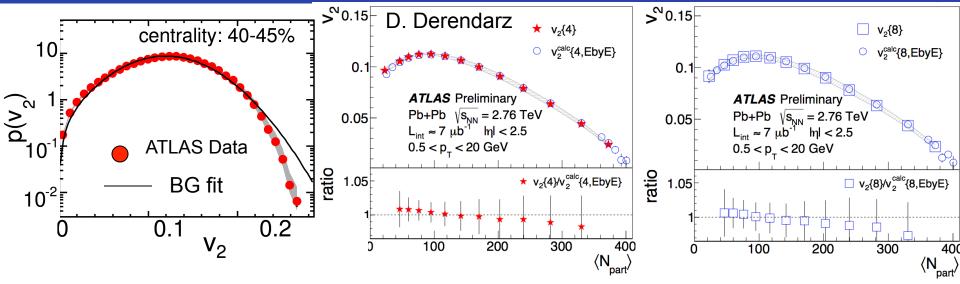


- Provide information about the underlying $p(v_n)$ distribution
- $v_2\{4\} \sim v_2\{6\} \sim v_2\{8\}$ Gaussian fluctuation around mean v_2^{RP} :

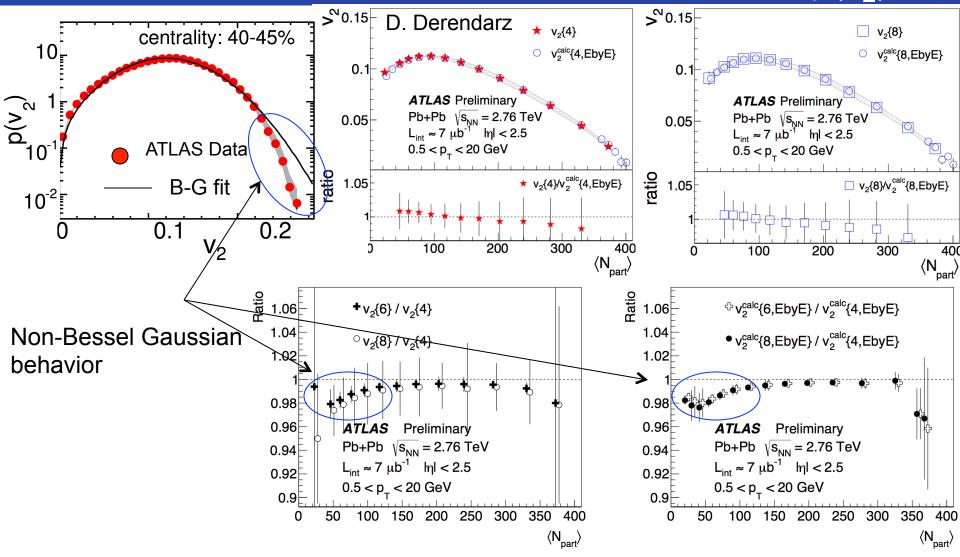
$$p(\vec{v}_n) = \frac{1}{2\pi\delta_{v_n}^2} e^{-(\vec{v}_n - \vec{v}_n^{\text{RP}})^2/(2\delta_{v_n}^2)}$$

Non-zero $v_3\{4\}$ (ALICE) and also $v_4\{4\}$ (ATLAS)

Cumulants from traditional method and from p(v₂)



Cumulants from traditional method and from p(v₂)



- Measuring $p(v_2)$ is equivalent to cumulants, more intuitive and simpler systematics
- Non-Bessel Gaussian is reflected by a 2% change beyond 4th order cumulants

How $(\varepsilon_n, \Phi_n^*)$ are transferred to (v_n, Φ_n) ?

Flow response is linear for v_2 and v_3 : $v_n \propto \varepsilon_n$ and $\Phi_n \approx \Phi_n^*$ i.e.

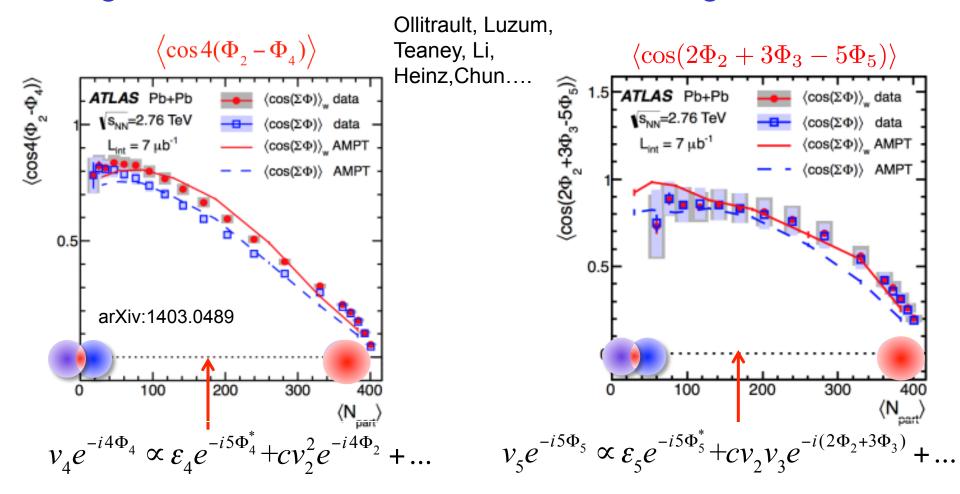
$$v_2 e^{-i2\Phi_2} \propto \epsilon_2 e^{-i2\Phi_2^*}, \ v_3 e^{-i3\Phi_3} \propto \epsilon_3 e^{-i3\Phi_3^*}$$

How $(\varepsilon_n, \Phi_n^*)$ are transferred to (v_n, Φ_n) ?

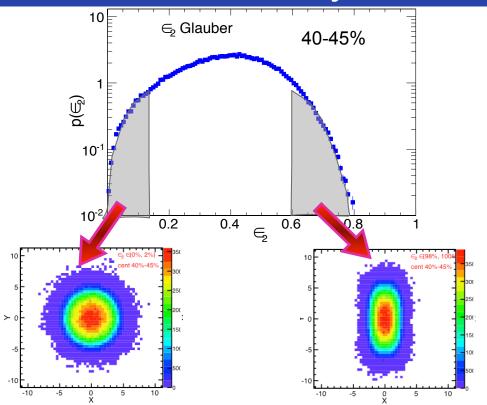
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■ Higher-order flow arises from EP correlations., e.g. :



More info by selecting on event-shape

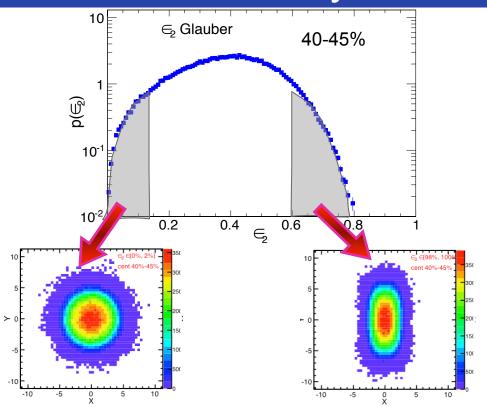


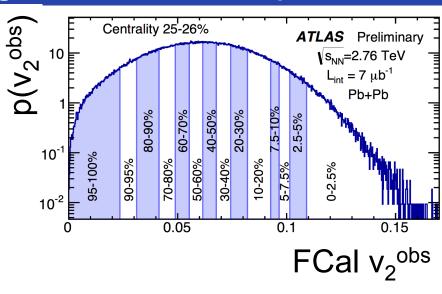
arXiv:1208.4563

arxiv:1311.7091

• Select events with certain v_2^{obs} in Forward Rapidity:

More info by selecting on event-shape



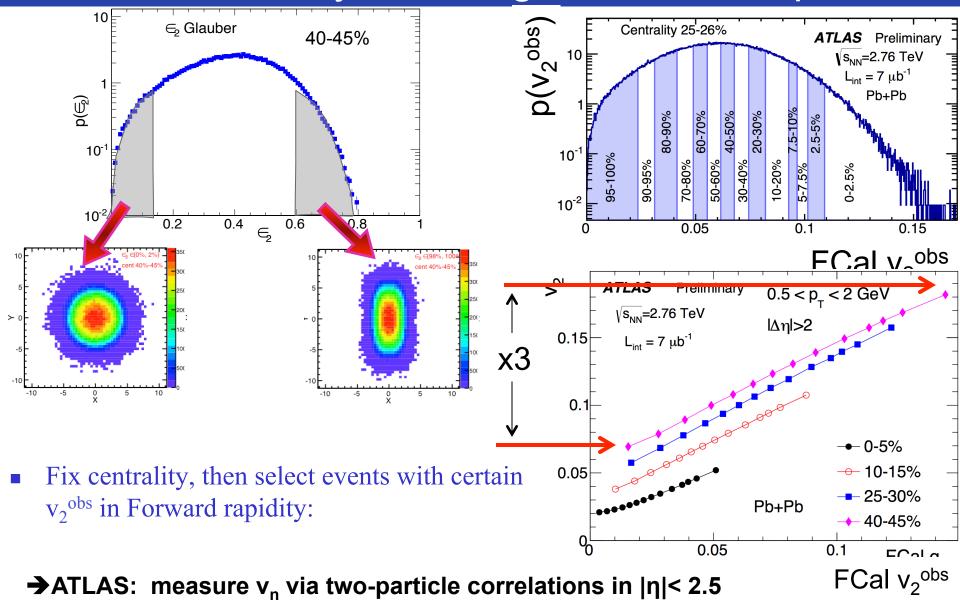


arXiv:1208.4563 arxiv:1311.7091

Fix centrality, then select events with certain v_2^{obs} in Forward rapidity:

→ATLAS: measure v_n via two-particle correlations in $|\eta| < 2.5$ Fix system size and change ellipticity!!

More info by selecting on event-shape

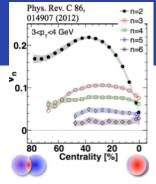


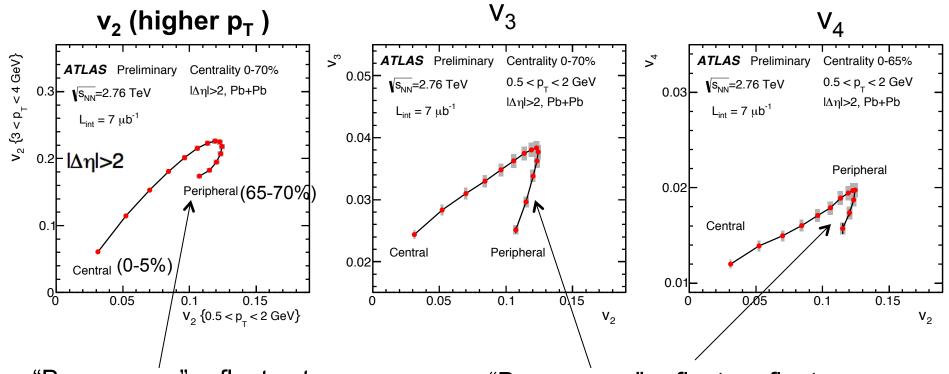
Vary ellipticity by a factor of 3!

S. Mohapatra

v_n-v₂ correlations: centrality dependence

• First correlation without event v_2 -selection, 5% steps





"Boomerang" reflects stronger viscous damping at higher p_T and peripheral

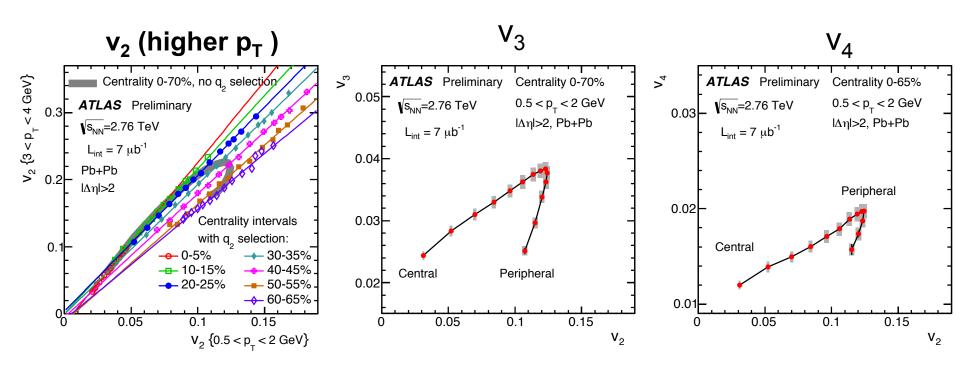
"Boomerang" reflects reflects different centrality dependence, which is also sensitive to the viscosity effect.

S. Mohapatra

v_n-v₂ correlations: within fixed centrality

• Fix system size and vary the ellipticity!

Probe $p(v_n, v_2)$



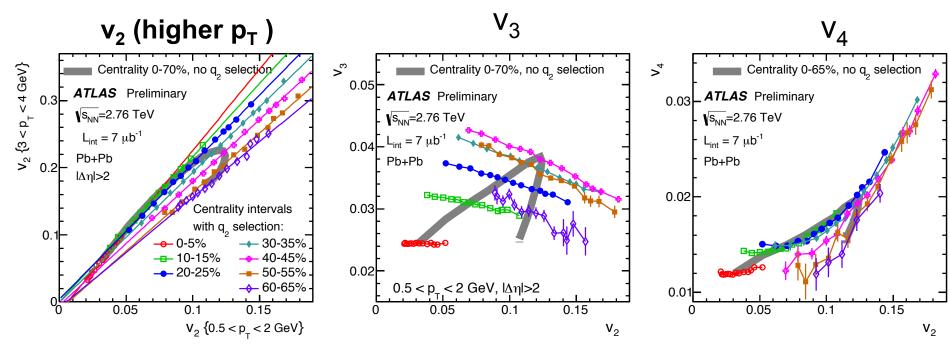
Linear correlation for forward v₂-selected bin → viscous damping controlled by system size, not shape

v_n-v₂ correlations: within fixed centrality

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Probe $p(v_n, v_2)$

• Overlay ε_3 - ε_2 and ε_4 - ε_2 correlations, rescaled



Linear correlation for forward v₂-selected bin → viscous damping controlled by system size, not shape

Clear anti-correlation,

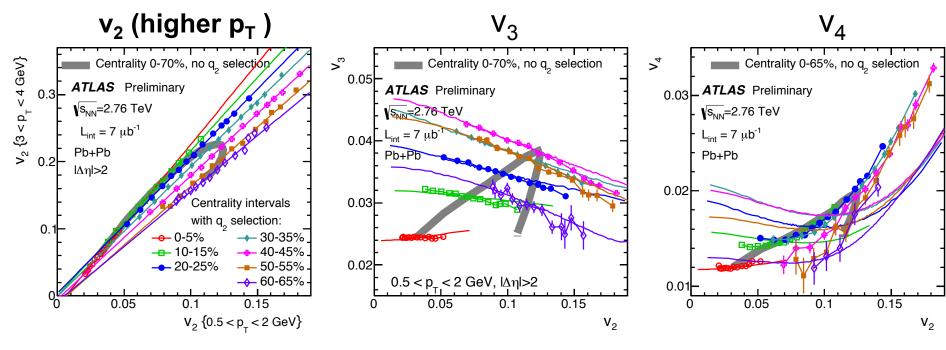
quadratic rise from nonlinear coupling to v_2^2

v_n-v₂ correlations: within fixed centrality

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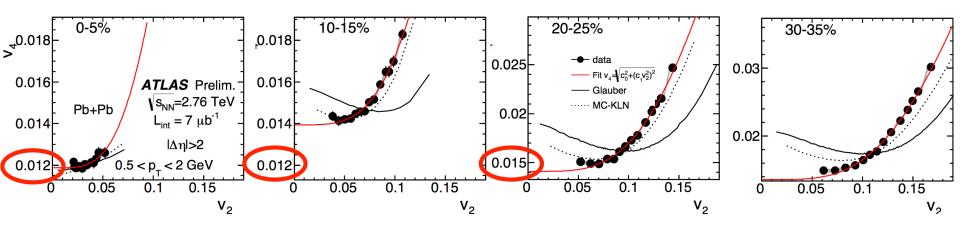
Linear correlation for forward v₂-selected bin → viscous damping controlled by system size, not shape

Clear anti-correlation, mostly initial geometry effect!!

quadratic rise from nonlinear coupling to v_2^2 initial geometry do not work!!

Initial geometry describe v₃-v₂ but fails v₄-v₂ correlation S. Mohapatra

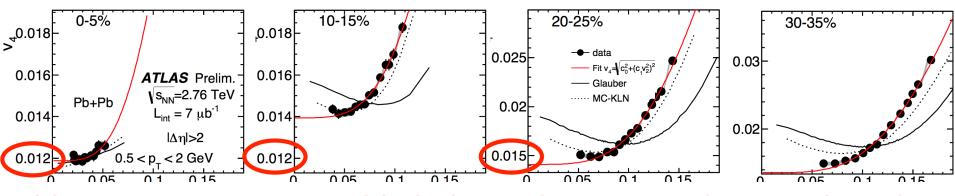
■ V_4 - V_2 correlation for fixed centrality bin $v_4 e^{i4\Phi_4} = c_0 e^{i\Phi_4^*} + c_1 \left(v_2 e^{i2\Phi_2}\right)^2 \Rightarrow \text{ Fit by } v_4 = \sqrt{c_0^2 + c_1^2 v_2^4}$



Fit $v_4 = \sqrt{c_0^2 + c_1^2 v_2^4}$ to separate linear (ε₄) and non-linear (ν₂²) component

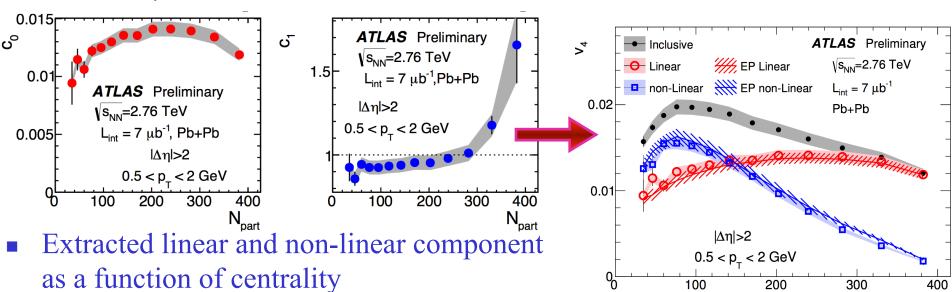
linear (ε₄) and non-linear (ν₂²) component of ν₄

■ V_4 - V_2 correlation for fixed centrality bin $v_4 e^{i4\Phi_4} = c_0 e^{i\Phi_4^*} + c_1 \left(v_2 e^{i2\Phi_2}\right)^2 \Rightarrow \text{ Fit by } v_4 = \sqrt{c_0^2 + c_1^2 v_2^4}$



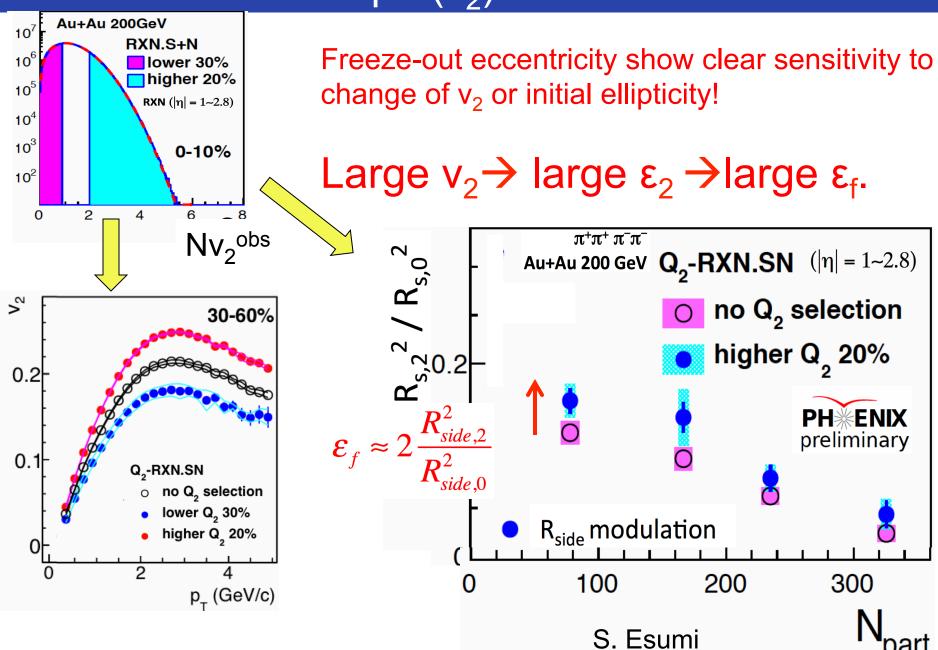
Linear-component provide independent constraints on viscosity

Fit $v_4 = \sqrt{c_0^2 + c_1^2 v_2^4}$ to separate linear (ε₄) and non-linear (ν₂²) component



See details at https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/CONFNOTES/ATLAS-CONF-2014-022/

Event-shape (v₂) selected HBT



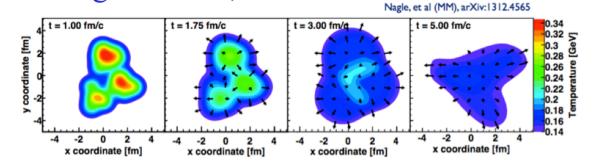
Future prospects: my humble opinion

(I): Precision event-shape selection

■ Different collision system e.g. He³+Au, June 16th!

P. ROMATSCHKE

Intrinsic trangularity

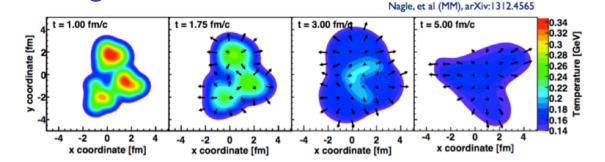


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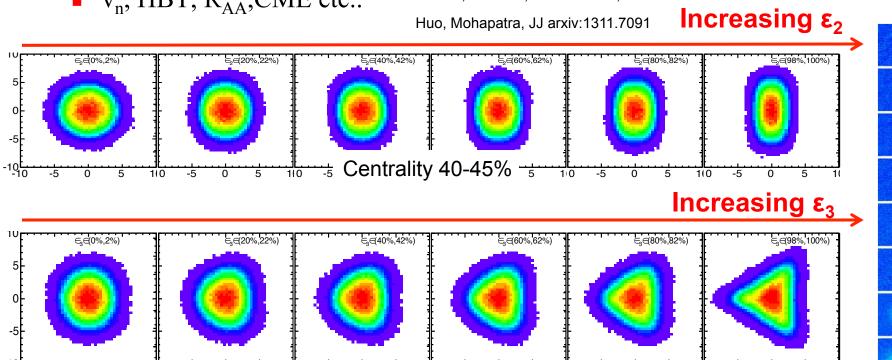
P. ROMATSCHKE

Intrinsic trangularity



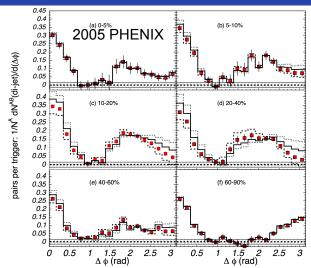
- Event-shape selections on v_2 and/or v_3 Fix size, change ε_2 and ε_3
- v_n, HBT, R_{AA},CME etc..

Schukraft, Timmins, and Voloshin, arXiv:1208.4563



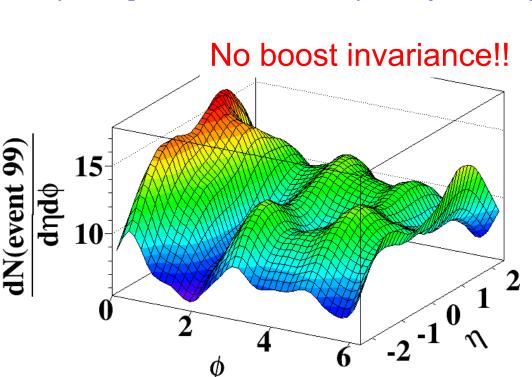
(II): understand jet-medium interaction

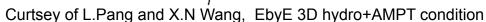
- How (mini)-jet are thermalized in medium?
 - Difficult due to dominance of collective flow
 - Until 2010, triangular flow was interpreted as "Mach-cone"
- Event-shape selection technique can help!
 - Require events to have small v_n, less flow subtraction.



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- How (mini)-jet are thermalized in medium
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 - Circa 2005, triangular flow was interpreted as "Mach-cone"
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(II): understand jet-medium interaction

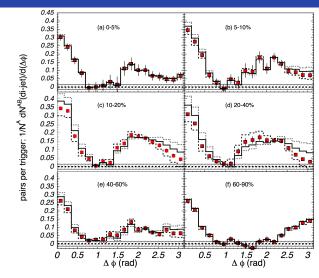
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- Event-shape selection technique can help!
 - Require events to have small v_n , less flow subtraction.
- $\eta \times \varphi$ space are dominated by fake-jets or "hydro-jets"
 - They can be found by jet-reco algorithm (vetoing good jets)

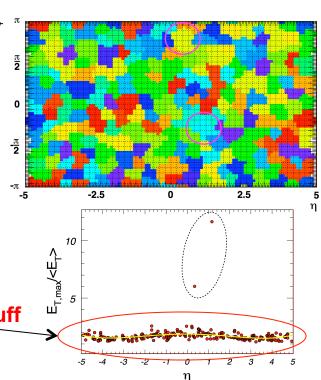
Then analysis spectrum or study substructure?

k_T algorithm

k_T algorithm

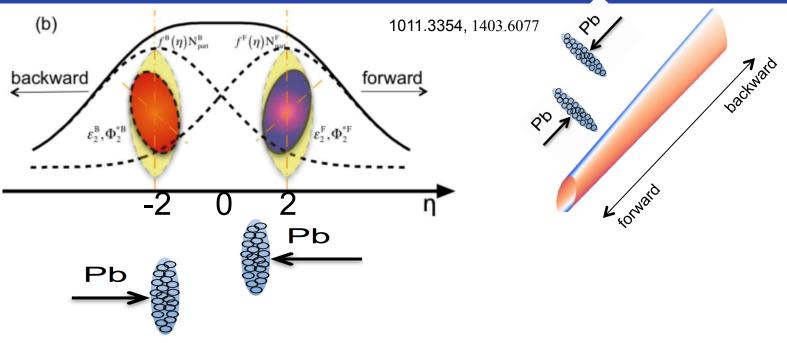
limit to the structure of the





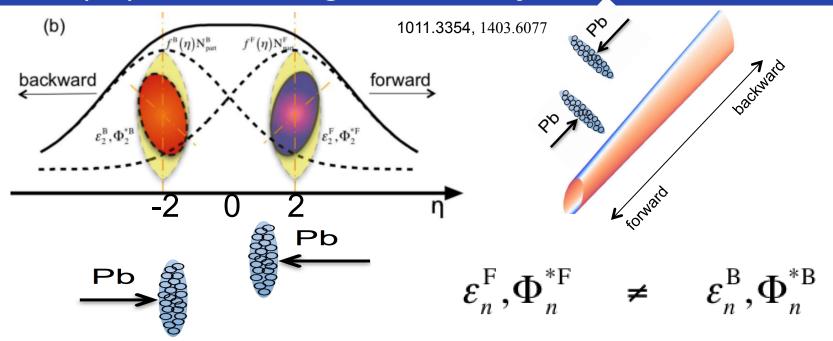
Curtsey of L.Pang and X.N Wang, EbyE 3D hydro+AMPT condition

(III): flow longitudinal dynamics



- Shape of participants in two nuclei not the same due to fluctuation $\varepsilon_n^F, \Phi_n^{*F} \neq \varepsilon_n^B, \Phi_n^{*B}$
- Particles are produced by independent fragmentation of wounded nucleons, emission function f(η) not symmetric in η→ Wounded nucleon model

(III): flow longitudinal dynamics



• Eccentricity vector interpolates between $\vec{\epsilon}_n^{\mathrm{F}}$ and $\vec{\epsilon}_n^{\mathrm{B}}$

$$\vec{\epsilon}_n^{\text{tot}}(\eta) \approx \alpha(\eta)\vec{\epsilon}_n^{\text{F}} + (1 - \alpha(\eta))\vec{\epsilon}_n^{\text{B}} \equiv \epsilon_n^{\text{tot}}(\eta)e^{in\Phi_n^{*\text{tot}}(\eta)}$$

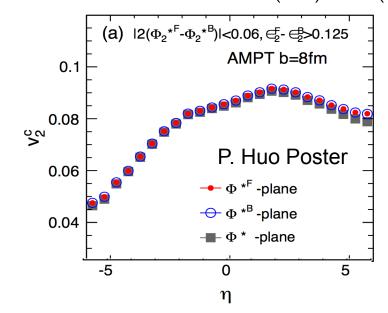
 $\alpha(\eta)$ determined by $f(\eta)$

• Hence
$$\vec{v}_n(\eta) \approx c_n(\eta) \left[\alpha(\eta)\vec{\epsilon}_n^{\mathrm{F}} + (1-\alpha(\eta))\vec{\epsilon}_n^{\mathrm{B}}\right]$$
 for n=2,3

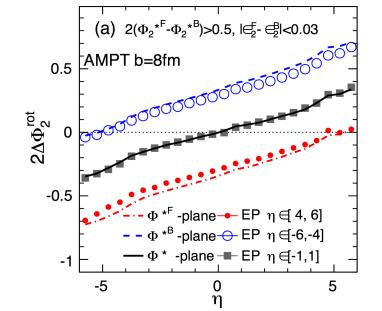
Picture verified in AMPT simulations, magnitude estimated 1403.6077

Asymmetry: $\varepsilon_n^{\rm F} \neq \varepsilon_n^{\rm B}$ Twist: $\Phi_n^{*{\rm F}} \neq \Phi_n^{*{\rm B}}$

Require $\varepsilon_2^F > \varepsilon_2^B$ see $v_2(+\eta) > v_2(-\eta)$

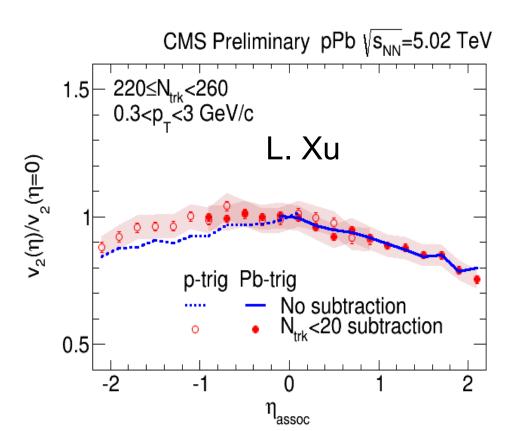


Require $\Phi_n^{*F} > \Phi_n^{*B}$ see $\Phi_2(+\eta) > \Phi_2(-\eta)$



Initial state twist and asymmetry survives collective expansion

Play a bigger role for Cu+Au, U+U and p+A system



Backup

Elliptic flow of identified particles

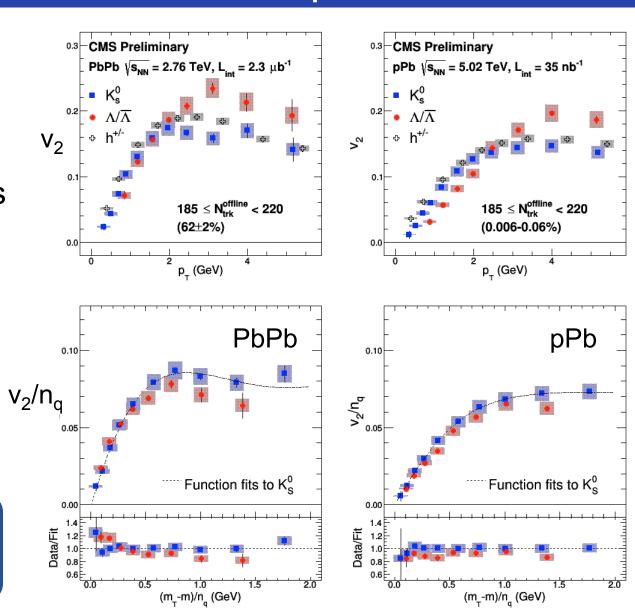
Identified K_S and ∧ & charged hadrons

v₂ (and v₃) from 2-particle correlations

show mass ordering In pPb and PbPb (stronger in pPb)

and ≈ quark scaling (better in pPb)

Talk by Sharma Poster by Chen PAS-HIN-14-002



Linear and non-linearity example

Hadrons freezeout from exponential distribution of the flow field

$$E\frac{d^3N}{d^3\vec{p}} \approx \frac{g}{(2\pi)^3} \int_{\Sigma} \exp(-\frac{p \cdot u(x)}{T}) p \cdot d^3\sigma(x)$$

■ Flow field u(x) has a harmonic modulation driven by geometry

$$u(\phi) = u_0(1 + 2\sum \beta_n \cos(\phi - \Phi_n))$$

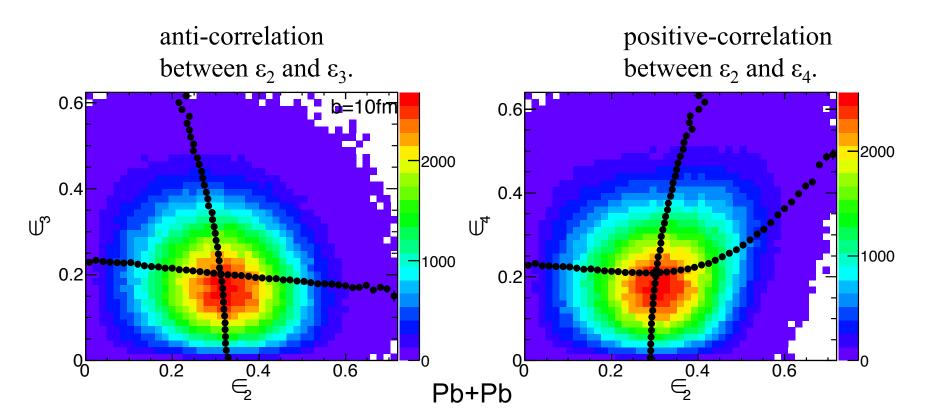
Quadratic term in saddle-point expansion leads to mode-mixing

$$\begin{array}{l} e^{-p_{\mathrm{T}}u(\phi)} \approx 1 - p_{\mathrm{T}}u(\phi) + \frac{1/2p_{\mathrm{T}}^2u^2(\phi)}{1/2p_{\mathrm{T}}^2u^2(\phi)}.. & \text{Borghini, Ollitrault 2005} \\ v_2(p_{\mathrm{T}}) \approx I(p_{\mathrm{T}})\beta_2, v_3(p_{\mathrm{T}}) \approx I(p_{\mathrm{T}})\beta_3 & \text{I}_{(p_{\mathrm{T}})} = \frac{\bar{u}_{\mathrm{max}}}{T}(p_{\mathrm{t}} - m_{\mathrm{t}}\bar{v}_{\mathrm{max}}) \\ v_4(p_{\mathrm{T}}) \approx I(p_{\mathrm{T}})\beta_4 + \frac{I(p_{\mathrm{T}})^2}{2}\beta_2^2 & \longrightarrow \mathsf{V_2}^2 \\ v_5(p_{\mathrm{T}}) \approx I(p_{\mathrm{T}})\beta_5 + I(p_{\mathrm{T}})^2\beta_2\beta_3 & \longrightarrow \mathsf{V_2}\mathsf{V_3} \\ v_6(p_{\mathrm{T}}) \approx I(p_{\mathrm{T}})\beta_6 + \frac{I(p_{\mathrm{T}})^3}{6}\beta_2^3 + \frac{I(p_{\mathrm{T}})^2}{2}\beta_3^2 + I(p_{\mathrm{T}})^2\beta_2\beta_4 & \text{V_2}^2, & \mathsf{V_2}\mathsf{V_4} \end{array}$$

$p(v_m, v_n)$ or v_m-v_n correlations

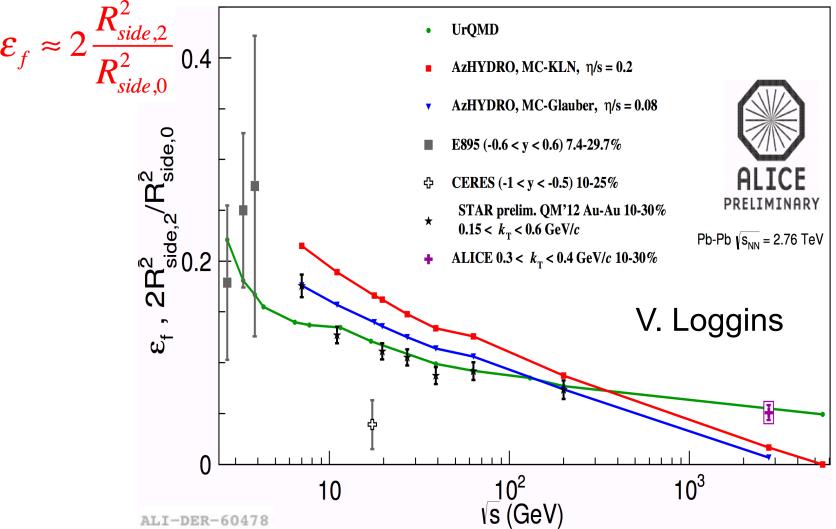
■ Evolution of v_n correlated with v_m via

- See also talk by S. Floerchinger
- Non-linearities from hydro evolution and freeze-out
- But also initial correlation



- Naturally studied via event-shape selection technique
 - E.g. select events with different v_2 and study v_n . in FIXED centrality

√s dependence of final spatial eccentricity



- Gradual decrease of ε_f as function of \sqrt{s} .
 - Hydro predicts stronger decrease,
 - UrQMD works but it probably under-predicts the flow.

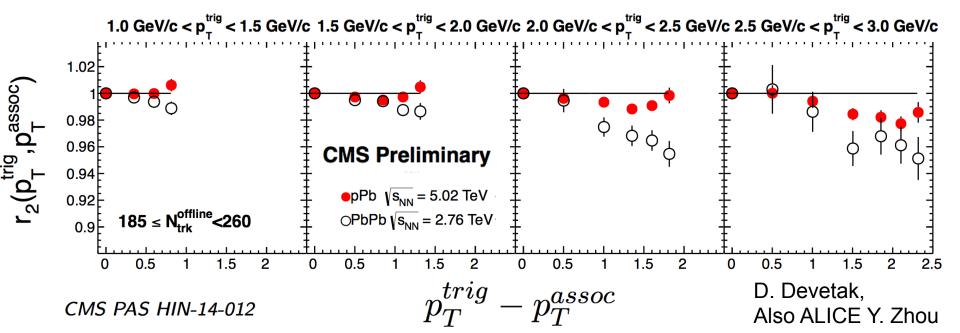
Intra-event flow fluctuation and factorization

• Flow angle and amplitude fluctuates in p_T (and η)

Ollitrault QM2012

$$ilde{r}_n(p_{T1},p_{T2}) := rac{\langle v_n(p_{T1})v_n(p_{T2}) ext{cos}[n(\Psi_n(p_{T1})-\Psi_n(p_{T2}))]
angle}{\langle v_n(p_{T1})v_n(p_{T2})
angle}$$

- Breaking is largest for v₂ in ultra-central Pb+Pb collisions
- Much smaller for other harmonics and in other centralities
- Very small (2-3%) breaking for high-multiplicity pPb collisions
 - Be aware of non-flow bias from di-jets, recoil subtraction is necessary in



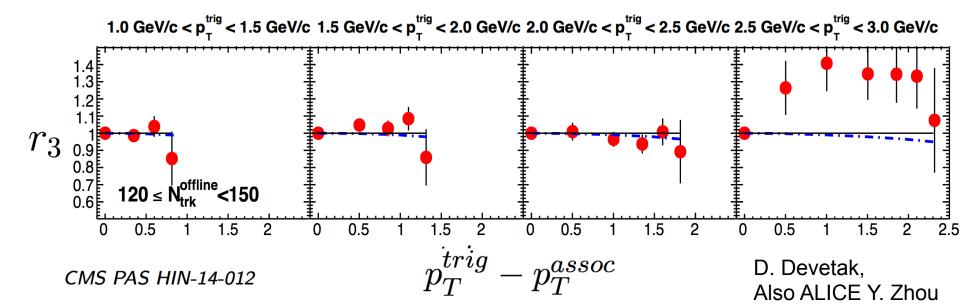
Intra-event flow fluctuation and factorization

• Flow angle and amplitude fluctuates in p_T (and η) Ollit

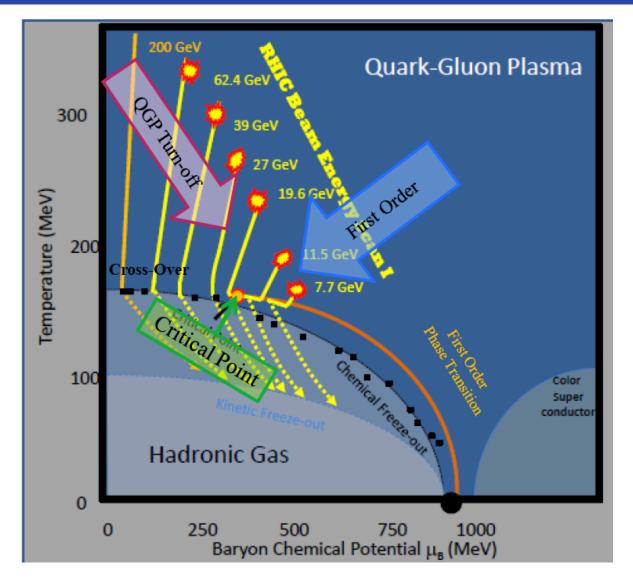
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- Breaking is largest for v₂ in ultra-central Pb+Pb collisions
- Much smaller for other harmonics and in other centralities
- Very small (2-3%) breaking for high-multiplicity pPb collisions
 - Be aware of non-flow bias from di-jets, recoil subtraction is necessary in order to compare with theory
 Kozlov et.al.:arXiv:1405.3976

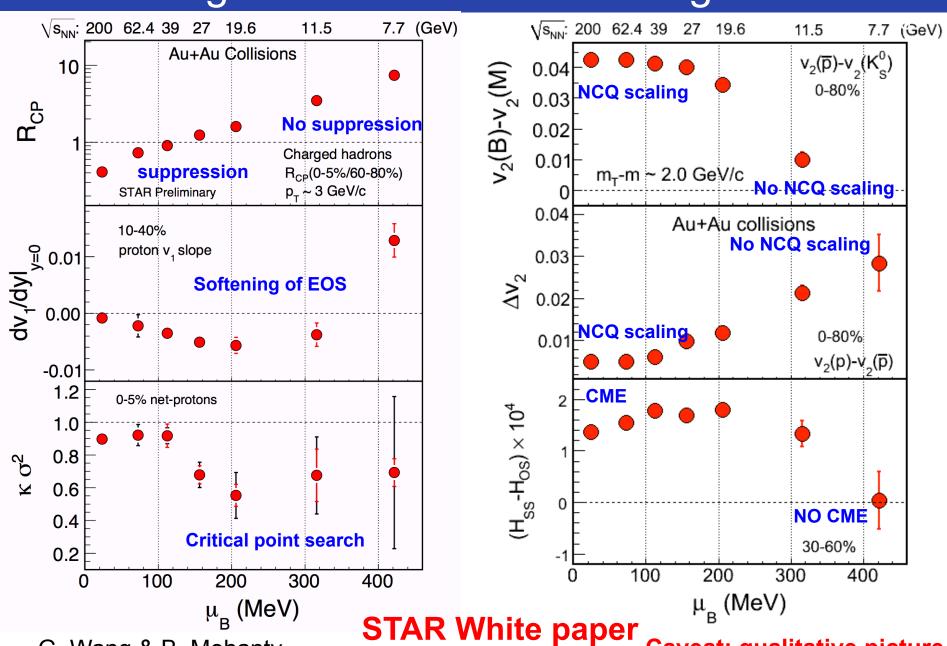


Beam Energy scan: search for CEP



■ Looking for non-monotonic change with \sqrt{s}

Looking for non-monotonic change with √s

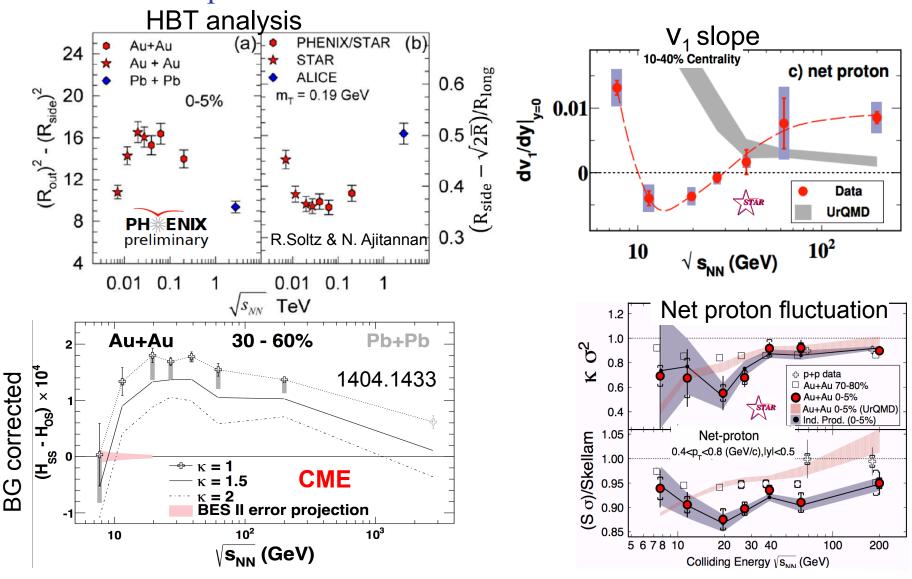


G. Wang & B. Mohanty

Caveat: qualitative picture

Looking for non-monotonic change with √s

• Shallow dips observed at $\sim 10\text{-}20$ GeV for several observables



More refined measurements with BES II and theory input!!