



# Forward-backward multiplicity correlations in PbPb, pPb and pp collisions from ATLAS

Jiangyong Jia for the ATLAS collaboration

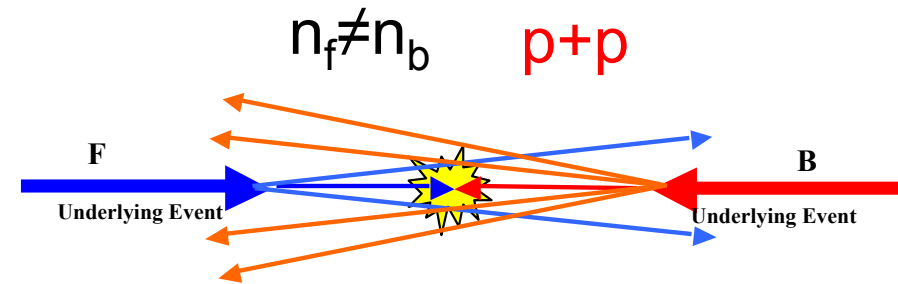
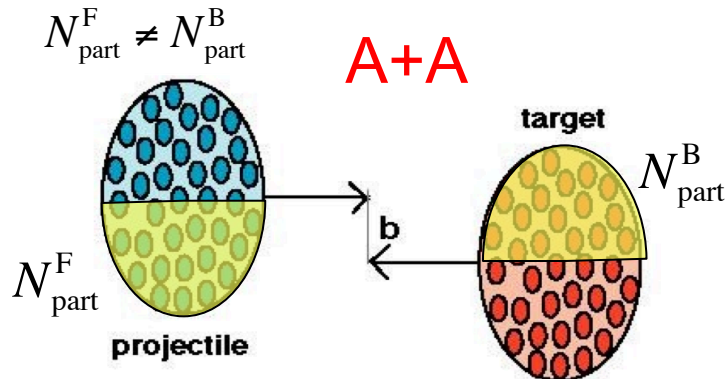
<http://cds.cern.ch/record/2029370>, ATLAS-CONF-2015-020

<http://cds.cern.ch/record/2055672>, ATLAS-CONF-2015-051

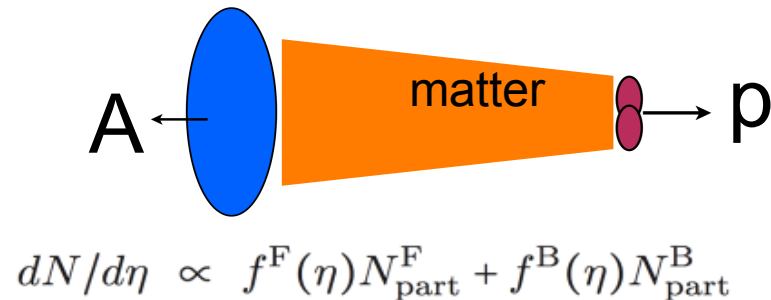


# Origin of pseudorapidity correlations

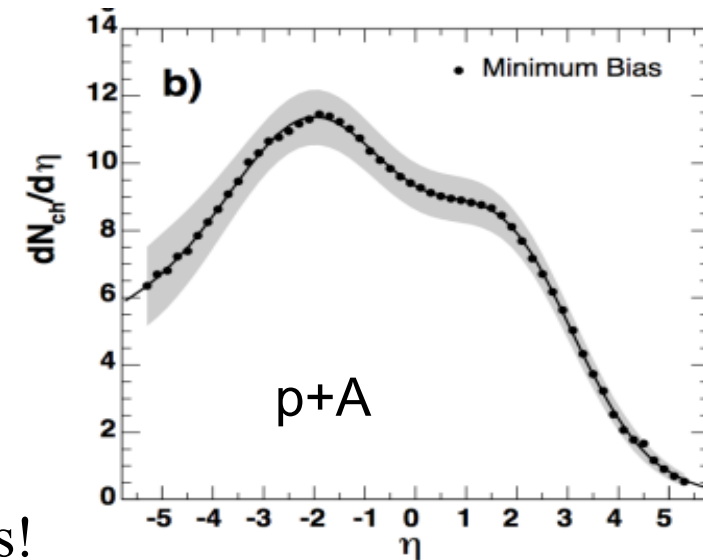
- $dN/d\eta$  shape reflects asymmetry in num. of forward/backward sources
  - Sources can be wounded nucleons, or partons in nucleons (MPI)



- Asymmetry seen directly in  $p+A$  collisions



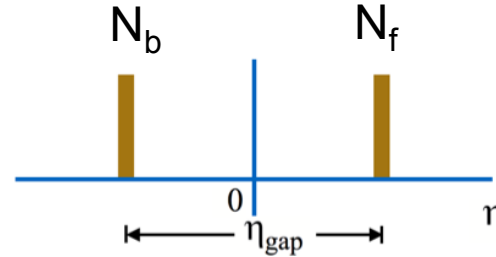
- Naturally exists in  $A+A$  collisions on EbyE bases!
- Goal: understand event-by-event fluctuation of  $dN/d\eta$ 
  1. Probes early time dynamics, longitudinal flow, final state effects.
  2. Inputs for 3+1D hydrodynamic models **W/O** boost invariance



# Observables

## Traditional observables:

Lots of people worked on this



$$b = \frac{\langle N_f N_b \rangle - \langle N_f \rangle \langle N_b \rangle}{\sigma_{N_f} \sigma_{N_b}}$$

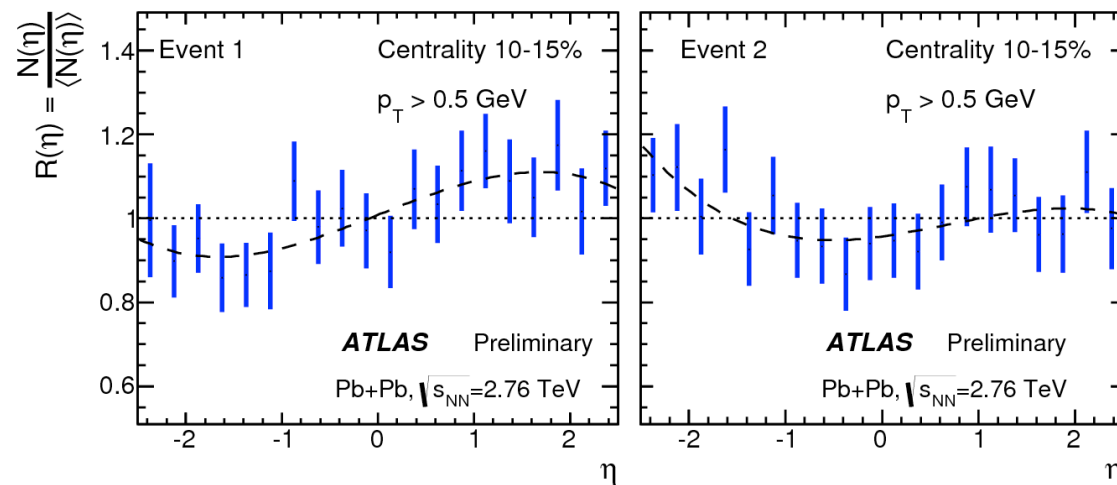
## Alternative observables: 2D correlation function

E. L. Berger, NPB 85 (1975) 61

$$C = \frac{\langle N(\eta_1) N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} = \langle R_S(\eta_1) R_S(\eta_2) \rangle$$

$$R_S(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle}$$

Single particle distribution

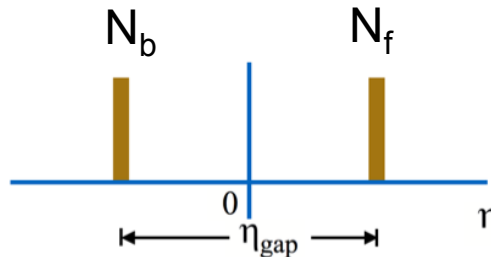


Correlation function disentangles **dynamical** fluctuation from **statistical** fluctuation

# Observables

## Traditional observables:

Lots of people worked on this



$$b = \frac{\langle N_f N_b \rangle - \langle N_f \rangle \langle N_b \rangle}{\sigma_{N_f} \sigma_{N_b}}$$

## Alternative observables: 2D correlation function

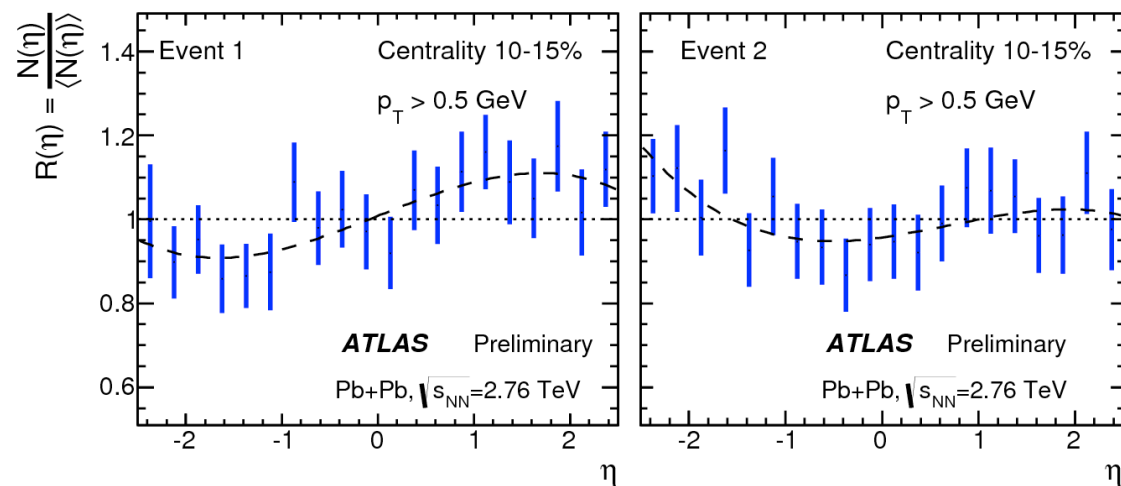
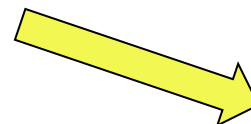
E. L. Berger, NPB 85 (1975) 61

$$C = \frac{\langle N(\eta_1) N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} = \langle R_S(\eta_1) R_S(\eta_2) \rangle$$

$$R_S(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle}$$

Single particle distribution

Mixed events may not match perfectly



Remove residual centrality dependence

$$C_N(\eta_1, \eta_2) = \frac{C(\eta_1, \eta_2)}{C_p(\eta_1) C_p(\eta_2)}$$

$$C_p(\eta_1) = \frac{\int C(\eta_1, \eta_2) d\eta_2}{2Y}, C_p(\eta_2) = \frac{\int C(\eta_1, \eta_2) d\eta_1}{2Y}$$

See 1506.03496 and talk by Peng Huo

Correlation function disentangles **dynamical** fluctuation from **statistical** fluctuation

# Quantifying the shape fluctuations

- EbyE fluct. expanded in Legendre polynomials

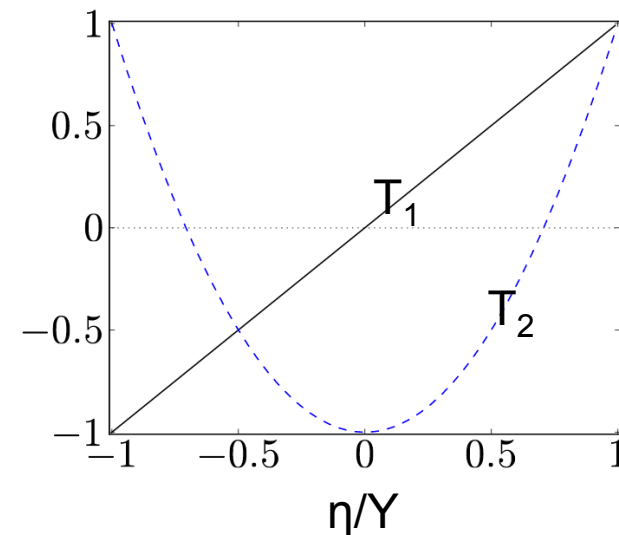
$$R_S(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle} = 1 + \sum_n a_n T_n(\eta) \quad T_n(\eta) \equiv \sqrt{\frac{2n+1}{3}} Y P_n\left(\frac{\eta}{Y}\right)$$

$$P_0(x) = 1, \quad P_1(x) = x, \quad P_2(x) = \frac{1}{2}(3x^2 - 1), \dots$$

$$\eta \in [-Y, Y], \quad Y = 2.4$$

- $a_1 \rightarrow$  fluctuation in the FB asymmetry of  $N(\eta)$ ,
- $a_2 \rightarrow$  fluctuation in the width of  $N(\eta)$

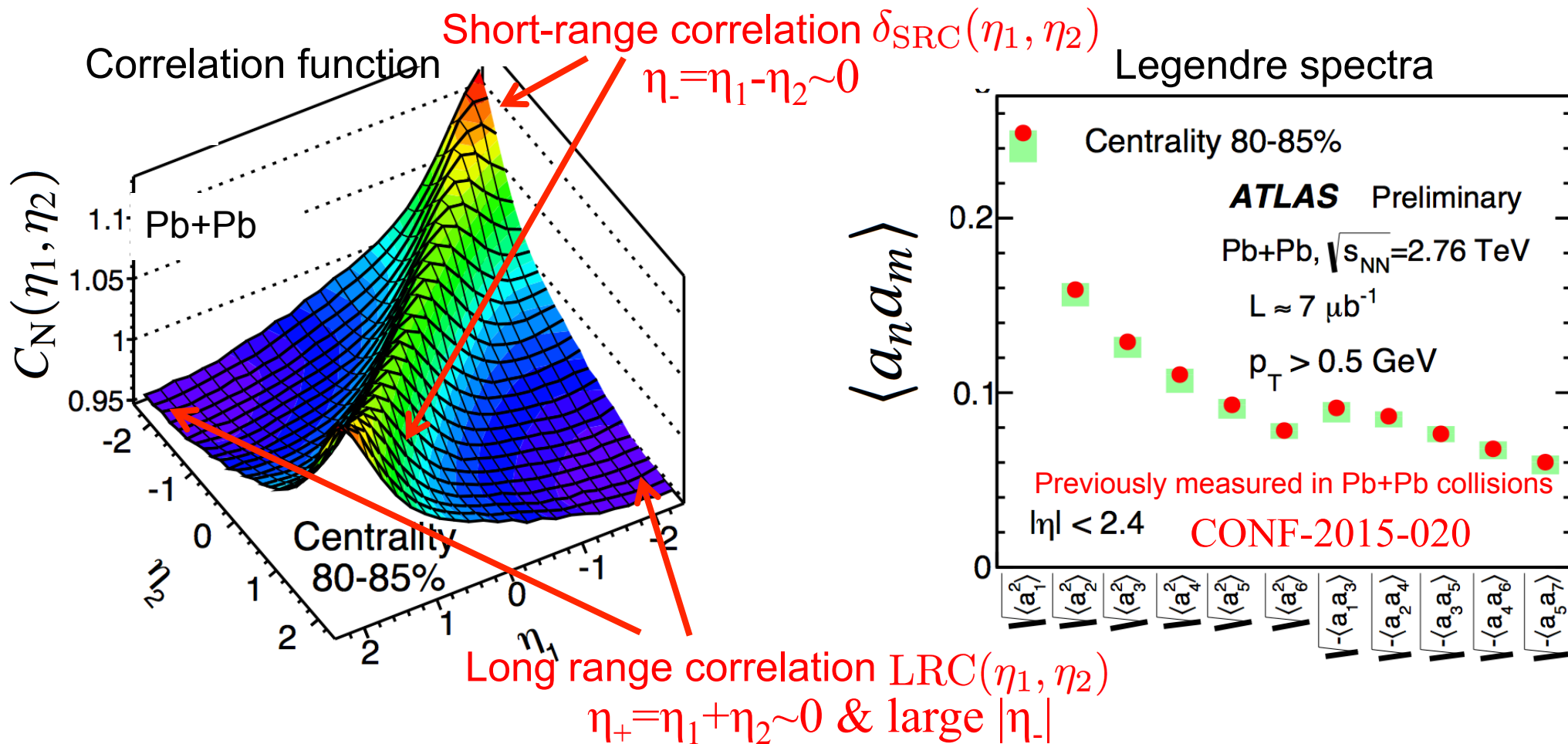
See Bzdak, Teaney 1210.1965



- Legendre expansion of two-particle correlations

$$\begin{aligned} C_N(\eta_1, \eta_2) &= 1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1) T_m(\eta_2) + T_n(\eta_2) T_m(\eta_1)}{2} \\ &= 1 + \langle a_1^2 \rangle \eta_1 \eta_2 + \langle a_2^2 \rangle \frac{5}{12Y^2} (3\eta_1^2 - Y^2)(3\eta_2^2 - Y^2) + \dots \end{aligned}$$

# Features of $C_N(\eta_1, \eta_2)$



- Corr. Func. = short-range corr. (SRC) + long-range corr. (LRC)

Goal of this measurement:

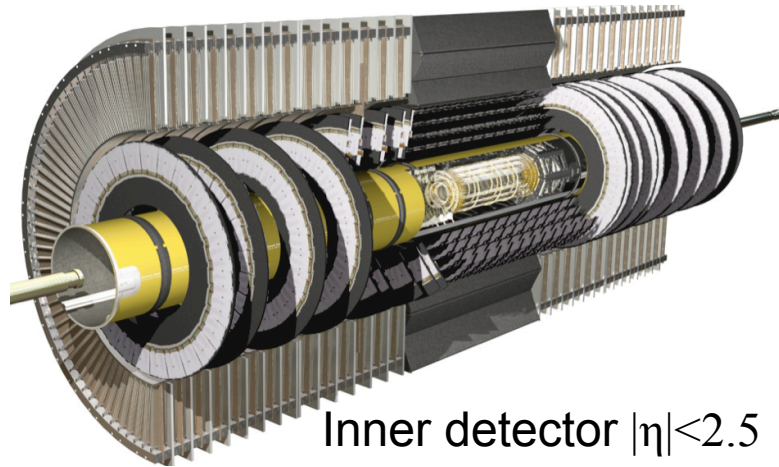
$$C(\eta_1, \eta_2) = 1 + \delta_{\text{SRC}}(\eta_1, \eta_2) + \text{LRC}(\eta_1, \eta_2)$$

1. Data-driven method to separate SRC from LRC
2. Compare SRC or LRC in three collision systems, pp, pPb, PbPb at similar  $N_{\text{ch}}$

# Pb+Pb, p+Pb and pp datasets

7

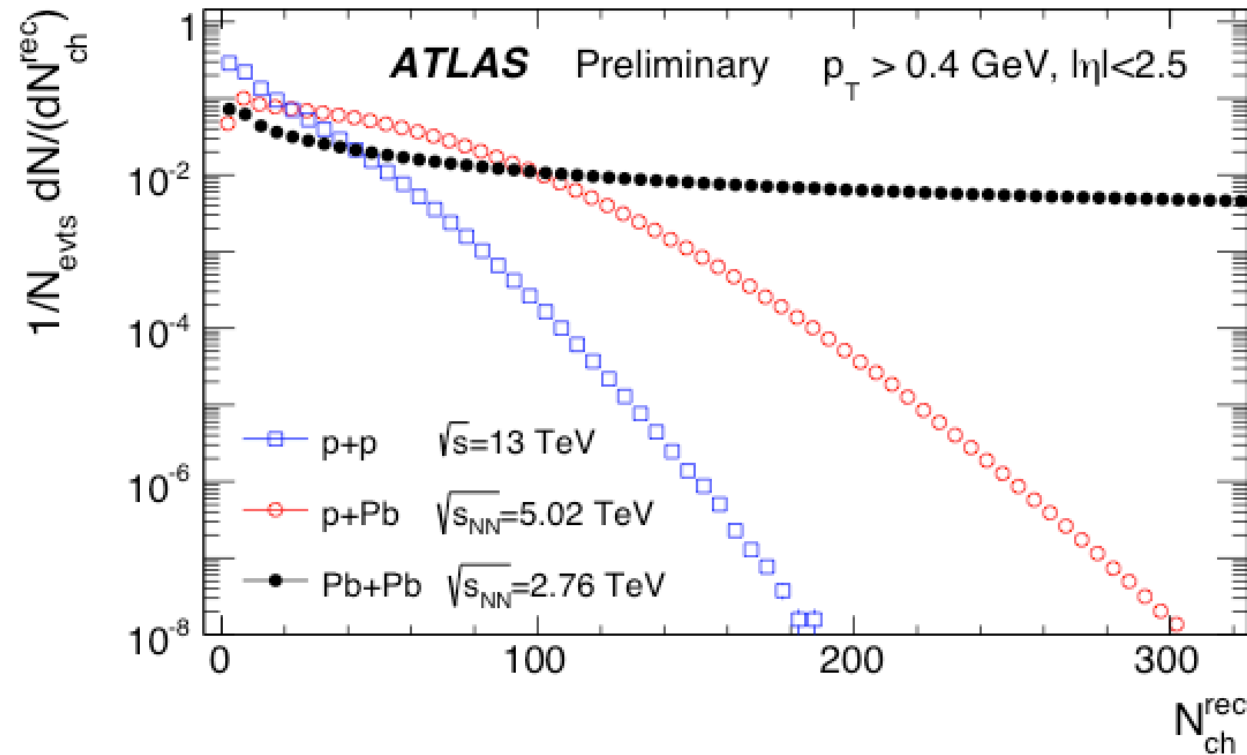
- $C_N(\eta_1, \eta_2)$  calculated using charged particles  $p_T > 0.2$  GeV.
- High-multiplicity track (HMT) trigger used to increase statistics



Pb+Pb 2.76 TeV, 2010, MB

p+Pb 5.02 TeV, 2013, MB+HMT

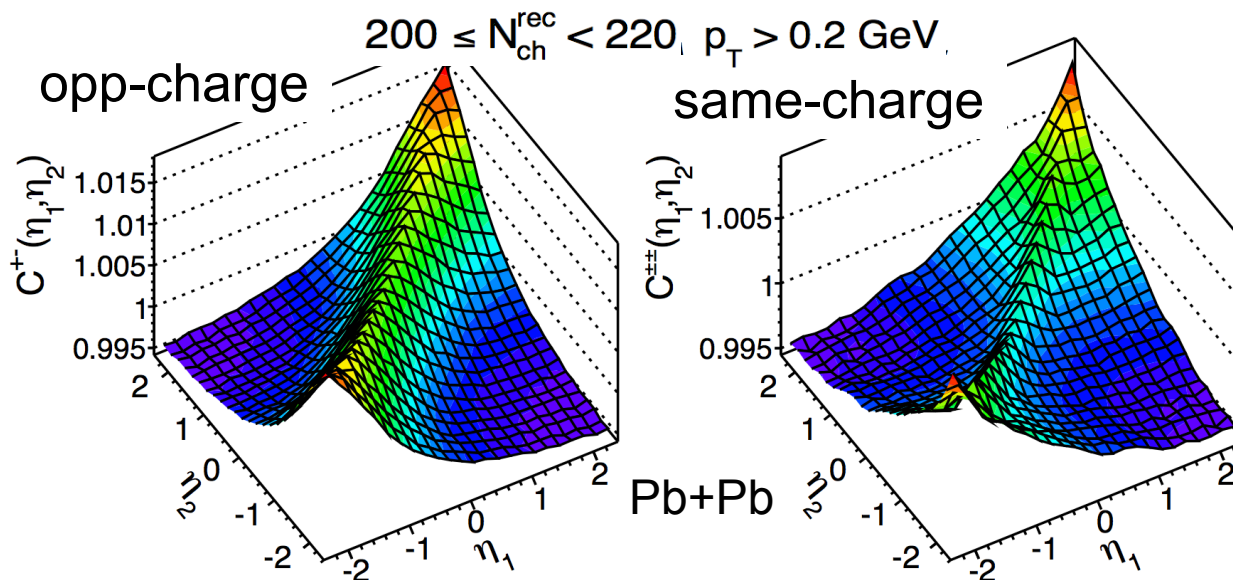
p+p 13 TeV, 2015, MB+HMT



- Analysis carried out in many bins over  $10 \leq N_{\text{ch}}^{\text{rec}} < 300$ .
- Results presented as a function efficiency-corrected values  $N_{\text{ch}} = bN_{\text{ch}}^{\text{rec}}$ 
  - $b \sim 1.19$  for pp and  $\sim 1.29$  for pPb and PbPb

How signals in three systems compare at same  $N_{\text{ch}}$ ?

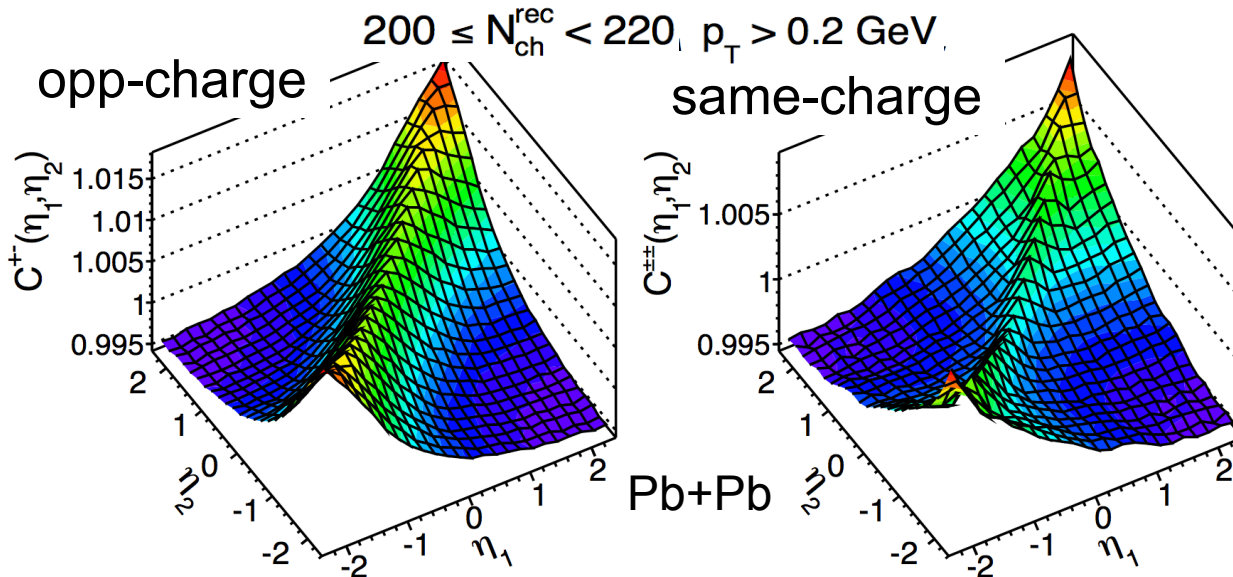
- CF for +- and ++,-- pairs separately.
  - different SRC, similar LRC (based on ratio)





# Properties of short-range correlations

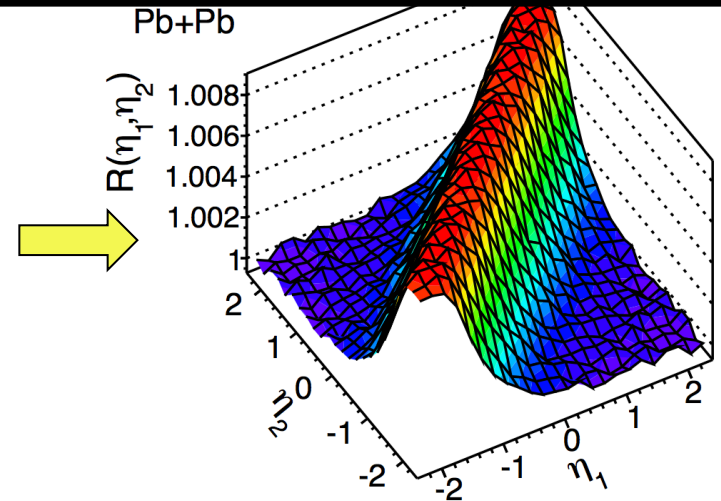
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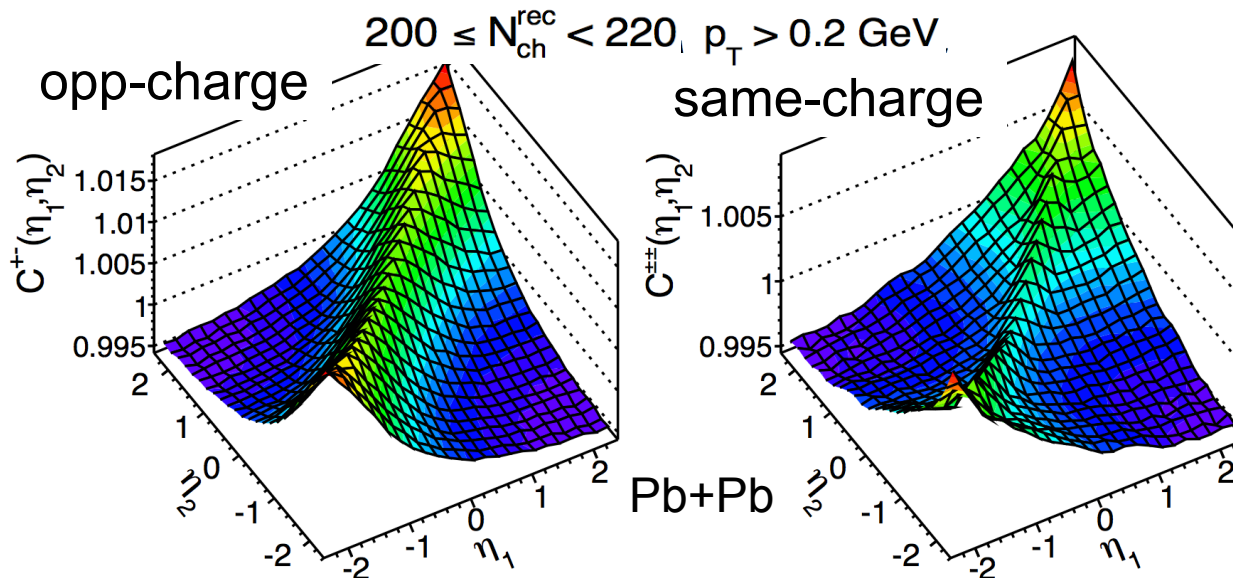
LRC drops out of the ratio

$$R(\eta_+, \eta_-) = \frac{C^{+-}(\eta_+, \eta_-)}{C^{\pm\pm}(\eta_+, \eta_-)} \quad \begin{array}{l} \eta_+ = \eta_1 + \eta_2 \\ \eta_- = \eta_1 - \eta_2 \end{array}$$

$$\approx 1 + \delta_{SRC}^{+-}(\eta_+, \eta_-) - \delta_{SRC}^{\pm\pm}(\eta_+, \eta_-)$$



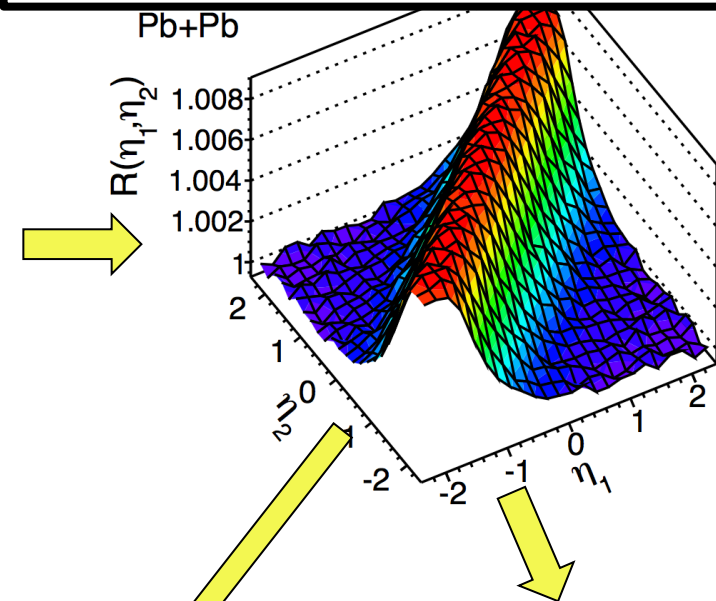
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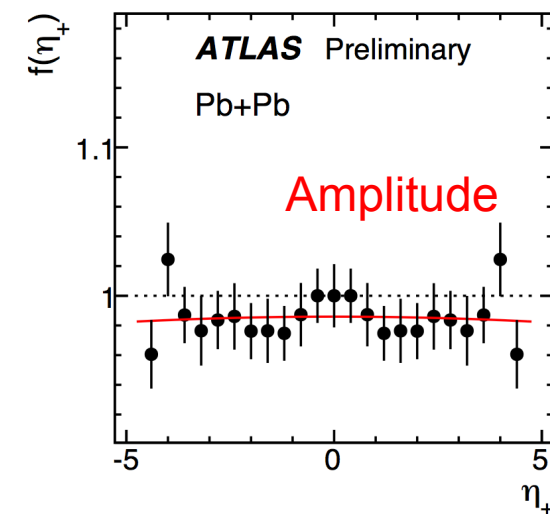
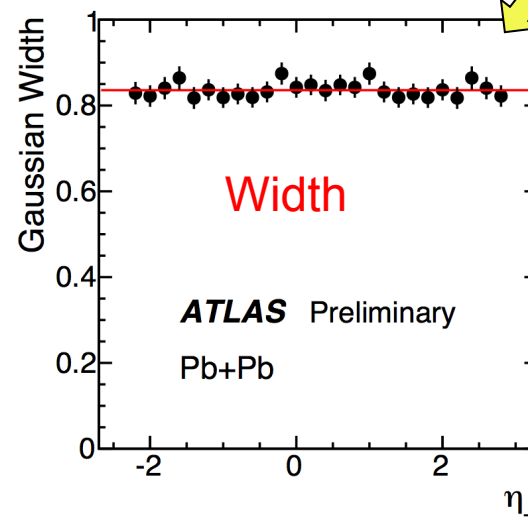
- Amplitude quantified via

$$f(\eta_+) = \frac{\int_{-0.4}^{0.4} R(\eta_+, \eta_-)/0.8 d\eta_- - 1}{\int_{-0.4}^{0.4} R(0, \eta_-)/0.8 d\eta_- - 1}$$

Shape along  $\eta_+$

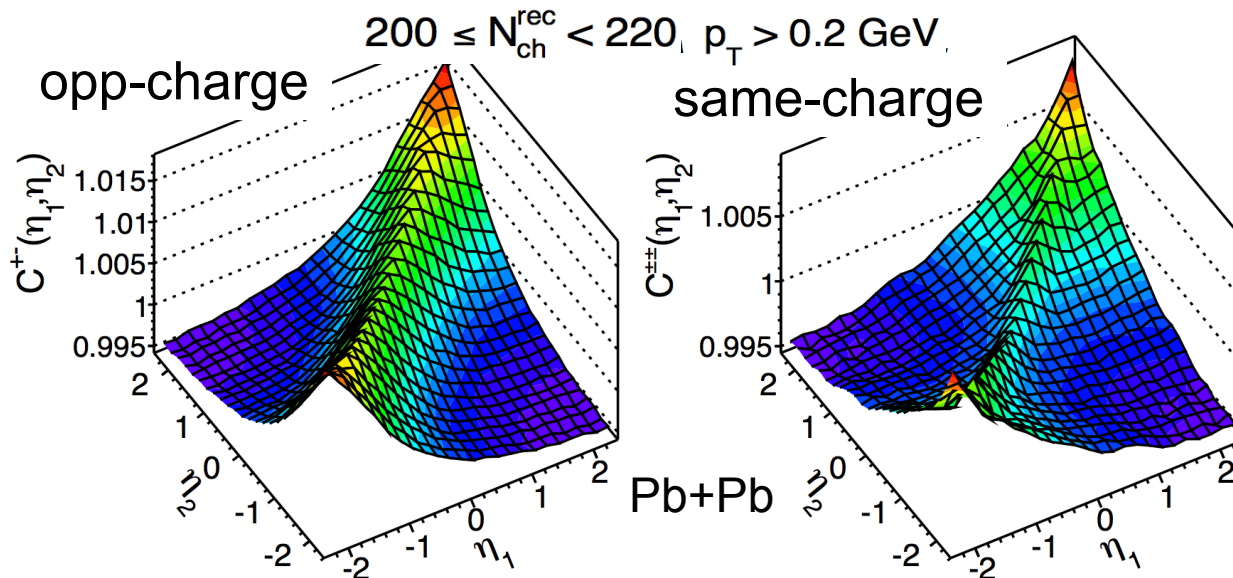
- $\eta_-$  peak width is constant in  $\eta_+$

Shape of  $\delta_{SRC}^{+-} - \delta_{SRC}^{\pm\pm}$   
factorize in  $\eta_+$  and  $\eta_-$



# Properties of short-range correlations

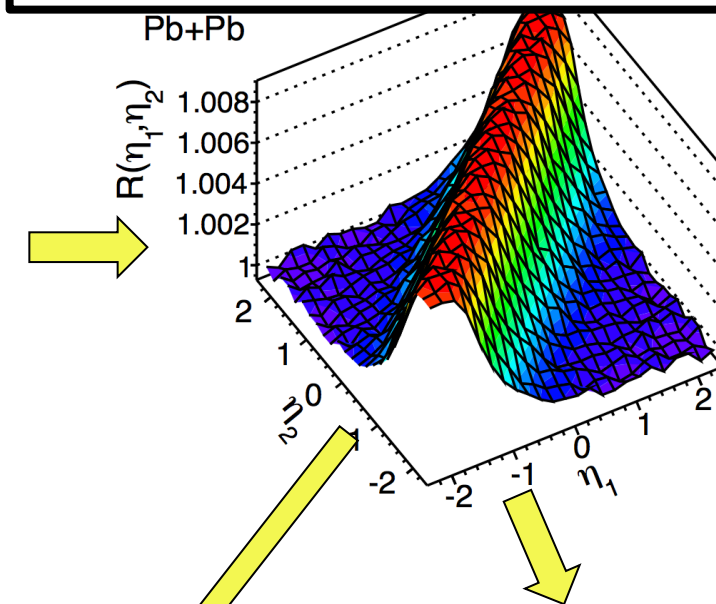
- CF for +- and ++,-- pairs separately.
  - different SRC, similar LRC (based on ratio)



LRC drops out of the ratio

$$R(\eta_+, \eta_-) = \frac{C^{+-}(\eta_+, \eta_-)}{C^{\pm\pm}(\eta_+, \eta_-)} \quad \begin{array}{l} \eta_+ = \eta_1 + \eta_2 \\ \eta_- = \eta_1 - \eta_2 \end{array}$$

$$\approx 1 + \delta_{SRC}^{+-}(\eta_+, \eta_-) - \delta_{SRC}^{\pm\pm}(\eta_+, \eta_-)$$



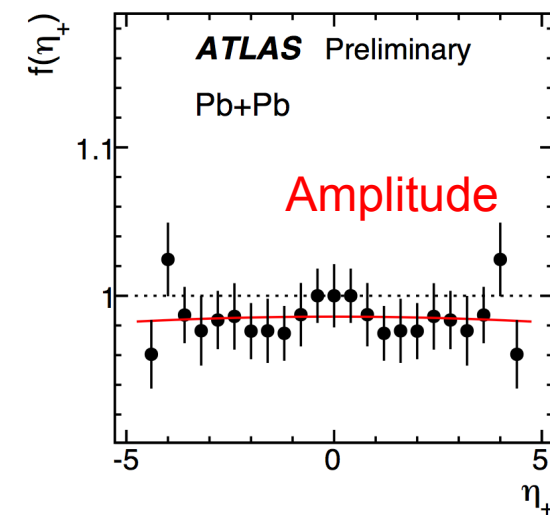
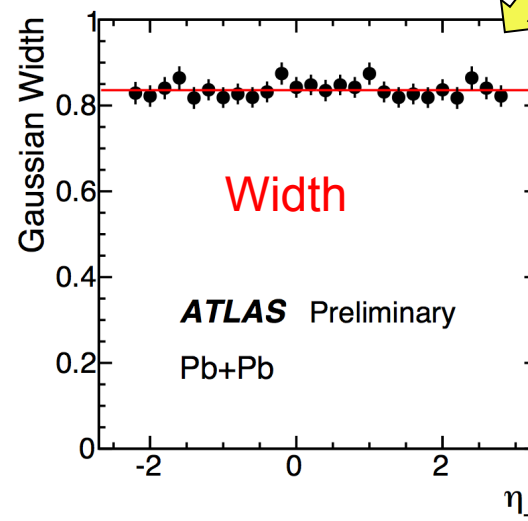
Hence,  $\delta_{SRC}(\eta_+, \eta_-)$  assumed to factorize in  $\eta_+, \eta_-$ .

$$\delta_{SRC}^{+-} = f(\eta_+)g^{+-}(\eta_-)$$

$$\delta_{SRC}^{\pm\pm} = f(\eta_+)g^{\pm\pm}(\eta_-)$$

$$R(\eta_+, \eta_-) \approx 1 + f(\eta_+) [g^{+-}(\eta_-) - g^{\pm\pm}(\eta_-)]$$

Key is to determine  $g(\eta_-)$ !

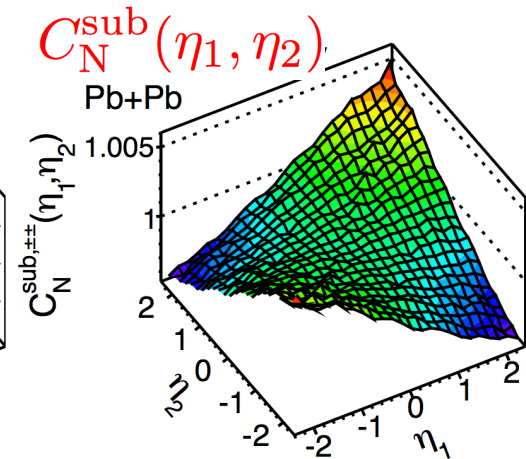
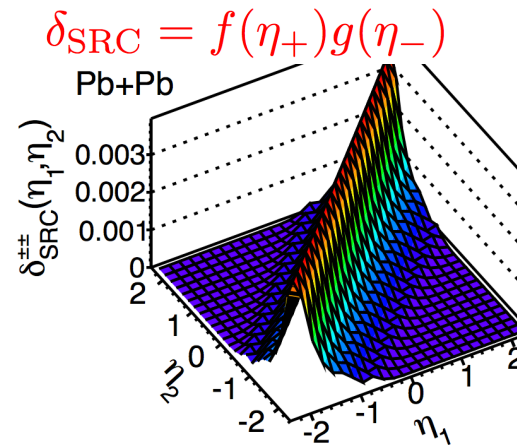
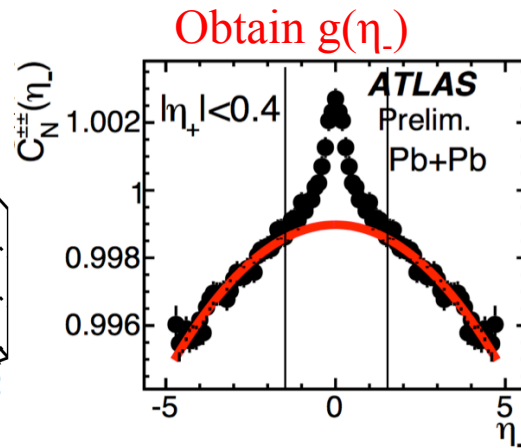
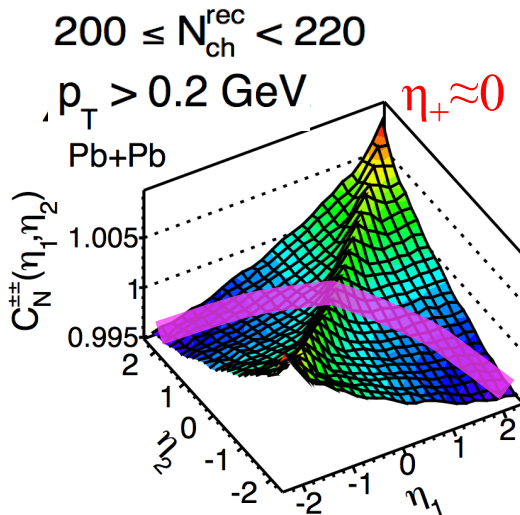


# Estimate short-range correlations

- Take  $C_N(\eta_{\pm})$  in  $|\eta_{\pm}| < 0.4$ , fit a quadratic function in  $|\eta_{\pm}| > \eta_0 = 1.5$ , difference between data and fit in  $|\eta_{\pm}| < 2$  is the  $g(\eta_{\pm})$  for SRC
  - Vary  $\eta_0$  and the range of  $\eta_{\pm}$  slices to check systematics.

$$\delta_{\text{SRC}}^{+-} = f(\eta_+)g^{+-}(\eta_-)$$

$$\delta_{\text{SRC}}^{\pm\pm} = f(\eta_+)g^{\pm\pm}(\eta_-)$$

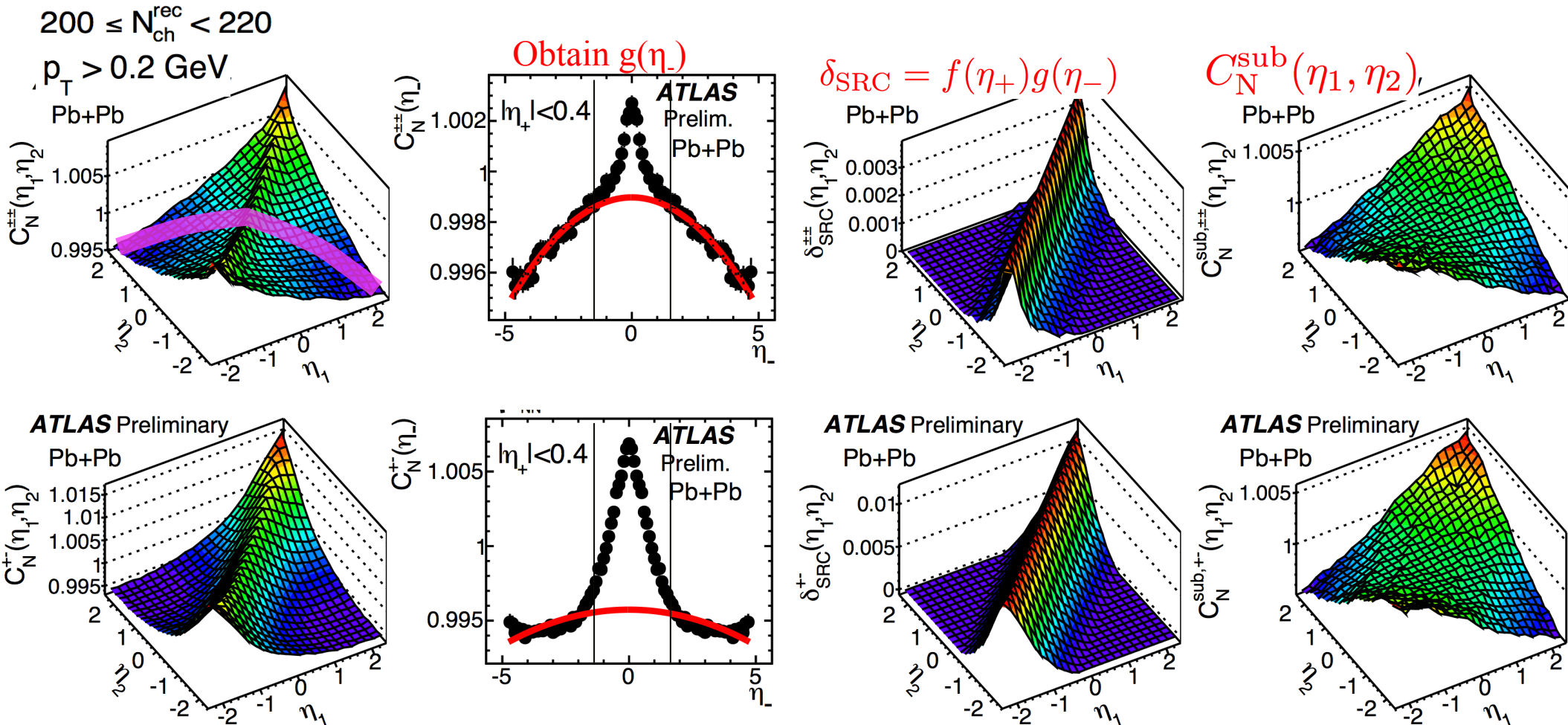


# Estimate short-range correlations

- Take  $C_N(\eta_-)$  in  $|\eta_+| < 0.4$ , fit a quadratic function in  $|\eta_-| > \eta_0 = 1.5$ , difference between data and fit in  $|\eta_-| < 2$  is the  $g(\eta_-)$  for SRC
  - Vary  $\eta_0$  and the range of  $\eta_+$  slices to check systematics.

$$\delta_{\text{SRC}}^{+-} = f(\eta_+)g^{+-}(\eta_-)$$

$$\delta_{\text{SRC}}^{\pm\pm} = f(\eta_+)g^{\pm\pm}(\eta_-)$$



The LRC,  $C_N^{\text{sub}}(\eta_+, \eta_-)$ , has similar magnitudes between ++, -- and +-.

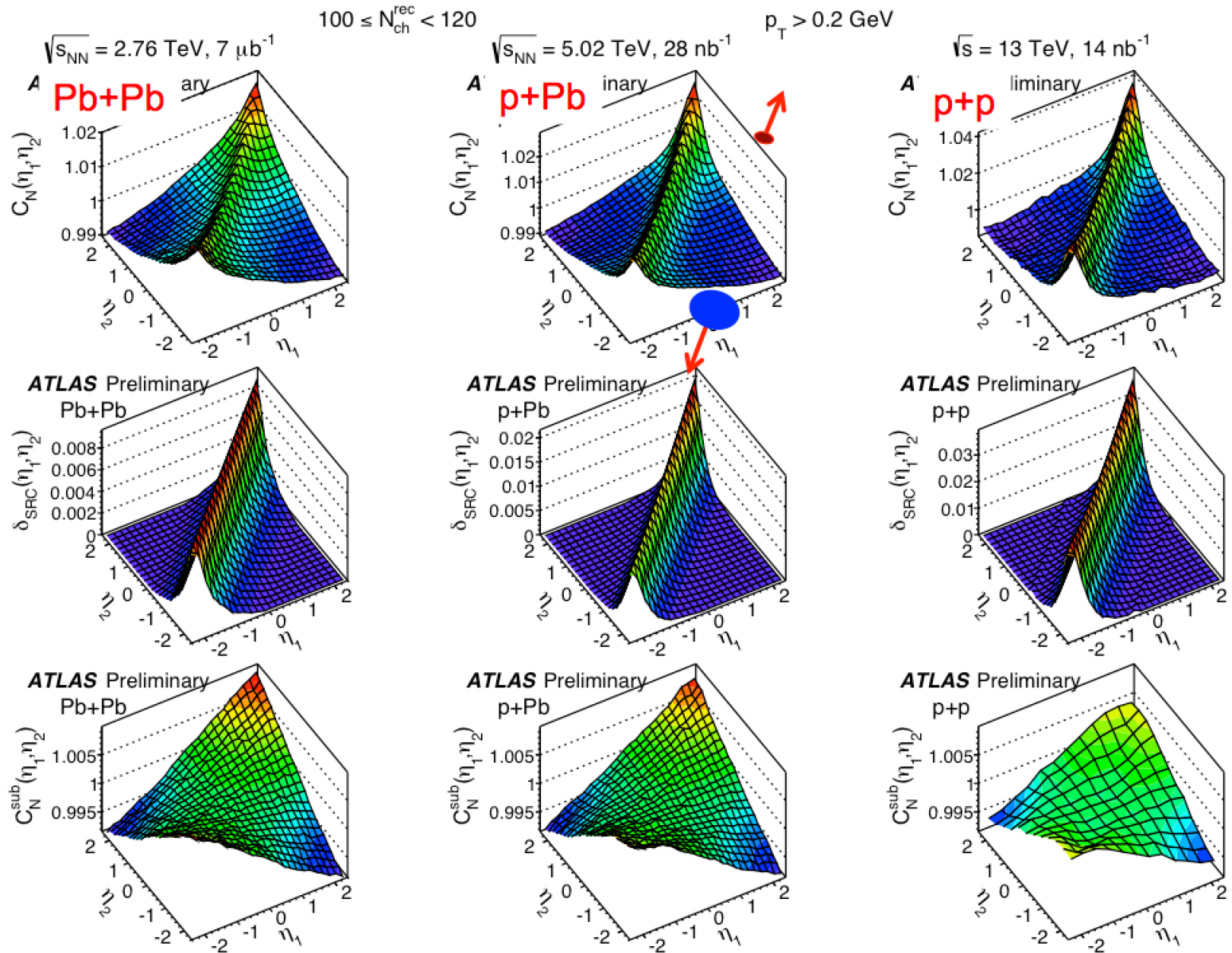
# Results

# Correlation functions in three systems

$$C_N(\eta_1, \eta_2)$$

$$\delta_{\text{SRC}}(\eta_1, \eta_2)$$

$$C_N^{\text{sub}}(\eta_1, \eta_2)$$



After SRC subtraction, similar LRC in all three systems

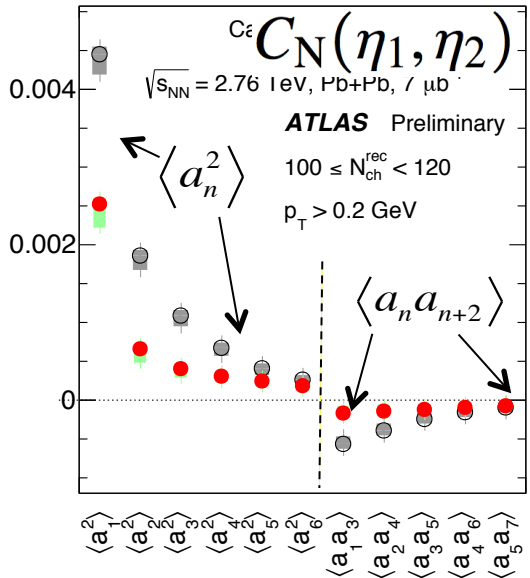
Most FB asymmetry in pPb collisions is due to the SRC.

# Legendre spectra in Pb+Pb

$$C_N(\eta_1, \eta_2) \text{ or } C_N^{\text{sub}}(\eta_1, \eta_2) = 1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}$$

Pb+Pb

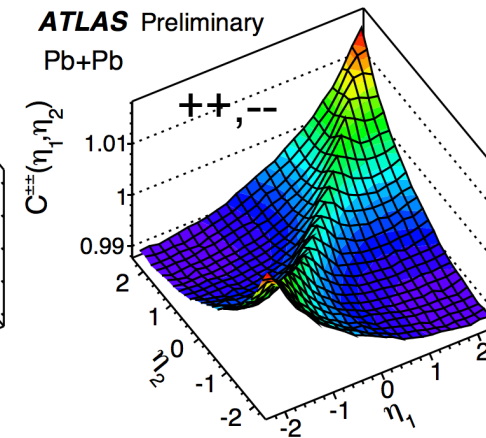
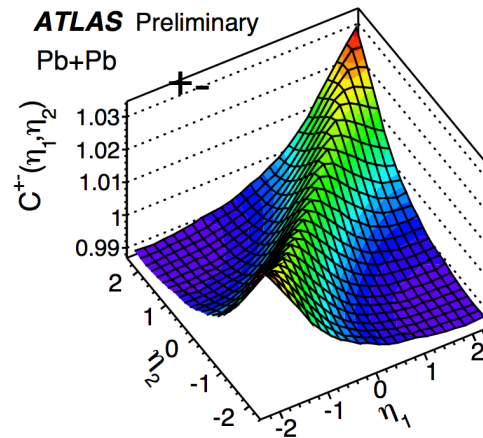
Before subtraction



○ +- pairs

● ++, -- pairs

Before SRC subtraction



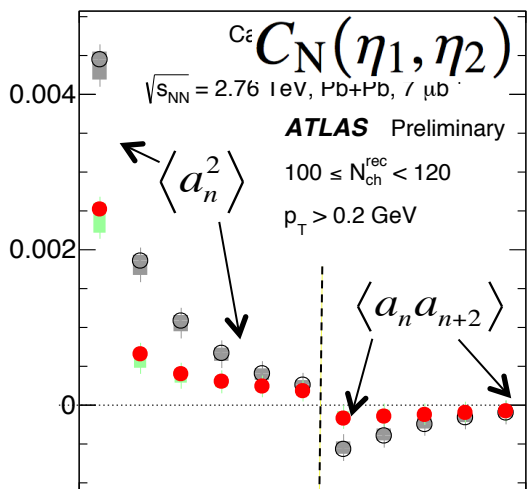
- The strong charge dependence  $\rightarrow$  SRC contributes to all coefficients



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Pb+Pb

Before subtraction

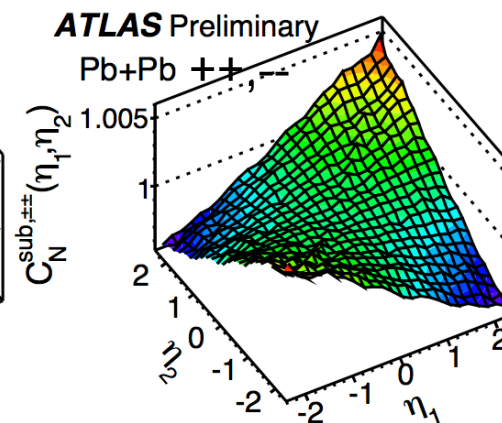
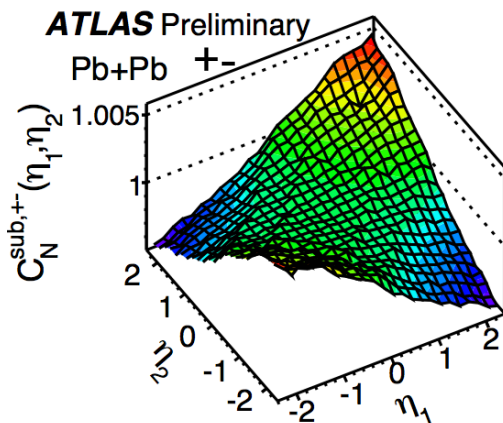
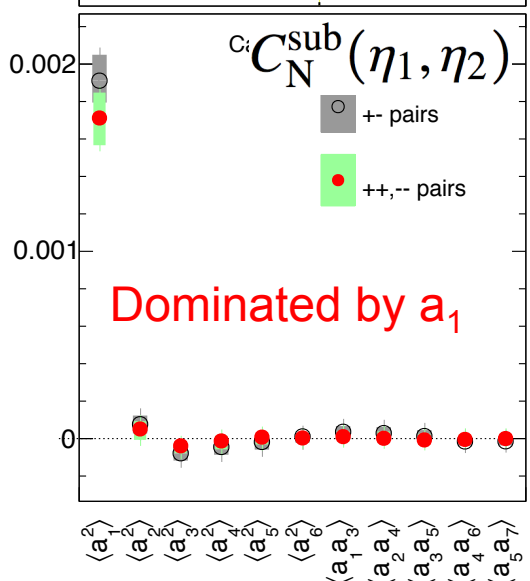


○ +- pairs

● ++,-- pairs

After SRC subtraction

After subtraction



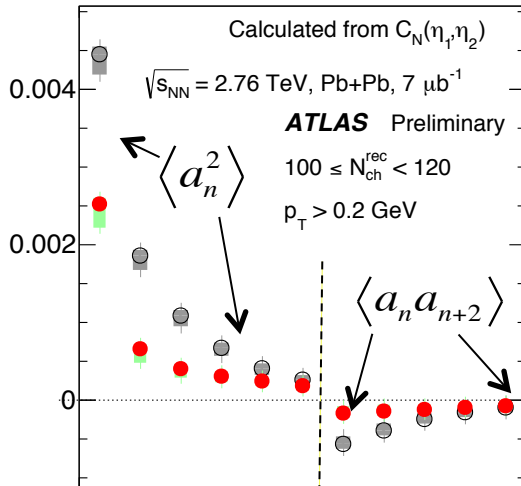
- The strong charge dependence  $\rightarrow$  SRC contributes to all coefficients
- After SRC removal, results are independent of charge combinations!

# Legendre spectra in three systems

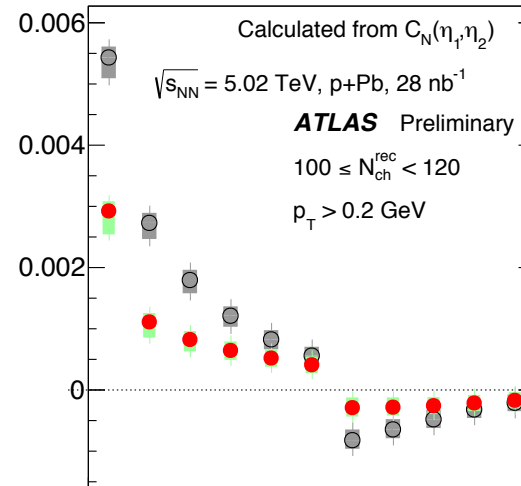
$$C_N(\eta_1, \eta_2) \text{ or } C_N^{\text{sub}}(\eta_1, \eta_2) = 1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}$$

Before subtraction

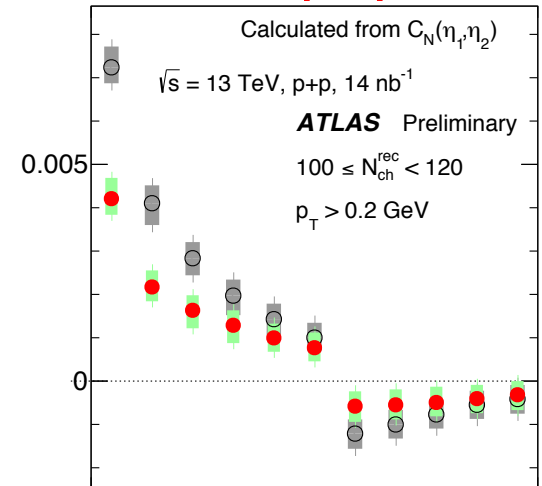
**Pb+Pb**



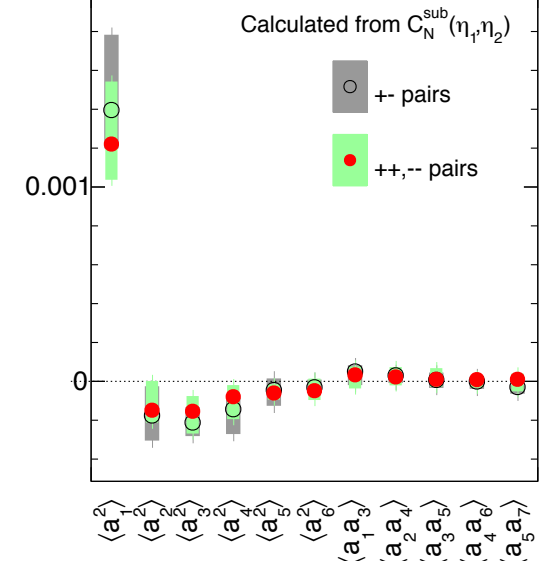
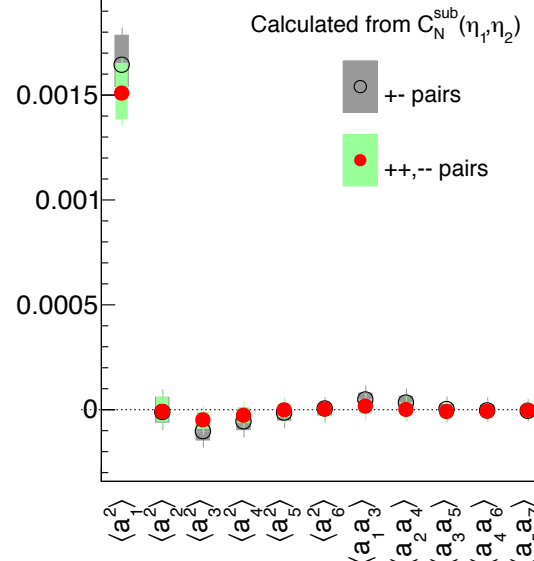
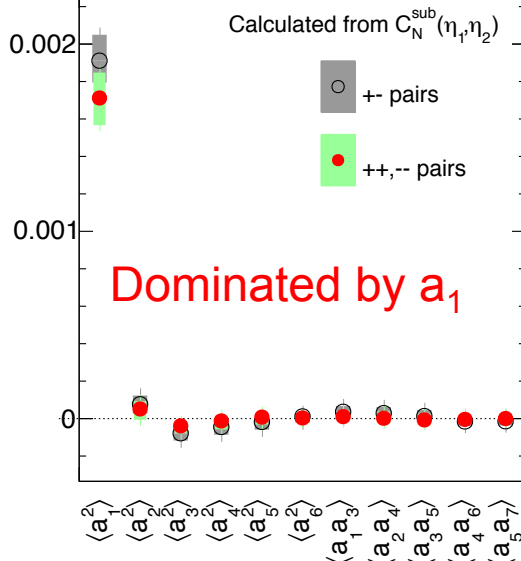
**p+Pb**



**p+p**



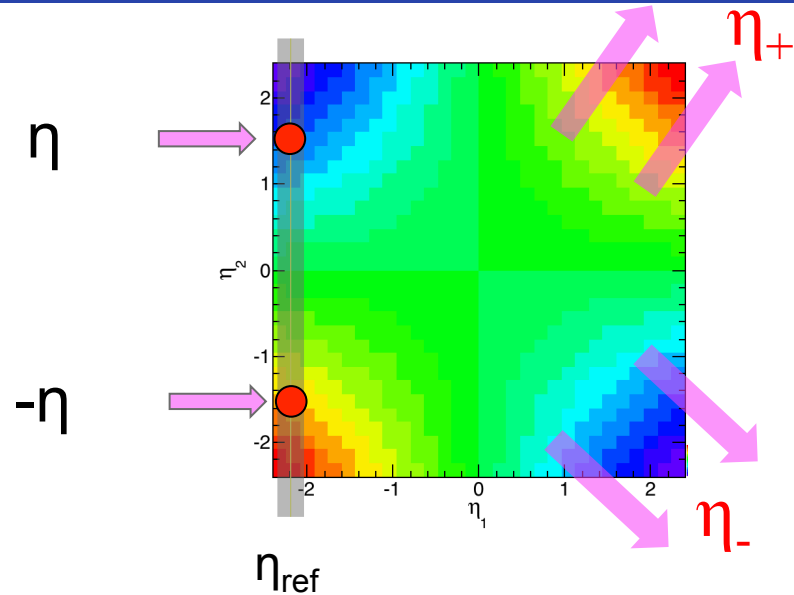
After subtraction



- The strong charge dependence  $\rightarrow$  SRC contributes to all coefficients

After SRC removal, results are independent of charge combinations!

# Projections of correlation function



CF dominated by  $a_1$ , thus:

$$C_N^{\text{sub}}(\eta_1, \eta_2) \approx 1 + \langle a_1^2 \rangle \eta_1 \eta_2 = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

2. Quadratic fit of  $C_N^{\text{sub}}(\eta_-)$  in narrow slice of  $\eta_+$ , this gives  $a_1$  as a function of  $\eta_+$ .
3. Quadratic fit of  $C_N^{\text{sub}}(\eta_+)$  in narrow slice of  $\eta_-$ , this gives  $a_1$  as a function of  $\eta_-$ .
4. Linear fit of the  $\eta$  dependence of  $r_N^{\text{sub}}(\eta, \eta_{\text{ref}})$  in narrow slice of  $\eta_{\text{ref}}$ .

$$r_N^{\text{sub}}(\eta, \eta_{\text{ref}}) = C_N^{\text{sub}}(-\eta, \eta_{\text{ref}}) / C_N^{\text{sub}}(\eta, \eta_{\text{ref}}) = 1 - 2 \langle a_1^2 \rangle \eta \eta_{\text{ref}}$$

similar to the CMS correlator for flow decorrelation 1503.01692

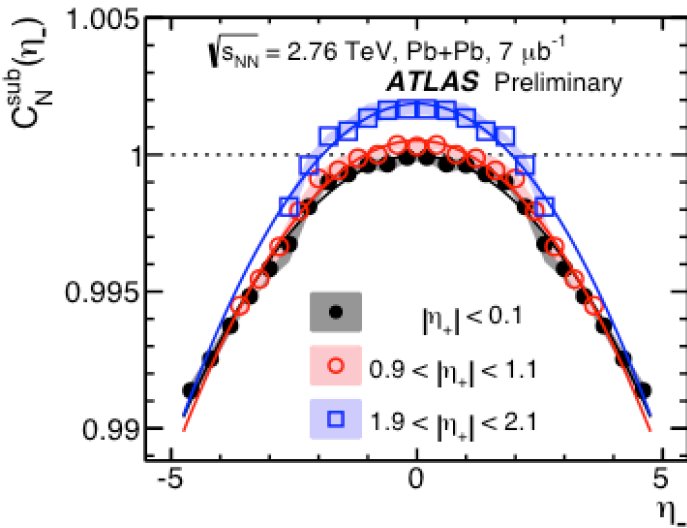
Compare to  $a_1$  obtained from Legendre expansion method

**Fit in limited  $\eta_1$  and  $\eta_2$  space, the systematics largely independent!**

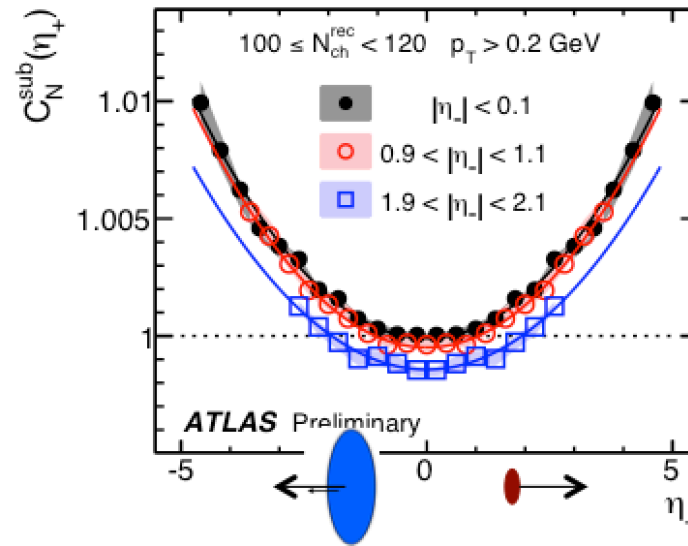
# Projections of CF in p+Pb

$$C_N^{\text{sub}}(\eta_1, \eta_2) \approx 1 + \langle a_1^2 \rangle \eta_1 \eta_2 = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2) \quad r_N^{\text{sub}}(\eta, \eta_{\text{ref}}) = 1 - 2 \langle a_1^2 \rangle |\eta_{\text{ref}}| \eta$$

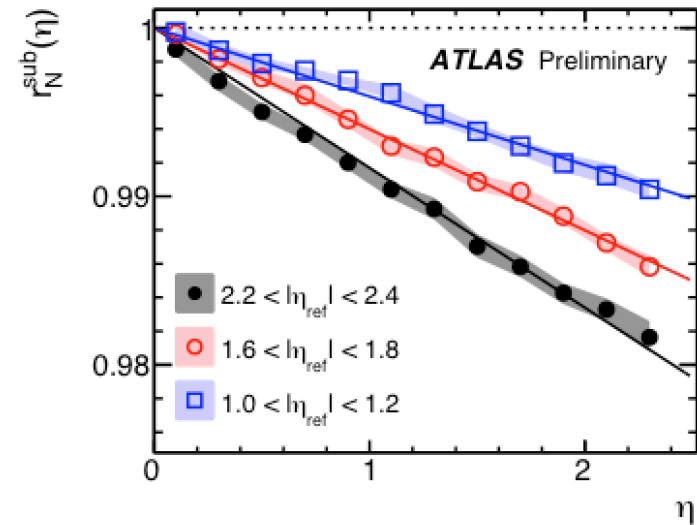
Fit  $\eta_-$  dependence



Fit  $\eta_+$  dependence



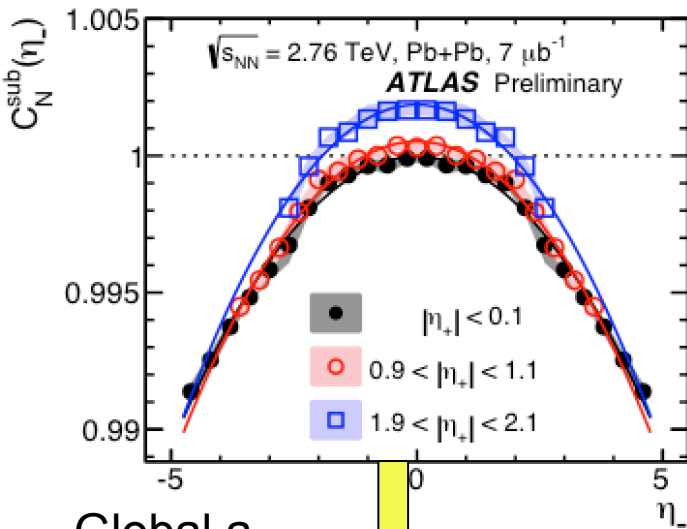
Fit  $\eta$  dependence



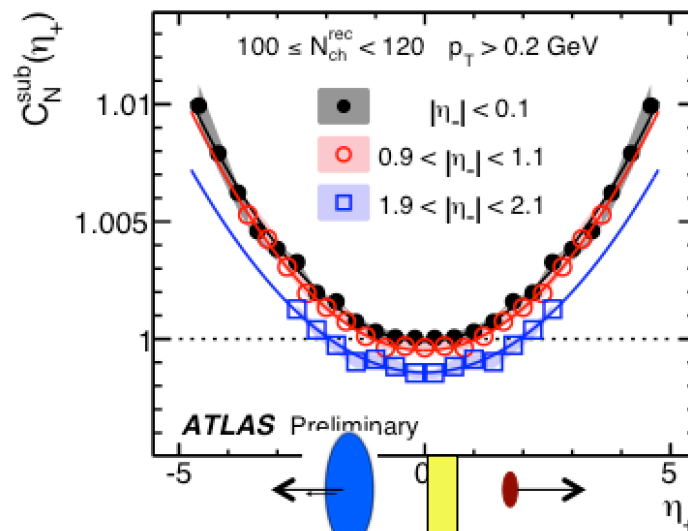
# Projections of CF in p+Pb

$$C_N^{\text{sub}}(\eta_1, \eta_2) \approx 1 + \langle a_1^2 \rangle \eta_1 \eta_2 = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2) \quad r_N^{\text{sub}}(\eta, \eta_{\text{ref}}) = 1 - 2 \langle a_1^2 \rangle |\eta_{\text{ref}}| \eta$$

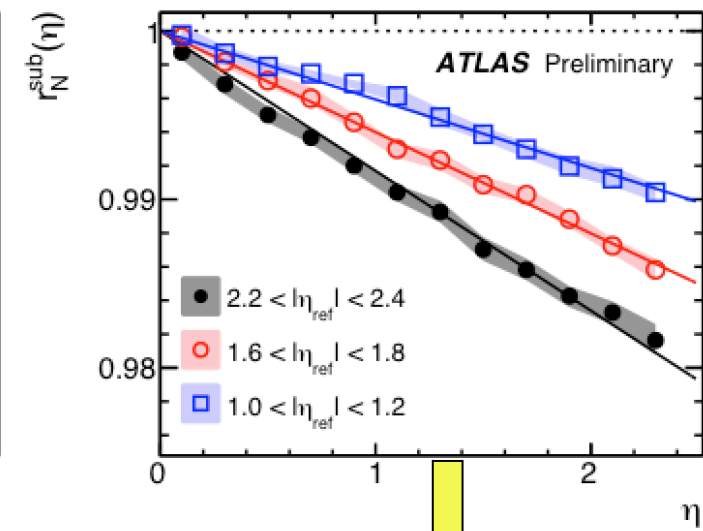
Fit  $\eta_-$  dependence



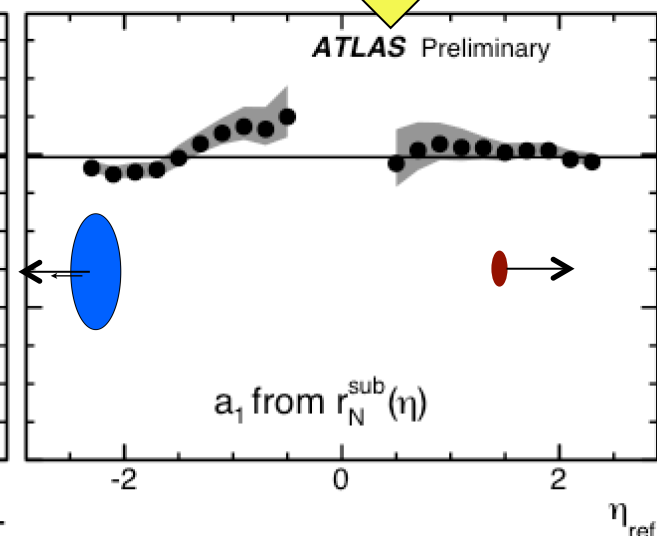
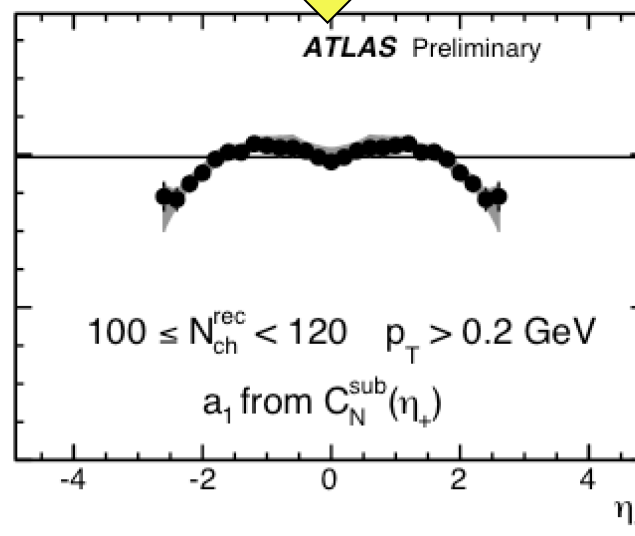
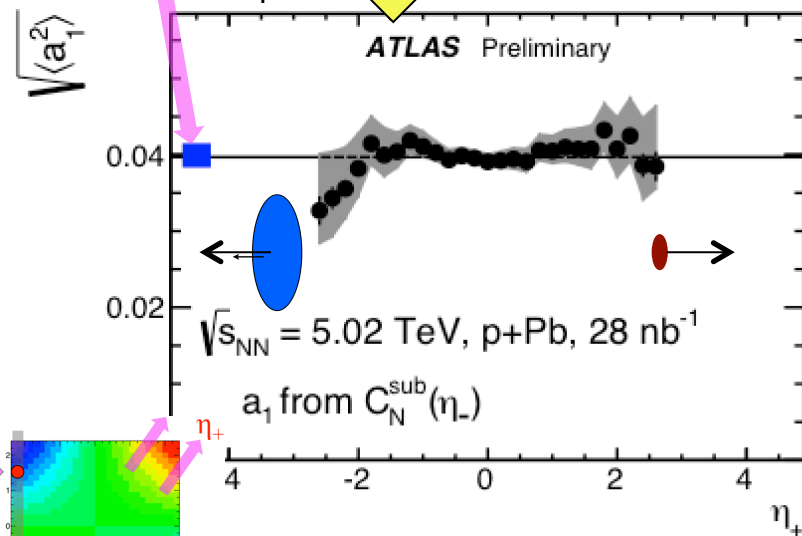
Fit  $\eta_+$  dependence



Fit  $\eta$  dependence



Global  $a_1$

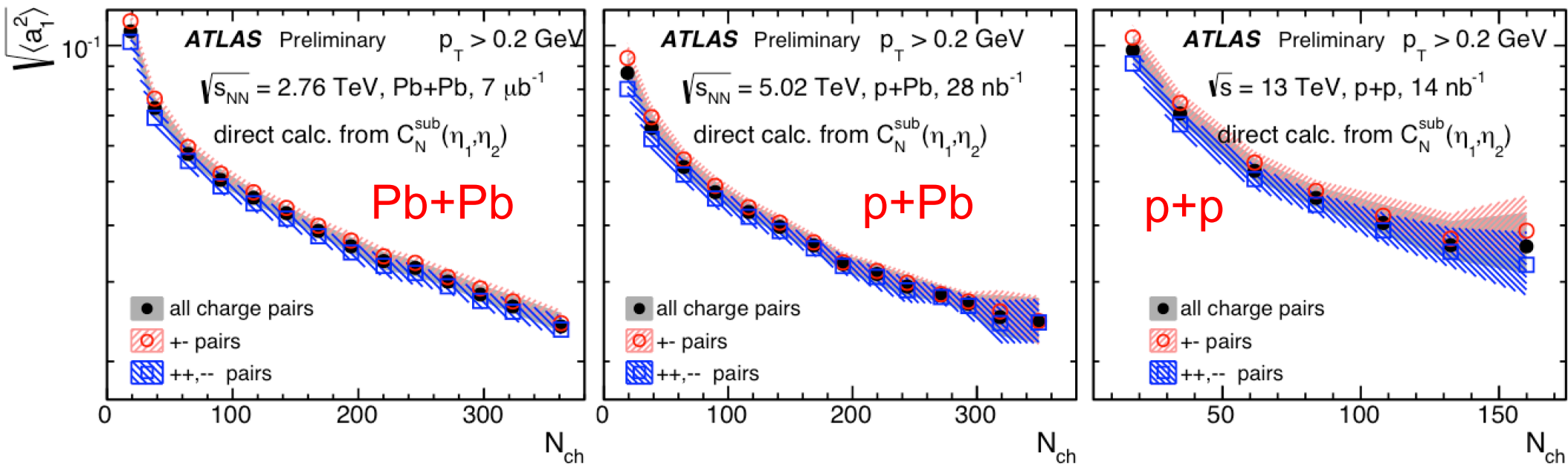


LRC is  $\sim$ symmetric between proton- and lead-going side!

# $N_{\text{ch}}$ dependence of LRC (in terms of $a_1$ )

$$C_N^{\text{sub}}(\eta_1, \eta_2) \approx 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$

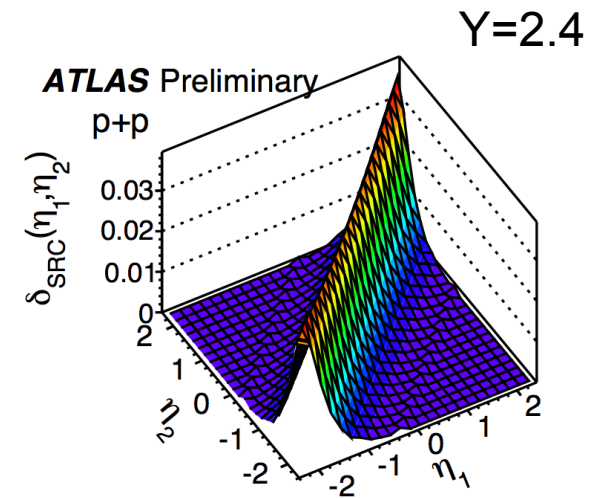
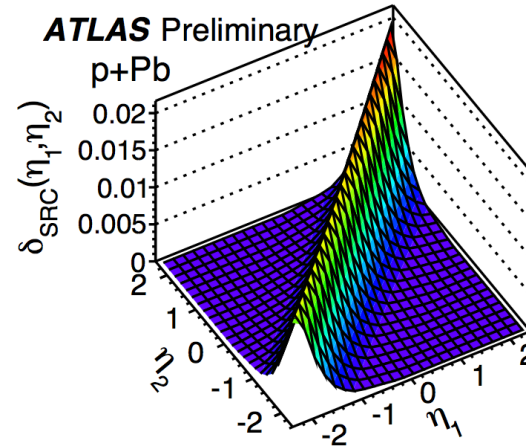
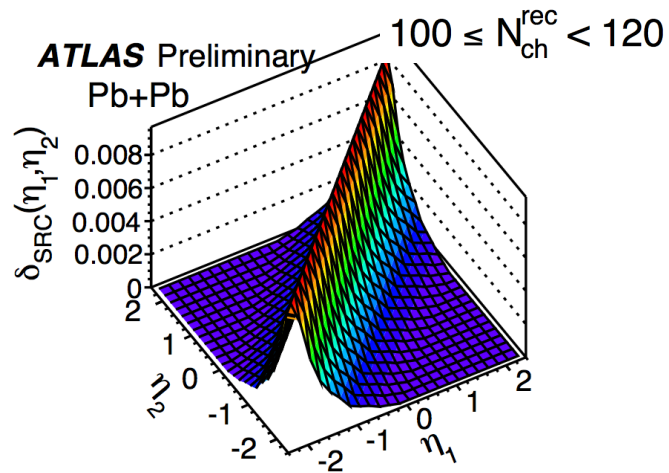
- Calculated from Legendre expansion method for all-charge, opposite-charge and all-charge pairs



No dependence on charge combinations

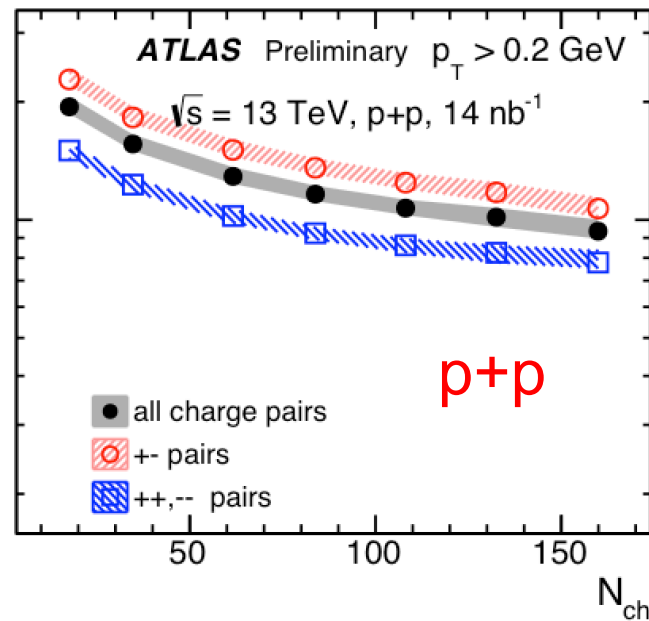
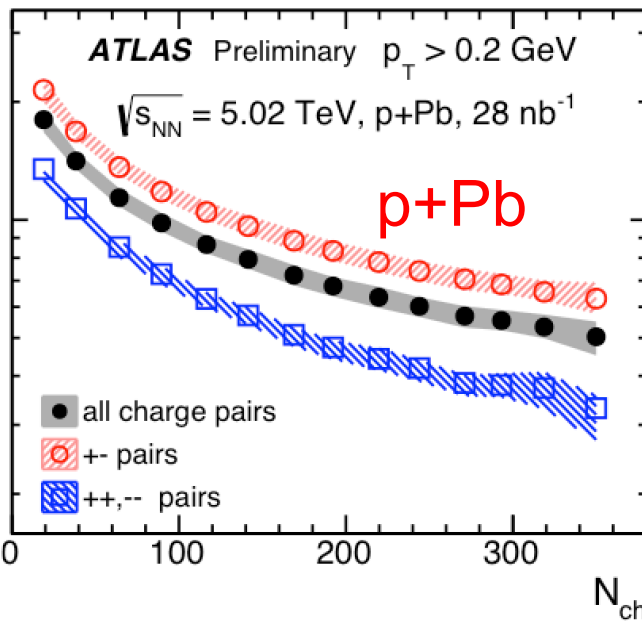
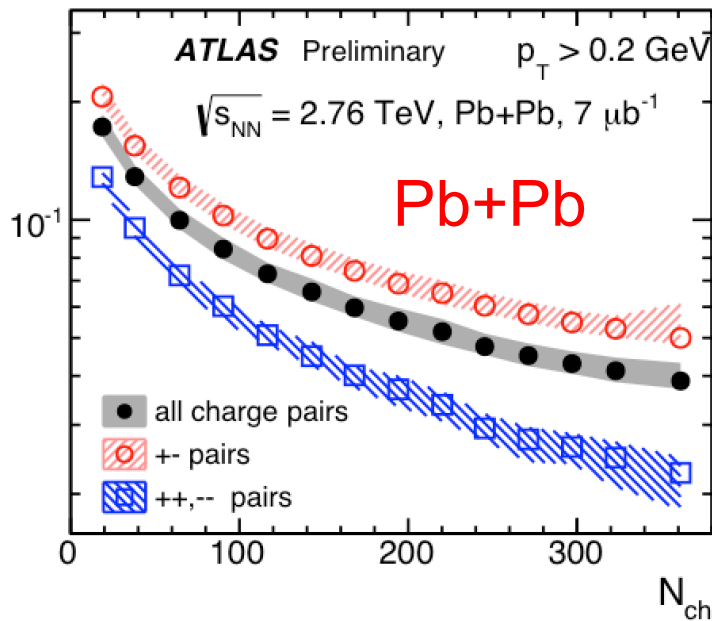
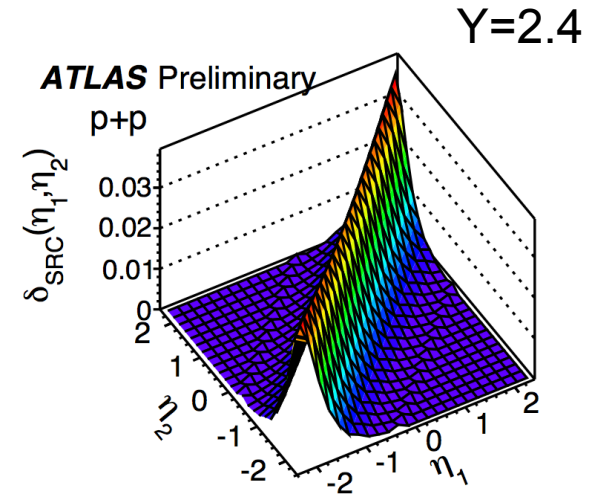
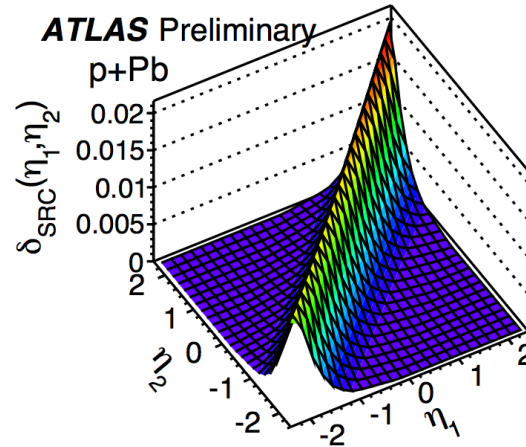
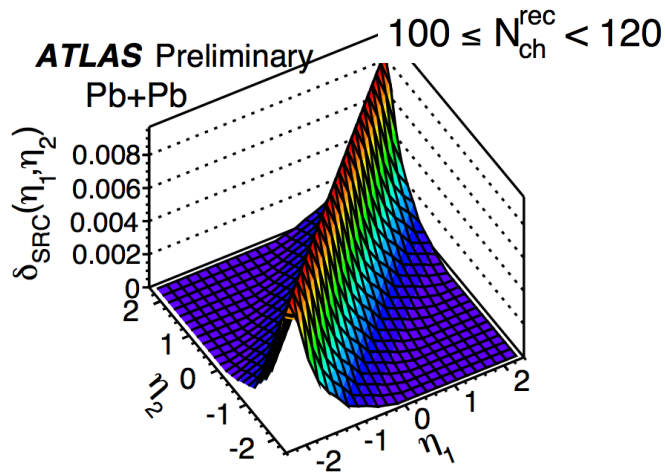
# $N_{ch}$ dependence of SRC

- Quantify SRC using its average amplitude  $\Delta_{SRC} = \frac{\int \delta_{SRC}(\eta_1, \eta_2) d\eta_1 d\eta_2}{4Y^2}$



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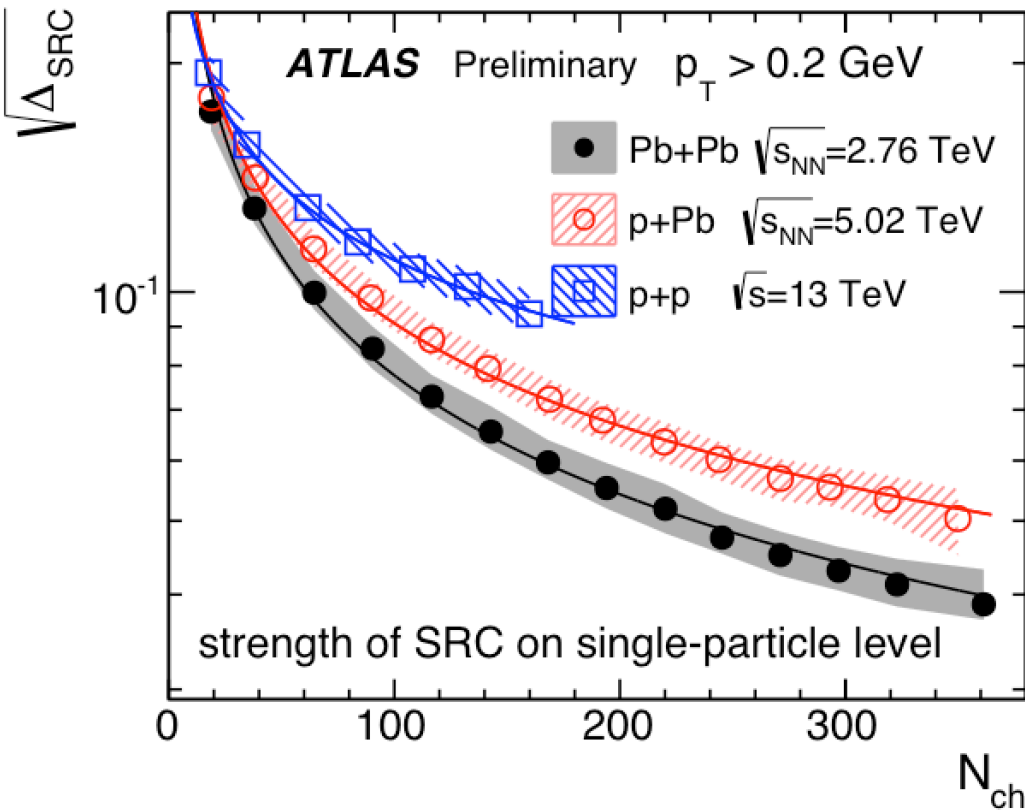


**Strong dependence on charge and system size**

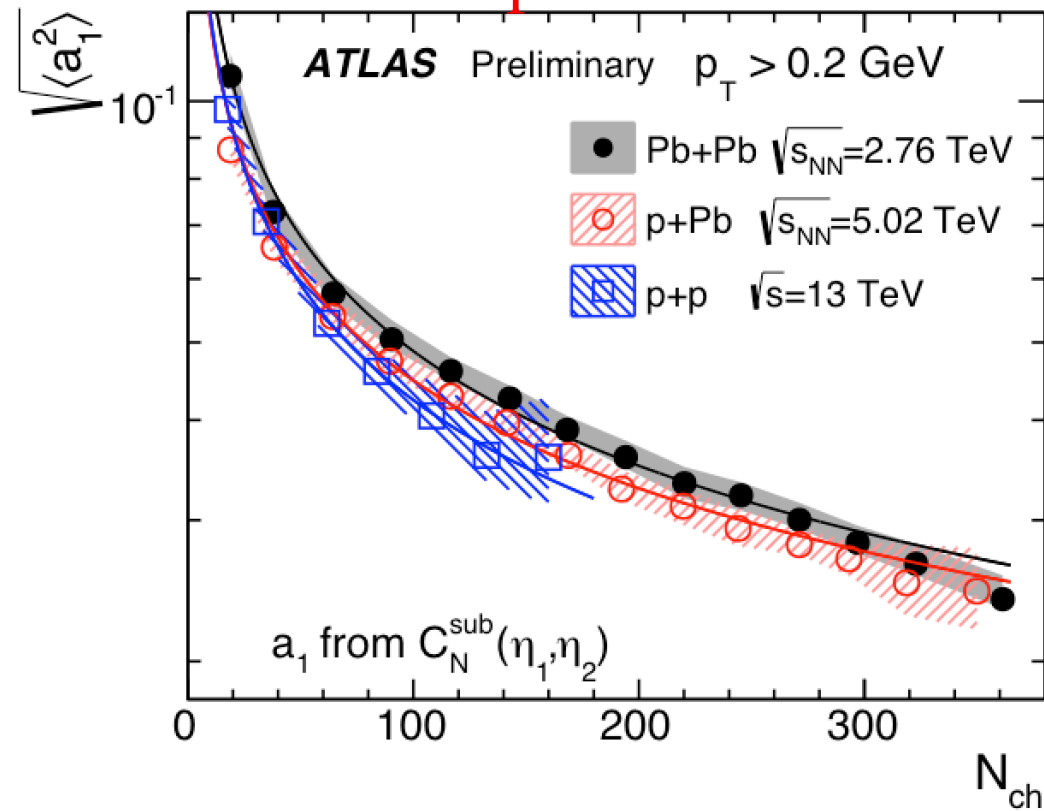


# $N_{\text{ch}}$ dep. of SRC and $a_1$ in three systems

## SRC



## $a_1$ for LRC



- They follow power-law function Fit with  $c/N_{\text{ch}}^\alpha$

	Pb+Pb	p+Pb	pp
$\alpha$ for $\sqrt{\Delta_{\text{SRC}}}$	$0.502 \pm 0.022$	$0.451 \pm 0.020$	$0.342 \pm 0.030$
$\alpha$ for $\sqrt{\langle a_1^2 \rangle}$	$0.467 \pm 0.011$	$0.448 \pm 0.019$	$0.489 \pm 0.032$

# Expected scaling behavior?

- SRC can be related to the number of sources  $n$  contributing to  $N_{\text{ch}}$

$$n = n_f + n_b \propto N_{\text{ch}}$$

- LRC expected to be related to the asymmetry between  $n_f$  and  $n_b$

$$A_n = \frac{n_f - n_b}{n_f + n_b}, \quad \langle a_1^2 \rangle \propto \langle A_n^2 \rangle$$

- Assume **independent cluster picture** NPB85 (1975)61: each source emits the same number of pairs and the number of sources follows Poisson fluctuations, then

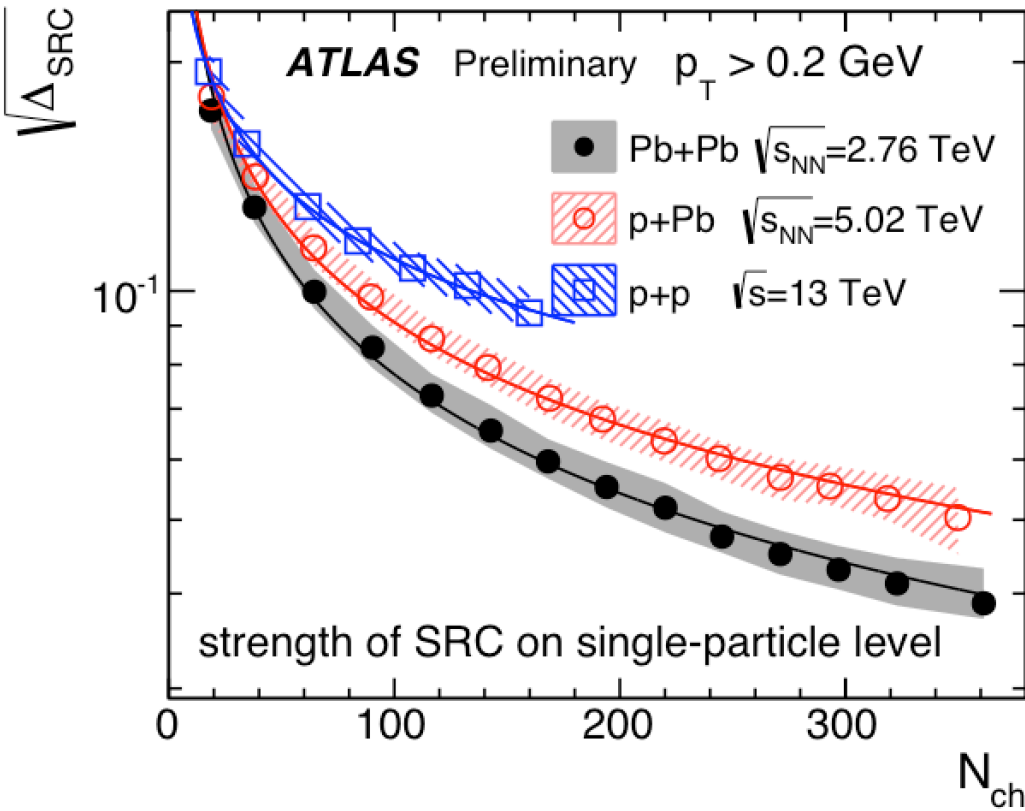
$$\sqrt{\Delta_{\text{SRC}}} \sim \sqrt{\langle a_1^2 \rangle} \sim \frac{1}{n^\alpha} \sim \frac{1}{N_{\text{ch}}^\alpha}, \quad \alpha \sim 0.5$$

Sources could be:

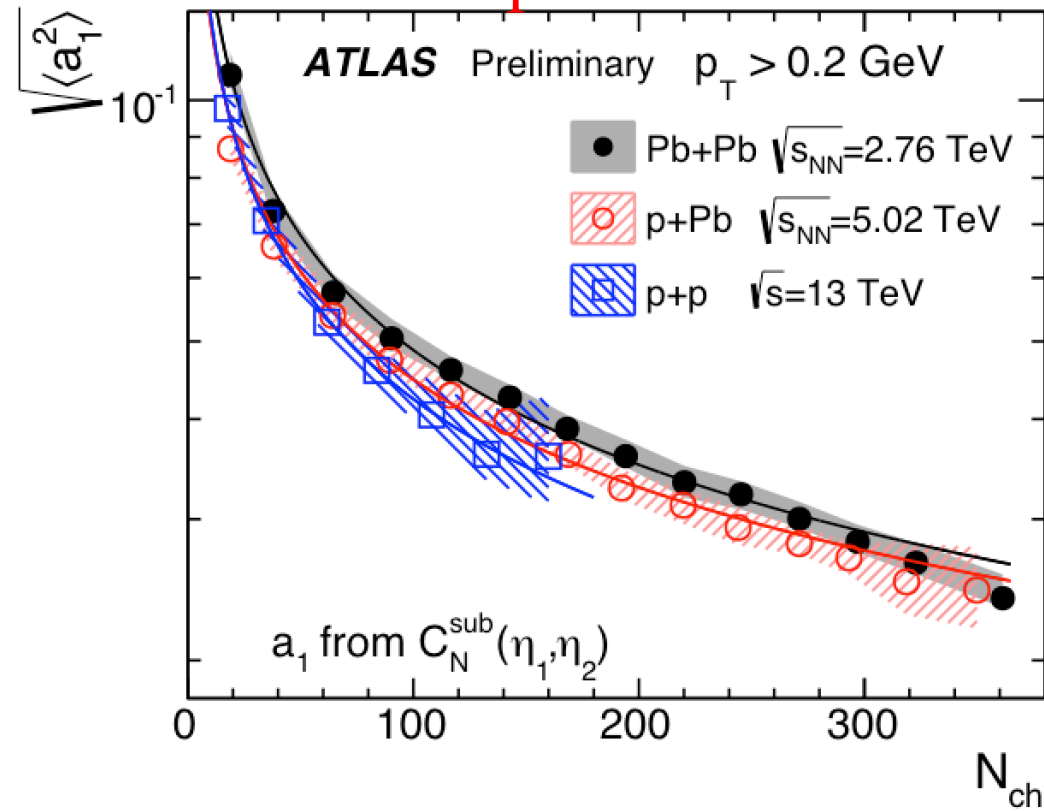
wounded nucleons, or partons (via frag.), flux tubes, or final state resonance decays

# $N_{ch}$ dep. of SRC and $a_1$ in three systems

## SRC



## $a_1$ for LRC



- They follow power-law function Fit with  $c/N_{ch}^\alpha$

	Pb+Pb	p+Pb	pp
$\alpha$ for $\sqrt{\Delta_{SRC}}$	<u><math>0.502 \pm 0.022</math></u>	<u><math>0.451 \pm 0.020</math></u>	<u><math>0.342 \pm 0.030</math></u>
$\alpha$ for $\sqrt{\langle a_1^2 \rangle}$	$0.467 \pm 0.011$	$0.448 \pm 0.019$	$0.489 \pm 0.032$

$\alpha$  smaller in pp  $\rightarrow$  num. of cluster is smaller or cluster size is larger at same  $N_{ch}$ ?

# Summary

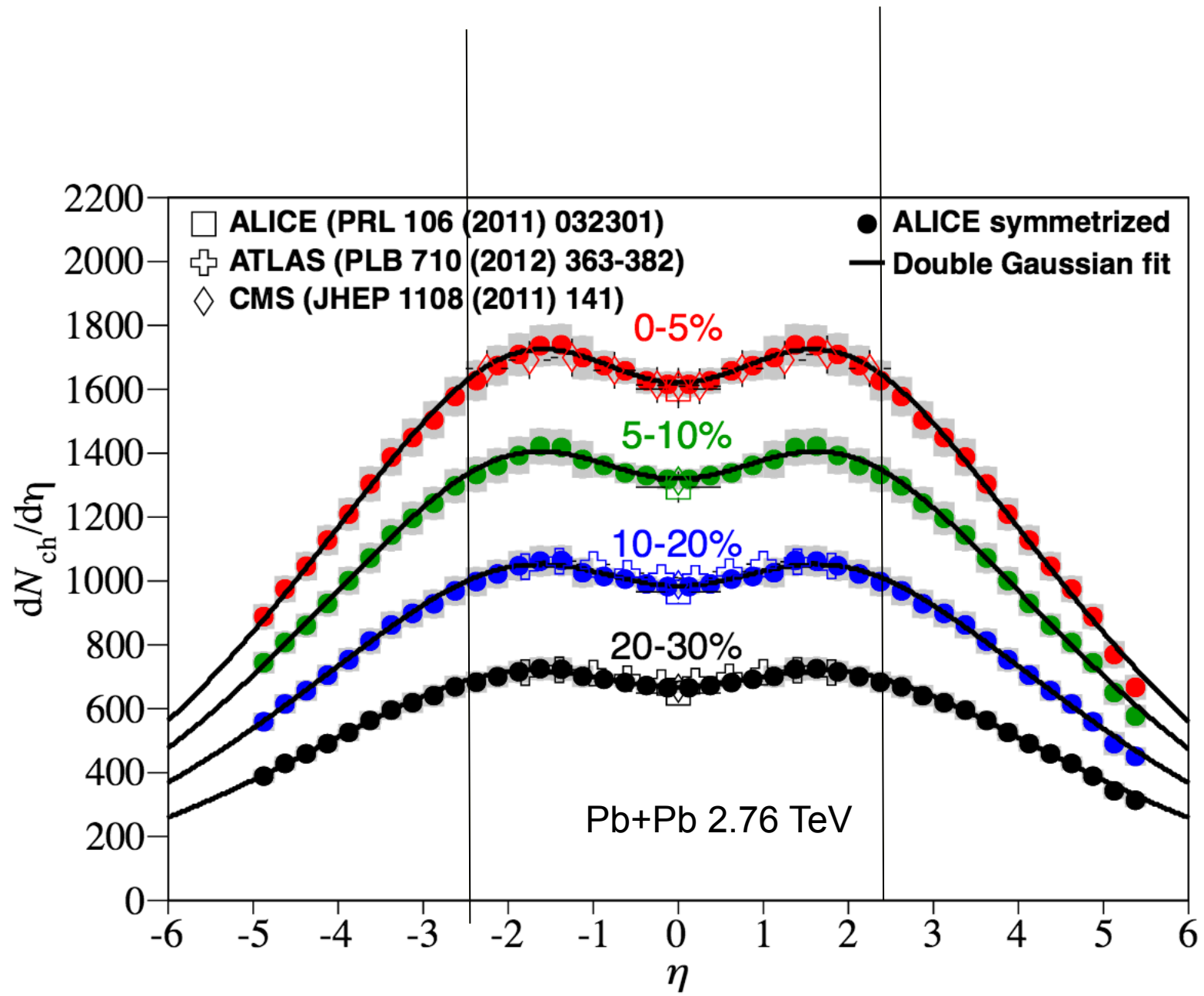
- Two-particle correlation  $C_N(\eta_1, \eta_2)$  measured in PbPb, pPb and pp collisions for  $p_T > 0.2$  GeV and  $|\eta| < 2.4$  at similar event multiplicity  $N_{ch}$ .
  - Sum of a short-range component (SRC) + a long-range component (LRC).
- Data-driven method to separate SRC and LRC based on the fact that SRC differs between +- and  $\pm\pm$  pairs, but not for LRC
  - LRC is symmetric in all systems, but in pPb SRC is asymmetric for  $\eta$  and  $-\eta$ .
  - LRC consistent with  $1 + \langle a^2_1 \rangle \eta_1 \eta_2$ ,  $\langle a^2_1 \rangle$  is extracted via Legendre expansion as well as from the projections of the LRC in limited  $\eta_1, \eta_2$  phase space
- $N_{ch}$ -scaling of LRC (via  $a_1$ ) and SRC are studied
  - LRC (via  $a_1$ ) controlled by  $N_{ch}$ , not by collision systems or charge combination
  - SRC depends strongly on collision system and charge combination
  - $N_{ch}$  dependence of LRC and SRC follows power-law with an index close to 0.5  
 → relation to the number of sources for particle production?

Important inputs for 3+1D hydrodynamic models **W/O** boost invariance  
 Insights on particle production, longitudinal transport, final-state effects

See works by Bzdak, Bozek, Broniowski 1509.02967, 1509.04124; , Akihiko, Schenke 1509.04103

END

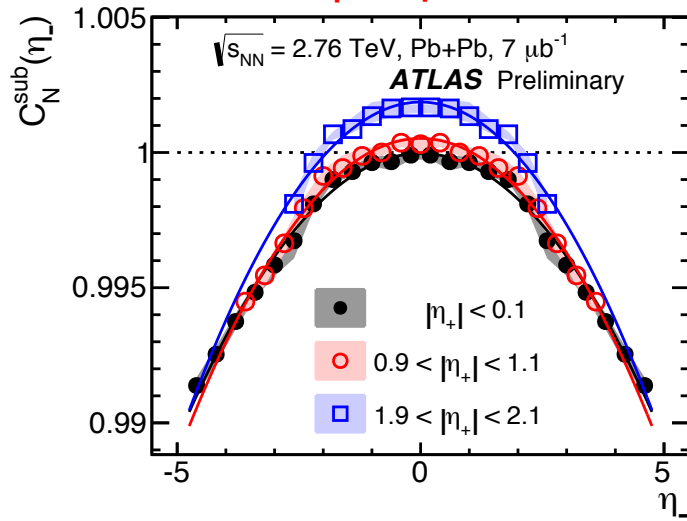
# ALICE $dN/d\eta$ distribution



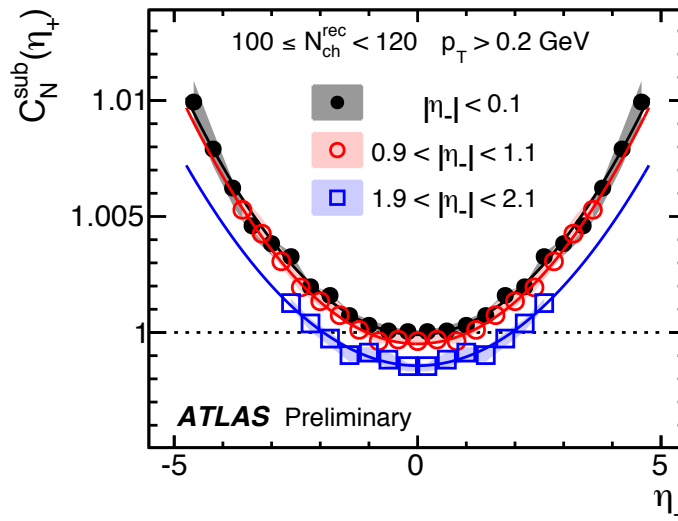
# Projections of CF in Pb+Pb

$$C_N^{\text{sub}}(\eta_1, \eta_2) \approx 1 + \langle a_1^2 \rangle \eta_1 \eta_2 = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2) \quad r_N^{\text{sub}}(\eta, \eta_{\text{ref}}) = 1 - 2 \langle a_1^2 \rangle |\eta_{\text{ref}}| \eta$$

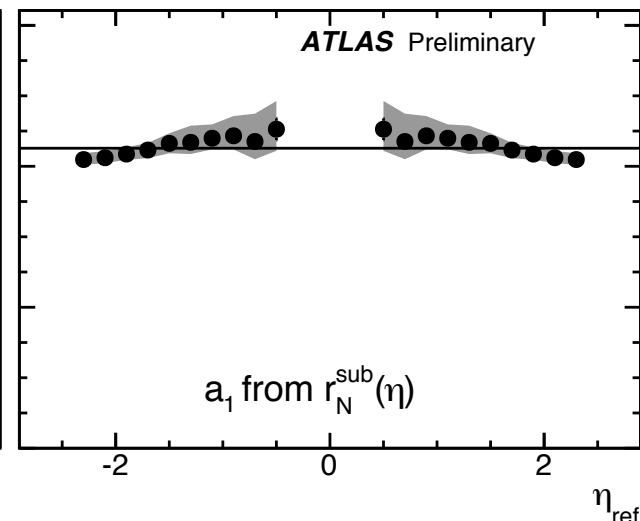
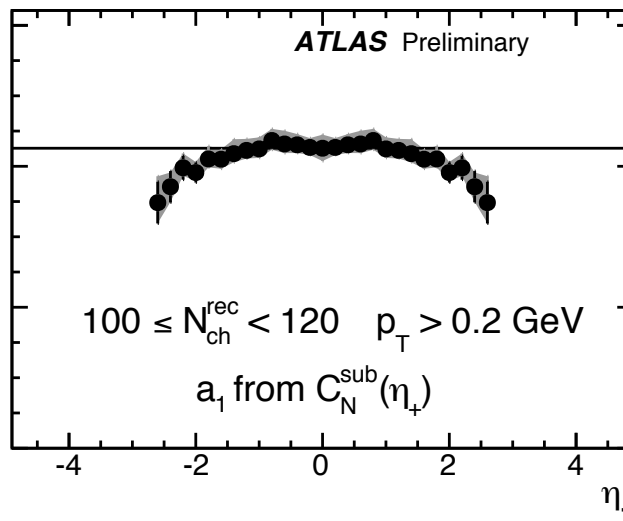
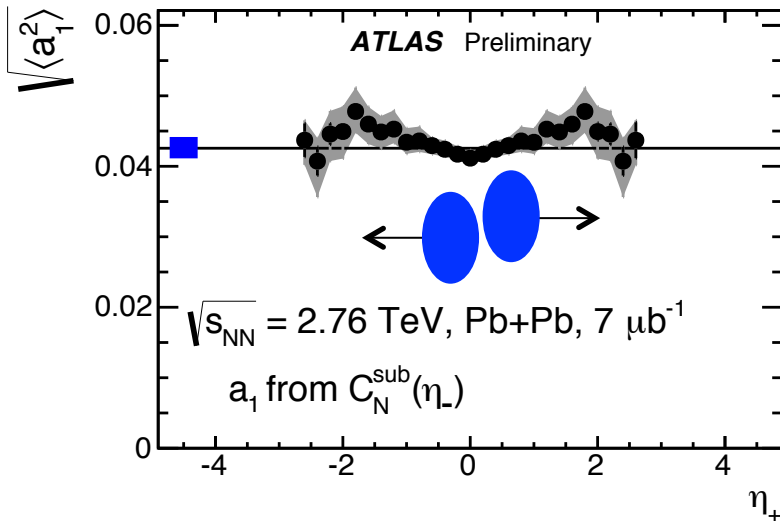
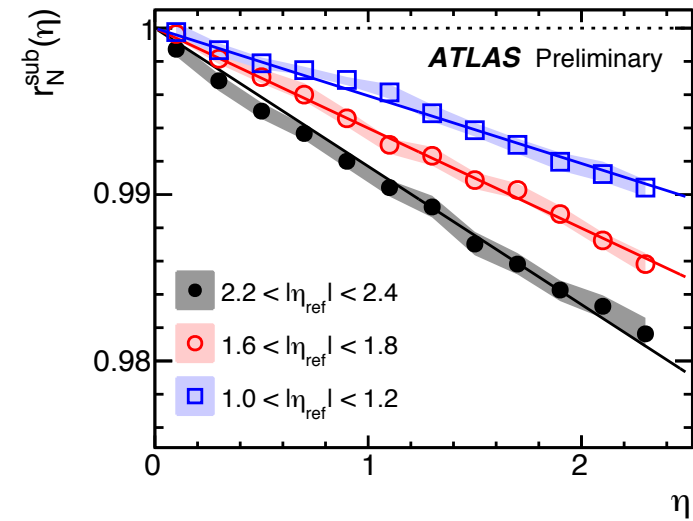
Fit  $\eta_-$  dependence



Fit  $\eta_+$  dependence



Fit  $\eta$  dependence



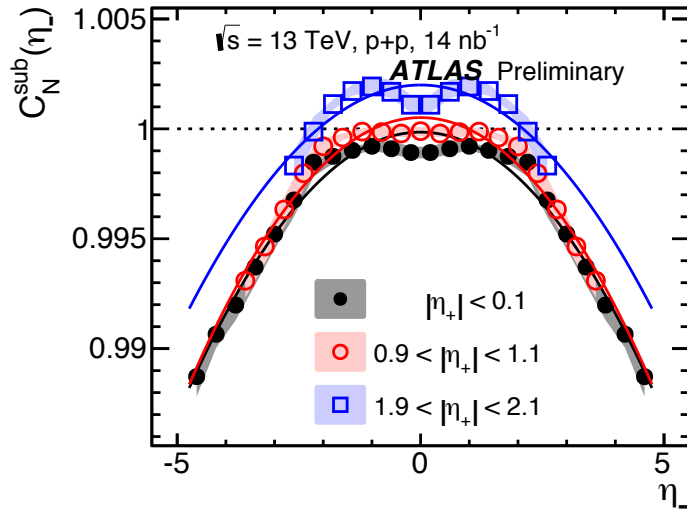
- Consistent  $a_1$  at different slices  $\rightarrow$  LRC dominated by  $a_1$ .

Consistent between four methods

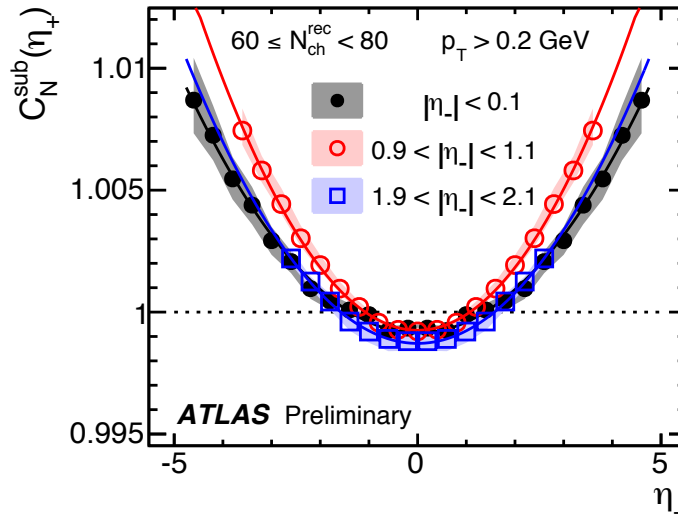
# Projections of CF in p+p

$$C_N^{\text{sub}}(\eta_1, \eta_2) \approx 1 + \langle a_1^2 \rangle \eta_1 \eta_2 = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2) \quad r_N^{\text{sub}}(\eta, \eta_{\text{ref}}) = 1 - 2 \langle a_1^2 \rangle |\eta_{\text{ref}}| \eta$$

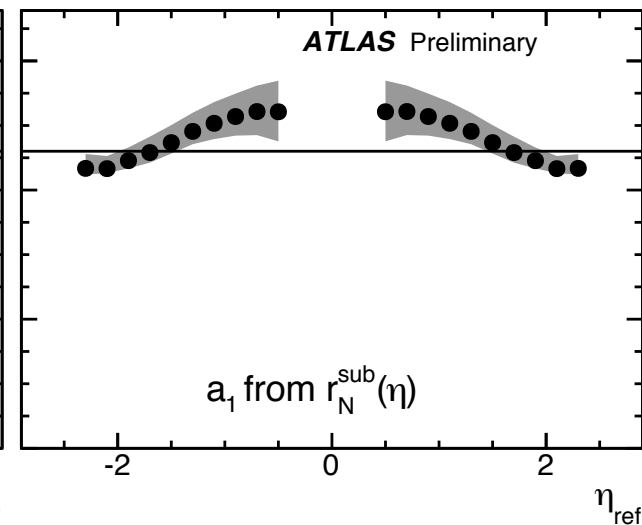
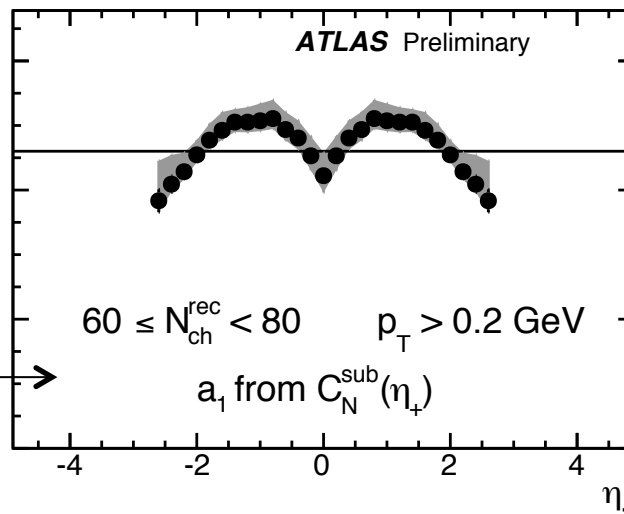
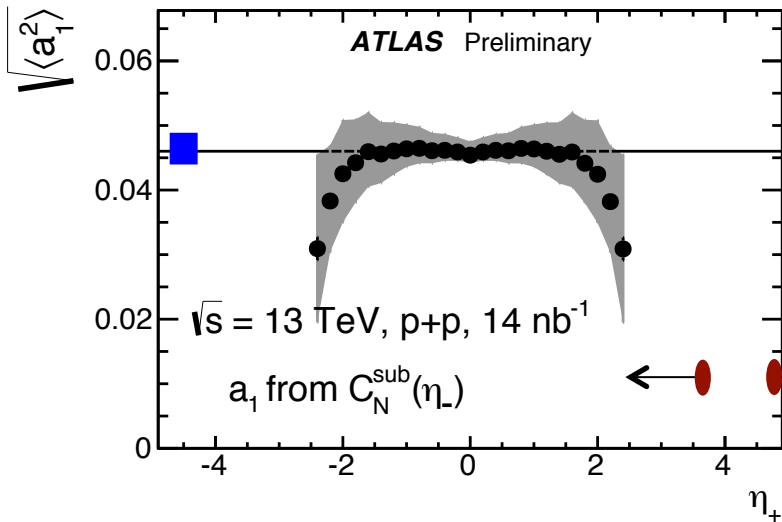
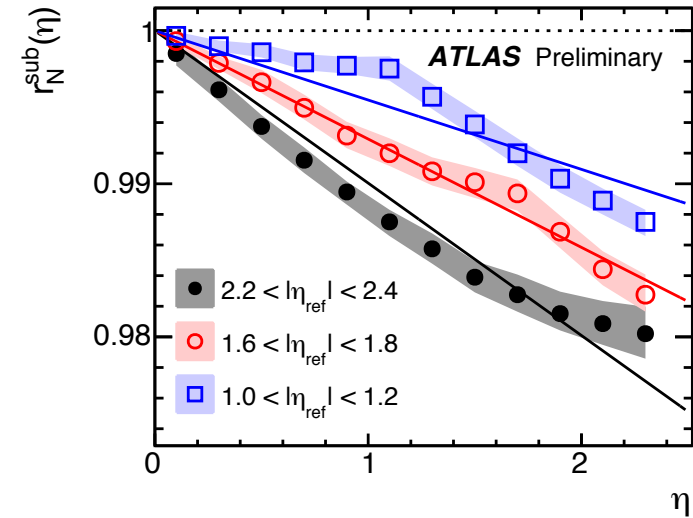
Fit  $\eta_-$  dependence



Fit  $\eta_+$  dependence



Fit  $\eta$  dependence



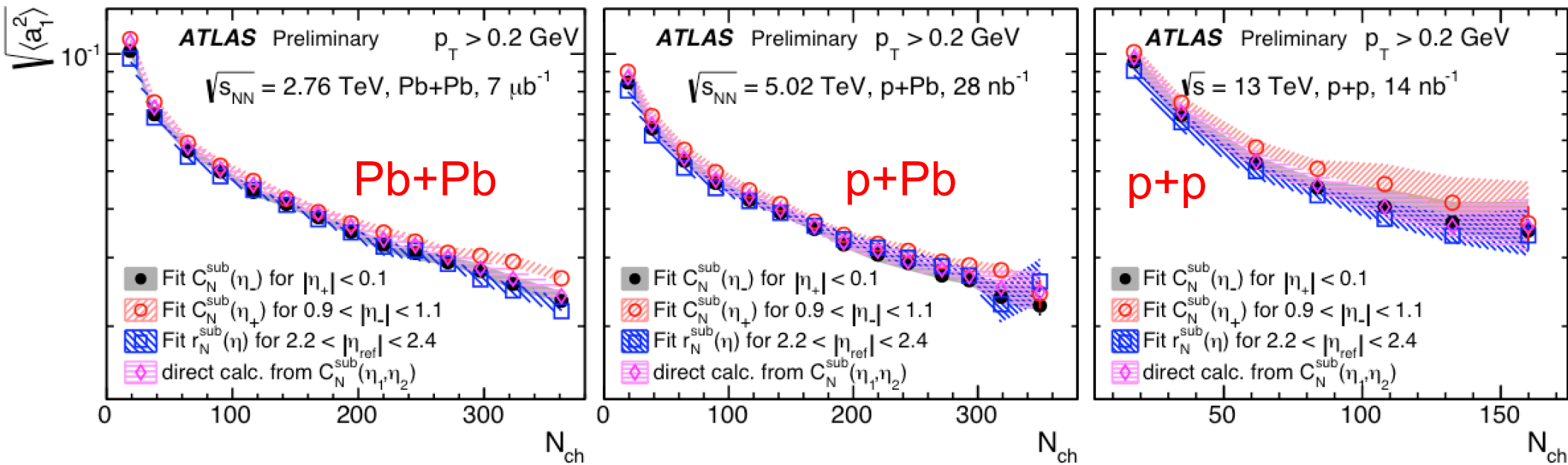
- Consistent  $a_1$  at different slices  $\rightarrow$  LRC dominated by  $a_1$ .

Consistent between four methods



# $a_1$ from four methods

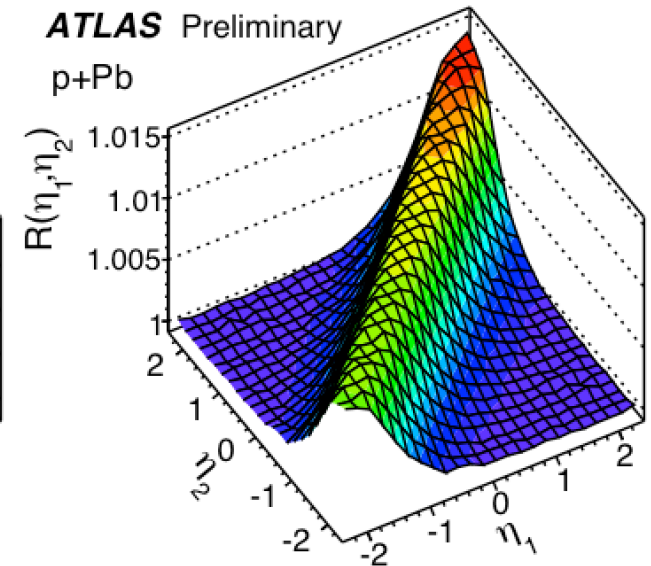
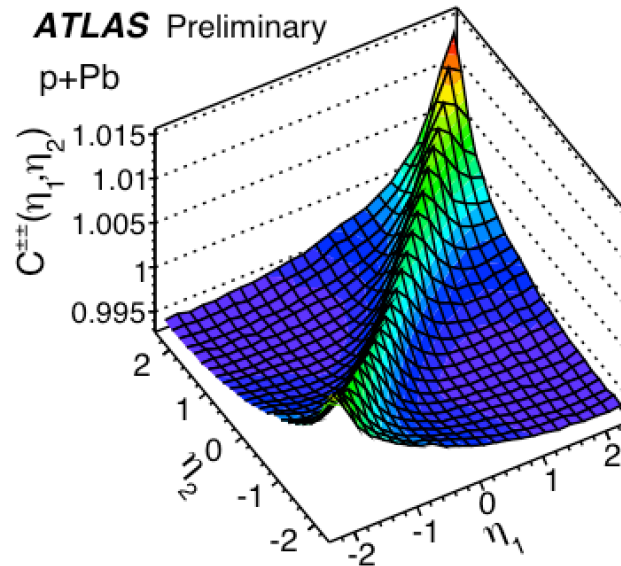
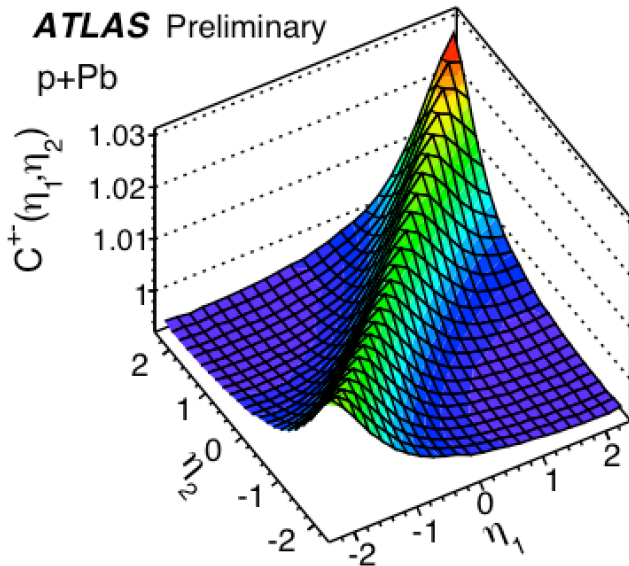
- (i) Quadratic fit to  $\eta_-$  direction,  $C_N^{\text{sub}}(\eta_-)|_{|\eta_+|<0.1}$
- (ii) Quadratic fit to  $\eta_+$  direction,  $C_N^{\text{sub}}(\eta_+)|_{0.9<|\eta_-|<1.1}$
- (iii) Linear fit to r correlator,  $r_N^{\text{sub}}(\eta)|_{2.2<|\eta_{\text{ref}}|<2.4}$
- (iv) Legendre expansion



4 methods consistent with each other in all three collision systems

# Properties of SRC in p+Pb

- Most of the FB asymmetry is in the magnitude of the SRC.
- $\eta_-$ -width of SRC is constant as a function of  $\eta_+$ .

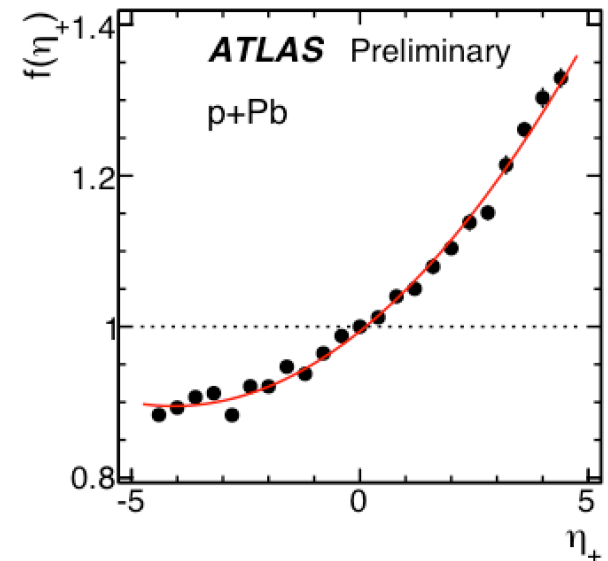
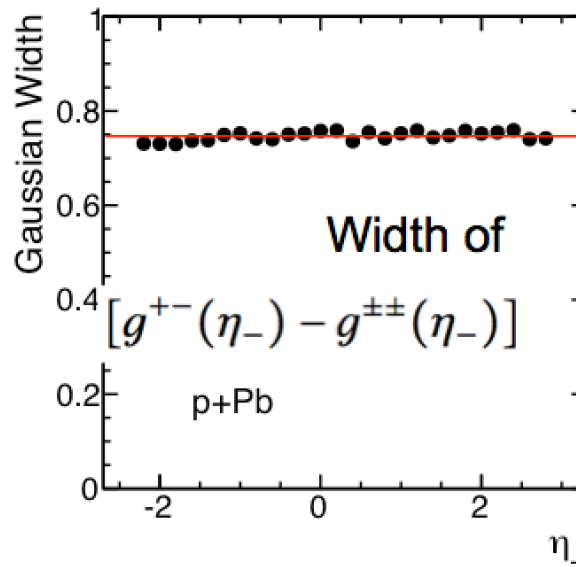


**ATLAS Preliminary**

$$200 \leq N_{\text{ch}}^{\text{rec}} < 220$$

$$\sqrt{s_{\text{NN}}} = 5.02 \text{ TeV, p+Pb, } 28 \text{ nb}^{-1}$$

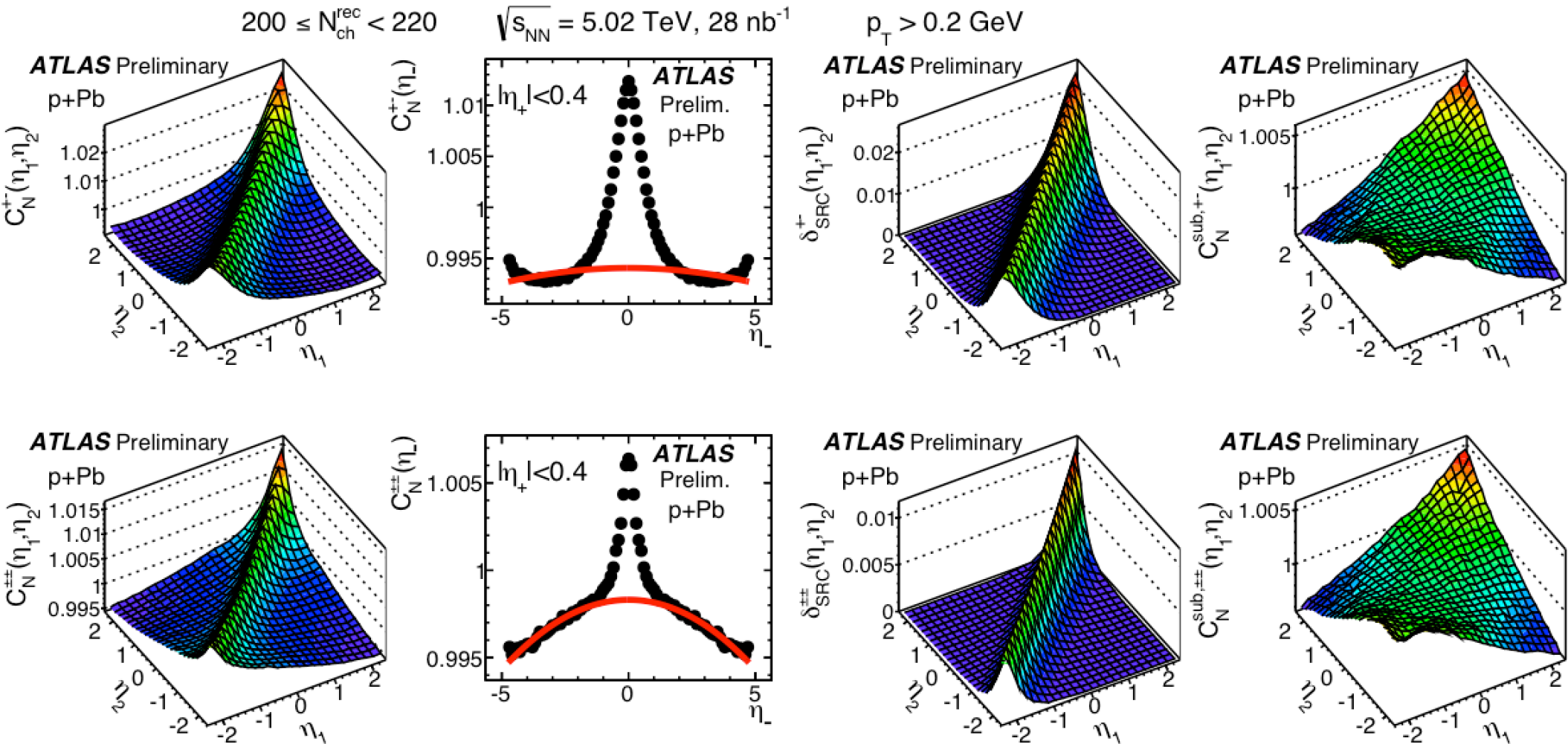
$$p_{\text{T}} > 0.2 \text{ GeV}$$



# Estimation of the SRC in pPb

$$R(\eta_+, \eta_-) \approx 1 + f(\eta_+) [g^{+-}(\eta_-) - g^{\pm\pm}(\eta_-)] , \quad \delta_{\text{SRC}}^{+-} = f(\eta_+)g^{+-}(\eta_-), \quad \delta_{\text{SRC}}^{\pm\pm} = f(\eta_+)g^{\pm\pm}(\eta_-)$$

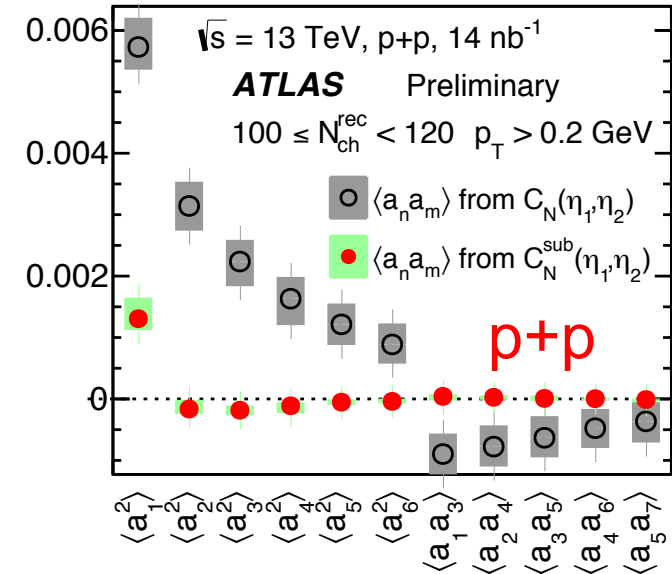
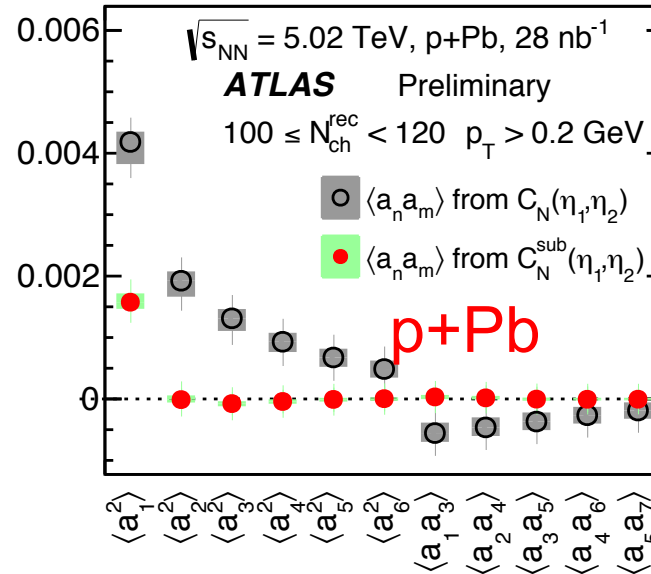
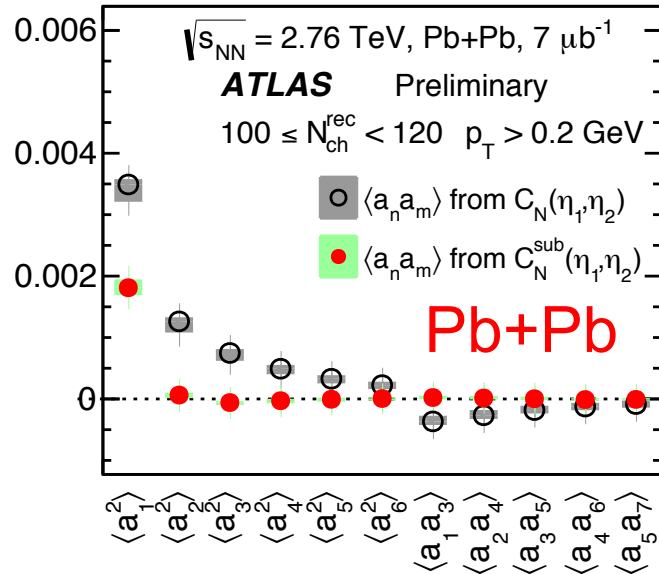
- Asymmetry between proton-going and lead-going direc is due to SRC
- LRC is very symmetric



- The LRC,  $C_N^{\text{sub}}(\eta_+, \eta_-)$ , has similar magnitude between charge combinations.

# Legendre spectra before and after subtraction

$$C_N(\eta_1, \eta_2) \text{ or } C_N^{\text{sub}}(\eta_1, \eta_2) = 1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}$$



- $a_n$  values significantly reduced after SRC subtraction
  - Dominated by  $a_1$ .

# Constructing correlation function

## ■ Signal and Background distributions

- Tracks from events with similar  $N_{\text{ch}}$  and  $z_{\text{vtx}}$

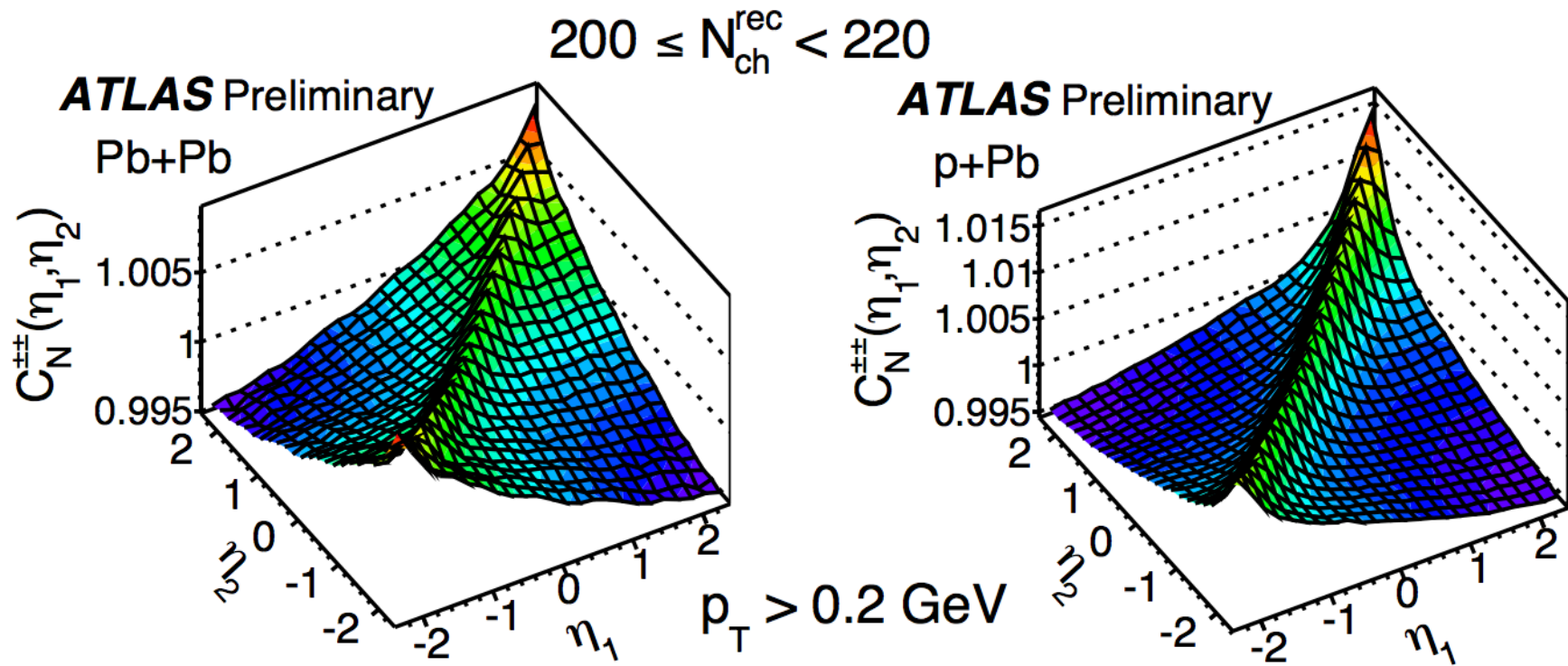
$$C = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} = \frac{S(\eta_1, \eta_2)}{B(\eta_1, \eta_2)}$$

## ■ Due to symmetry in PbPb or pp, only one quadrant is independent.

- $\eta_- = \eta_1 - \eta_2 > 0, \eta_+ = \eta_1 + \eta_2 > 0$   $C_N(\eta_1, \eta_2) = C_N(\eta_2, \eta_1)$   $C_N(\eta_1, \eta_2) = C_N(-\eta_1, -\eta_2)$

## ■ In pPb collision, only one half is independent

- $\eta_- = \eta_1 - \eta_2 > 0$   $C_N(\eta_1, \eta_2) = C_N(\eta_2, \eta_1)$
- But distribution can be symmetrized in any case to compare PbPb and pp



# Summary of systematics

- Evaluate based on ratios of correlation function

$$d(\eta_1, \eta_2) = \frac{C(\eta_1, \eta_2)_{\text{check}}}{C(\eta_1, \eta_2)_{\text{default}}} \quad \delta_{\text{sys}} C = \sqrt{\sum_k (d_k - 1)^2} \quad \delta_{\text{sys}} a_n = \sqrt{\sum_k ((a_n)_k - 1)^2}$$

- Separately for  $C_N(\eta_1, \eta_2)$  &  $C_N^{\text{sub}}(\eta_1, \eta_2)$
- Uncertainty propagate to the  $a_1$  calculated from four methods

## Correlation function

Collision system	Pb+Pb	p+Pb	pp
Event-mixing [%]	0.4–0.7	0.4–2.2	0.2–1.4
Run-by-run stability [%]	0.3–0.5	0.3–1.5	0.2–1.5
$z_{\text{vtx}}$ variation [%]	0.3–0.6	0.3–1.5	0.2–1.6
Track selection & efficiency [%]	0.6–1.2	0.2–1.3	0.3–0.7
MC consistency [%]	0.2–1.6	0.5–2.5	0.7–3.3
Charge dependence [%]	1.0–1.8	0.8–3.8	1.5–2.5
SRC subtraction [%]	1.1–2.1	1.0–5.9	1.2–5.0
Total [%]	1.7–3.2	2.1–7.6	2.5–6.9

## $a_1$ from the four methods

Collision system	quadratic fit to the $C_N^{\text{sub}}(\eta_-) _{ \eta_+ <0.1}$			quadratic fit to the $C_N^{\text{sub}}(\eta_+) _{0.9< \eta_- <1.1}$		
	Pb+Pb	p+Pb	pp	Pb+Pb	p+Pb	pp
Event-mixing [%]	0.5–2.2	0.3–1.8	0.2–2.8	0.2–1.7	0.2–1.6	0.2–2.7
Run-by-run stability [%]	0.2–1.3	0.2–1.7	0.2–2.8	0.2–1.5	0.2–1.1	0.2–1.6
$z_{\text{vtx}}$ variation [%]	0.3–1.9	0.1–2.2	0.1–1.6	0.1–1.8	0.2–0.7	0.1–0.9
Track selec.& efficiency[%]	0.4–2.1	0.3–0.9	0.8–2.2	0.8–3.7	1.0	0.9–1.2
MC consistency [%]	0.2–3.6	0.4–3.9	0.2–10.0	0.2–4.3	0.2–2.4	0.2–4.7
Charge dependence [%]	0.9–4.2	1.0–10.2	2.8–4.6	0.4–3.8	0.6–3.1	1.2–6.2
SRC subtraction [%]	0.9–2.5	1.2–6.3	1.3–4.8	1.4–2.5	1.2–3.7	1.2–4.6
Total [%]	2.1–5.2	2.7–10.3	10–12	2.4–5.5	2.5–6.8	3.5–11.2
Collision system	linear fit to the $r_N^{\text{sub}}(\eta) _{2.2< \eta_{\text{ref}} <2.4}$			Global Legendre expansion of $C_N^{\text{sub}}$		
	Pb+Pb	p+Pb	pp	Pb+Pb	p+Pb	pp
Event-mixing [%]	0.3–2.3	0.3–1.4	0.1–1.5	0.2–1.8	0.1–1.7	0.1–0.9
Run-by-run stability [%]	0.1–1.2	0.1–1.7	0.2–2.8	0.2–0.7	0.1–1.3	0.1–2.1
$z_{\text{vtx}}$ variation [%]	0.2–1.2	0.2–2.1	0.2–2.6	0.1–1.3	0.2–2.5	0.2–1.7
Track selec.& efficiency[%]	0.4–1.3	0.6–0.9	0.7–1.7	0.3–0.9	0.4–0.7	0.8–2.4
MC consistency [%]	0.2–2.6	0.2–3.7	0.8–7.6	0.2–2.5	0.4–3.2	0.1–6.7
Charge dependence [%]	0.4–4.9	0.1–8.8	1.6–5.3	2.3–5.3	1.0–12.7	3.4–8.1
SRC subtraction [%]	1.4–3.2	2.2–3.4	1.7–5.0	1.7–4.3	2.0–8.9	2.7–9.6
Total [%]	2.4–6.2	2.9–8.9	4.4–9.8	3.4–6.4	4.1–12.9	6.2–12.5