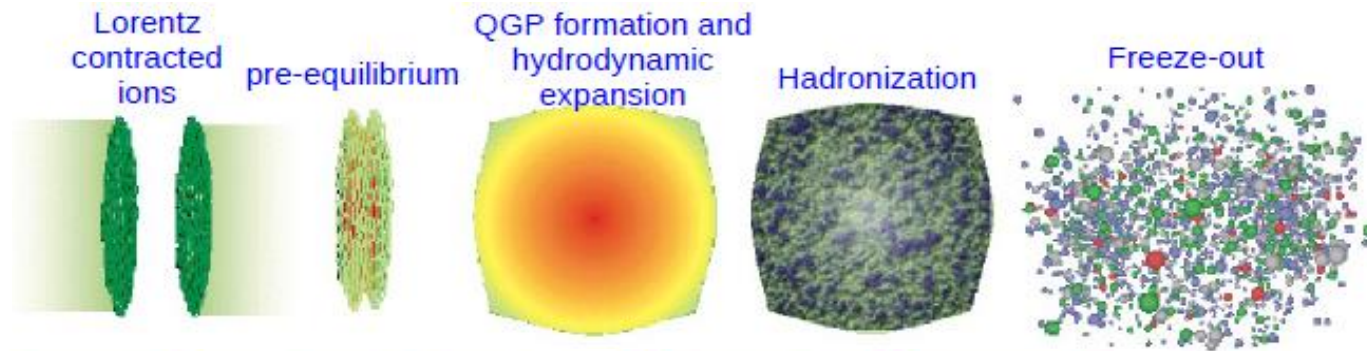


Anatomy of particle production and azimuthal anisotropy in small and large systems

Roy A. Lacey
Stony Brook University

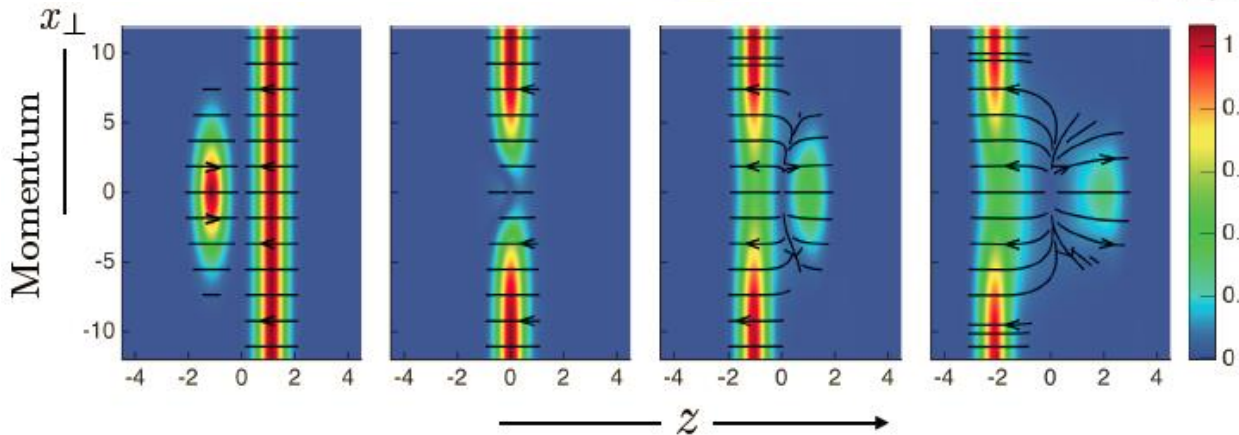
Backdrop

A+A
collision

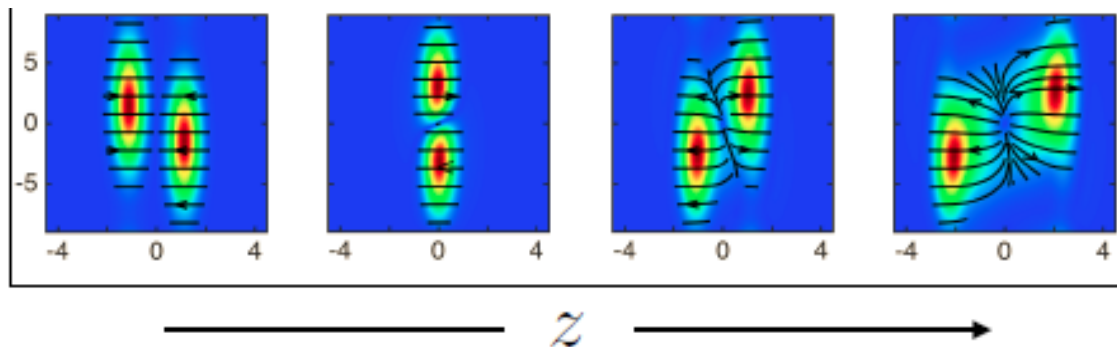


S. Bass

p+A
collision



p+p
collision

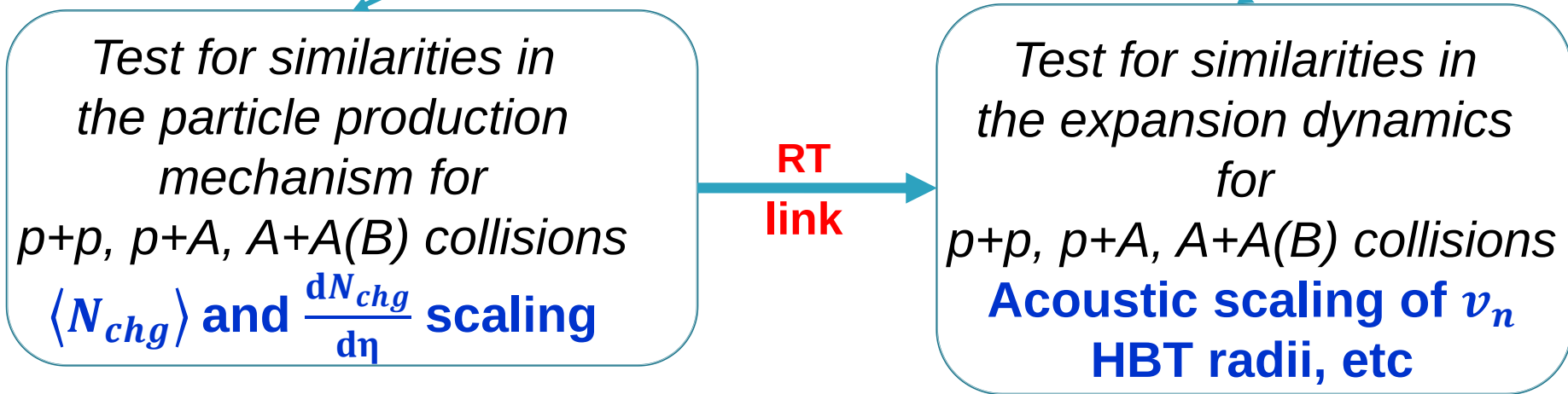


P. Chesler
Hydrodynamic
expansion
dynamics for
sizes as small
as $RT \sim 1$

Essential question

➤ Whether hydro-like expansion dynamics is maintained with reduced system size, and how do we tell?

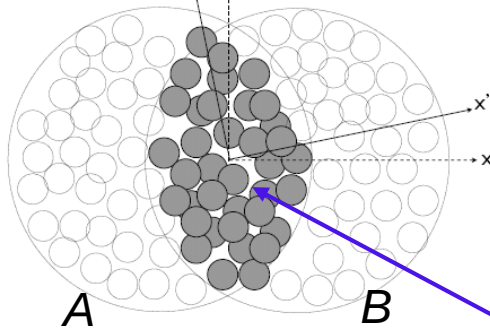
Strategy



The scaling properties of $\langle N_{chg} \rangle$, $\frac{dN_{chg}}{d\eta}$, v_n , etc can provide key insights

✓ Scaling coefficients provide crucial constraints for transport coefficients

Nucleon Glauber



$$\Psi_n^* = \frac{1}{n} \tan^{-1} \left(\frac{S_{ny}}{S_{nx}} \right)$$

$$\varepsilon_n = \langle \cos n(\phi - \psi_n^*) \rangle$$

$$\frac{1}{\bar{R}} = \sqrt{\left(\frac{1}{\sigma_x^2} + \frac{1}{\sigma_y^2} \right)}$$

σ_x & $\sigma_y \rightarrow$ RMS widths of density distribution

Phys. Rev. C 81, 061901(R) (2010)

$$S_{nx} \equiv S_n \cos(n\Psi_n^*) = \int d\mathbf{r}_\perp \rho_s(\mathbf{r}_\perp) \omega(\mathbf{r}_\perp) \cos(n\phi)$$

$$S_{ny} \equiv S_n \sin(n\Psi_n^*) = \int d\mathbf{r}_\perp \rho_s(\mathbf{r}_\perp) \omega(\mathbf{r}_\perp) \sin(n\phi),$$

N_{part}

Quark Glauber

n-n cross section

p-p profile

✓ Elastic scattering measurements

rms radius

➤ **Consistency of approach for nucleon and quark Glauber**

✓ **Geometric fluctuations included**

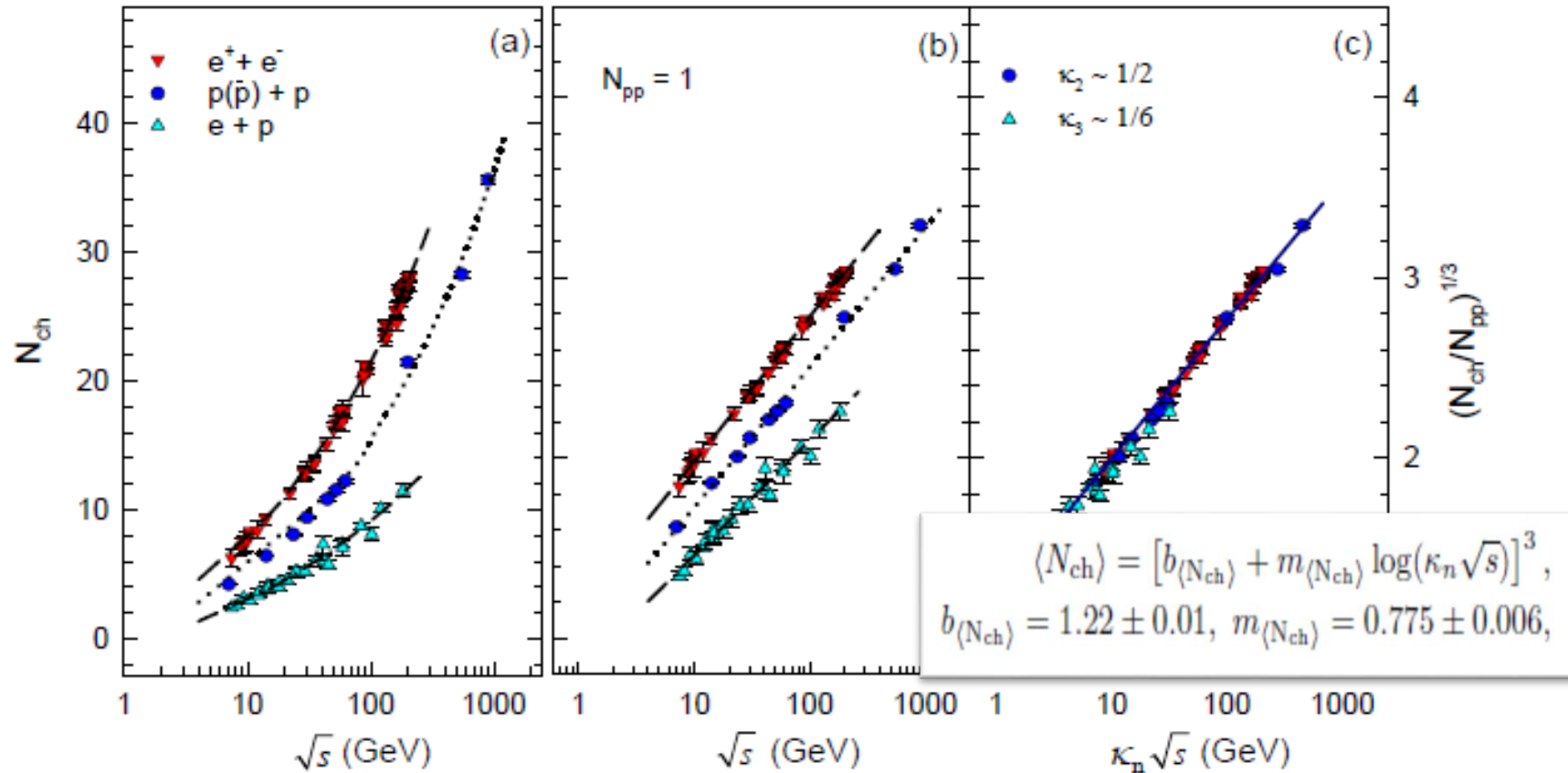
$\langle N_{chg} \rangle$ and $\frac{dN_{chg}}{d\eta}$ scaling

Operational Ansatz

$$S \sim (TR)^3 \sim \text{const.},$$

$$\langle N_{chg} \rangle, \frac{dN_{chg}}{d\eta} \propto S$$

$N_{npp,qpp}^{1/3} \propto R$ for early-time thermalization

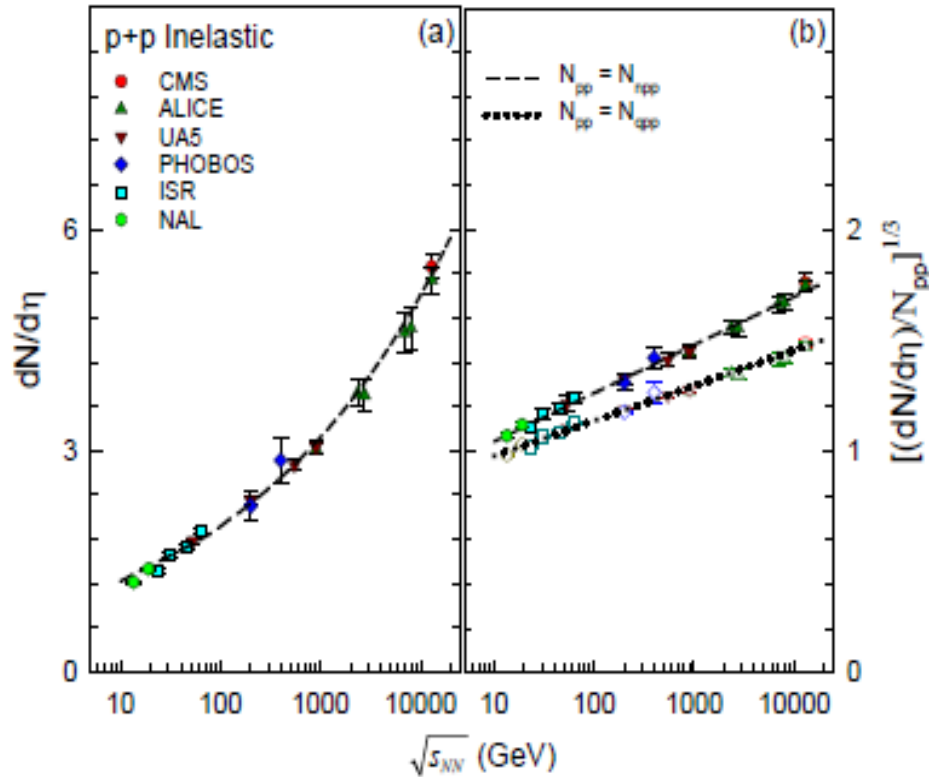


Scaling validates important role of quark participants

- ✓ Large fluctuations – leading particle effect
- ✓ $\kappa_{2,3}$ related to number of quark participants

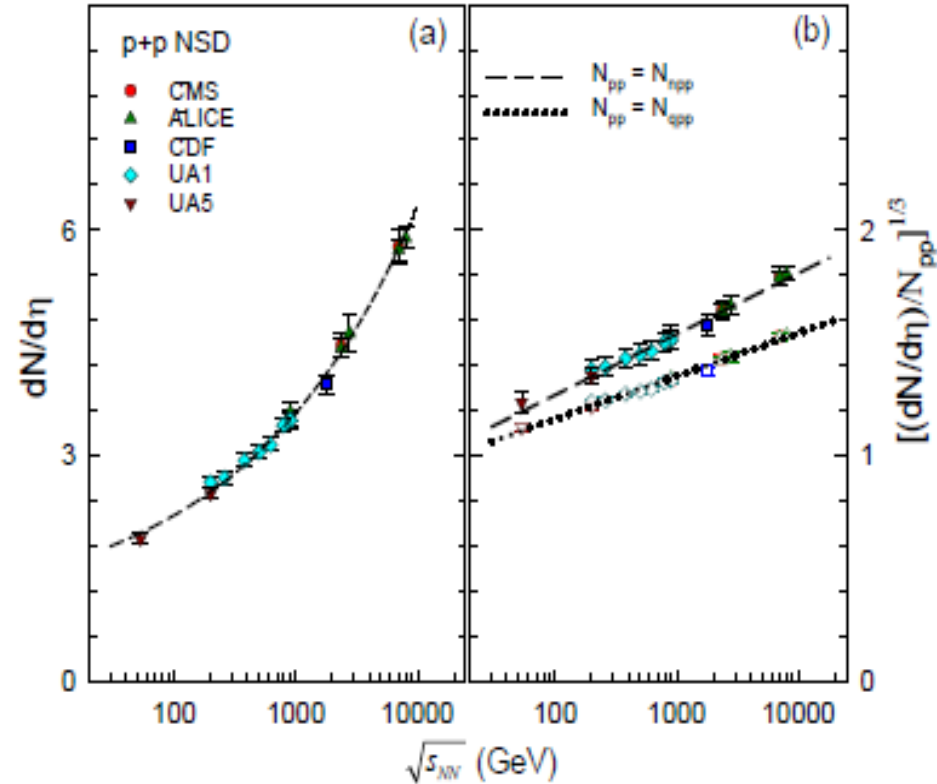
→ fraction of available cm energy

$\frac{dN_{chg}}{d\eta}$ scaling p+p



$$dN_{ch}/d\eta|_{INE} = [b_{INE} + m_{INE} \log(\sqrt{s_{NN}})]^3,$$

$$b_{INE} = 0.826 \pm 0.008, \quad m_{INE} = 0.220 \pm 0.004,$$

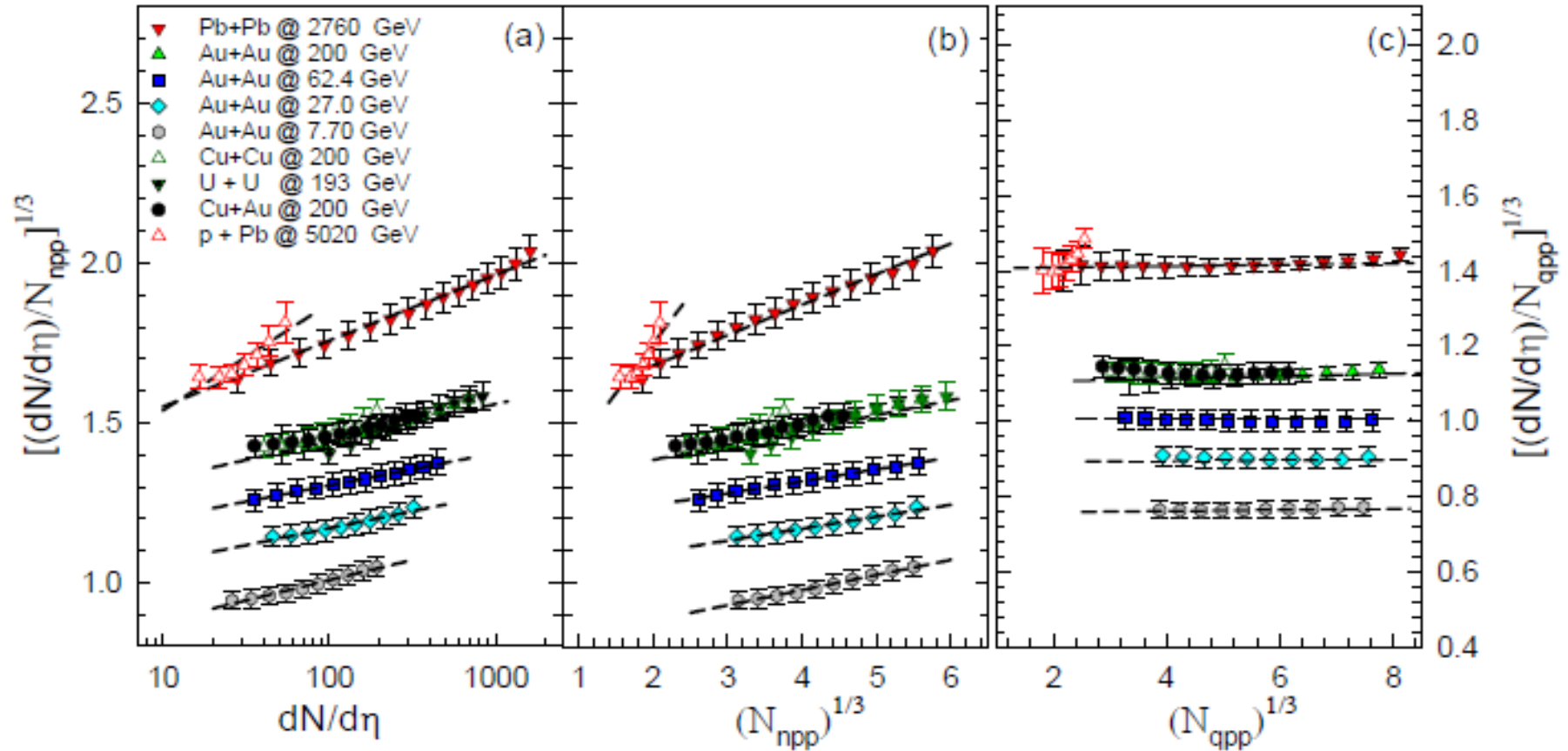


$$dN_{ch}/d\eta|_{NSD} = [b_{NSD} + m_{NSD} \log(\sqrt{s_{NN}})]^3,$$

$$b_{NSD} = 0.747 \pm 0.022, \quad m_{NSD} = 0.267 \pm 0.007,$$

Further scaling validation over full range of $\sqrt{s_{NN}}$ for p+p

- ✓ Similar $\sqrt{s_{NN}}$ trend for quark and nucleon scaled multiplicity density



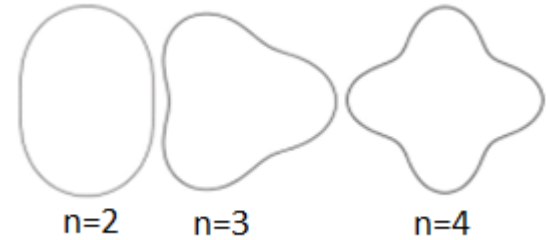
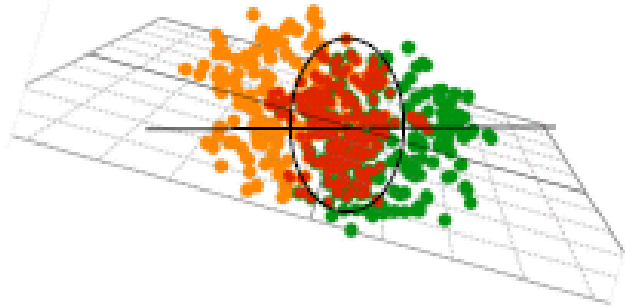
$$dN_{ch}/d\eta|_{|\eta|=0.5} = N_{qpp} [b_{AA} + m_{AA} \log(\sqrt{s})]^3,$$

$$b_{AA} = 0.530 \pm 0.008, \quad m_{AA} = 0.258 \pm 0.004,$$

Scaling validated for p+A & A+A(B) systems

- ✓ Similar patterns for A+A(B) systems at the same $\sqrt{s_{NN}}$.
- ✓ Logarithmic dependence of $\langle p_T \rangle$ on multiplicity

Flow is acoustic



$$\frac{dN}{d\phi} \propto \left(1 + 2 \sum_{n=1} v_n \cos[n(\phi - \Psi_n)] \right)$$

$$k = n / \bar{R}$$

$$t \propto \bar{R}$$

Acoustic viscous modulation of v_n

$$\delta T_{\mu\nu}(t, k) = \exp\left(-\frac{2}{3} \frac{\eta}{s} k^2 \frac{t}{T}\right) \delta T_{\mu\nu}(0)$$

Staig & Shuryak arXiv:1008.3139

Scaling expectations:

$$\delta T_{\mu\nu}(n, t) = \exp(-\beta n^2) \delta T_{\mu\nu}(0), \quad \beta = \frac{2}{3} \frac{\eta}{s} \frac{1}{\bar{R}^2} \frac{t}{T}$$

n^2 dependence

$$\left(\frac{v_n(p_T)}{\varepsilon_n} \right) \propto \exp\left(-\frac{\beta'}{RT} n^2\right)$$

Straightforward to include bulk viscosity

v_n 's are related

$$\frac{(v_n(p_T))^{1/n}}{(v_{n'}(p_T))^{1/n'}} \sim \frac{(\varepsilon_{n'})^{1/n'}}{(\varepsilon_n)^{1/n}} \cdot \exp\left(-\frac{\beta'}{RT} (n - n')\right)$$

System size dependence

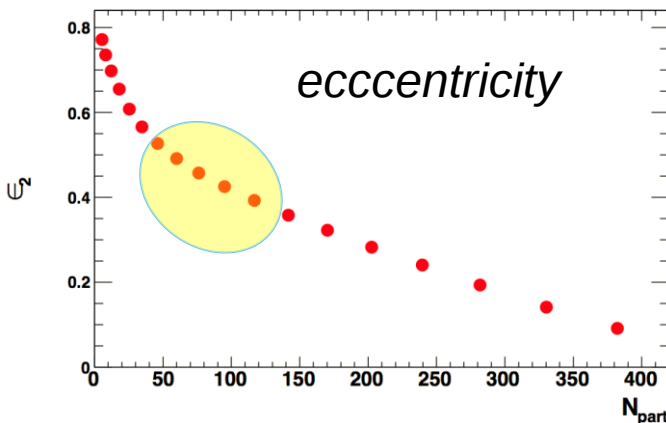
$$\ln\left(\frac{v_n}{\varepsilon_n}\right) \propto \frac{-\beta''}{RT}$$

Each of these scaling expectations has been validated

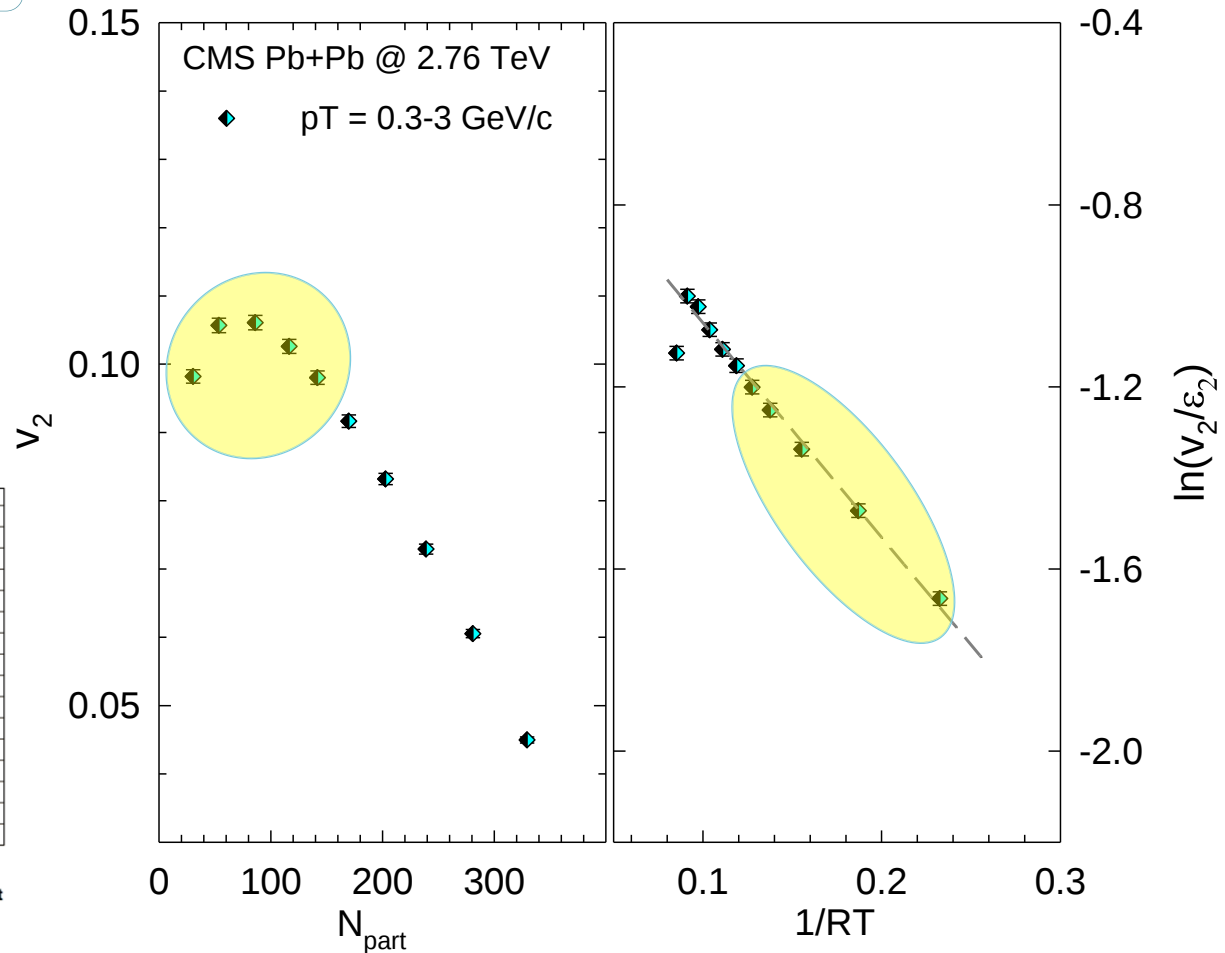
Acoustic Scaling – RT

$$\ln \left(\frac{v_n}{\varepsilon_n} \right) \propto \frac{-\beta''}{RT}$$

$$RT \propto \left(\frac{dN_{chg}}{d\eta} \right)^{1/3}$$

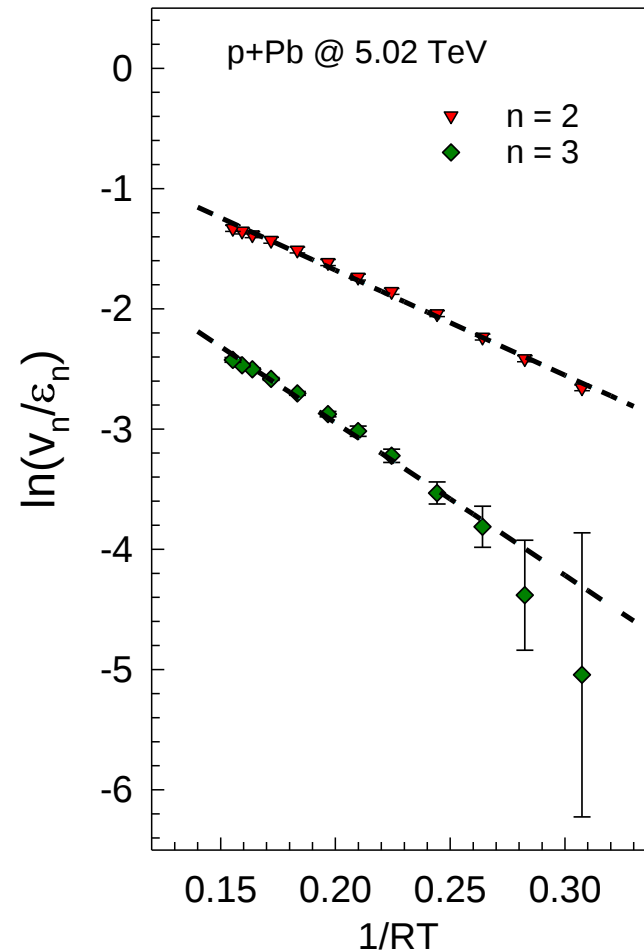


➤ **Eccentricity change
alone is not sufficient**



- ✓ **Characteristic 1/(RT) viscous damping validated**
- ✓ **Similar patterns for other p_T selections**
- ✓ **Important constraint for η/s & ζ/s**

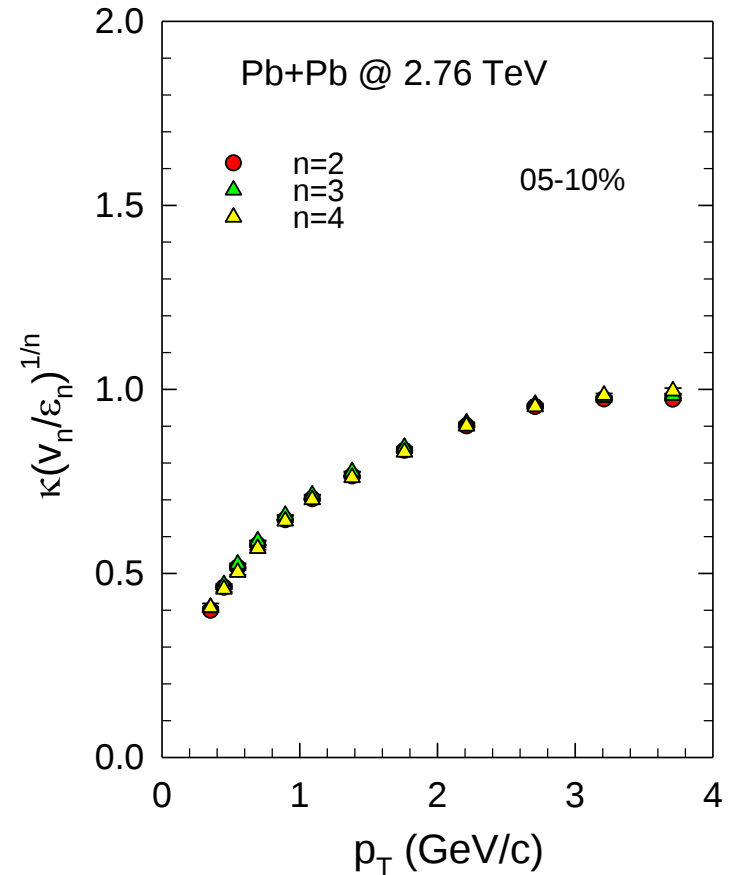
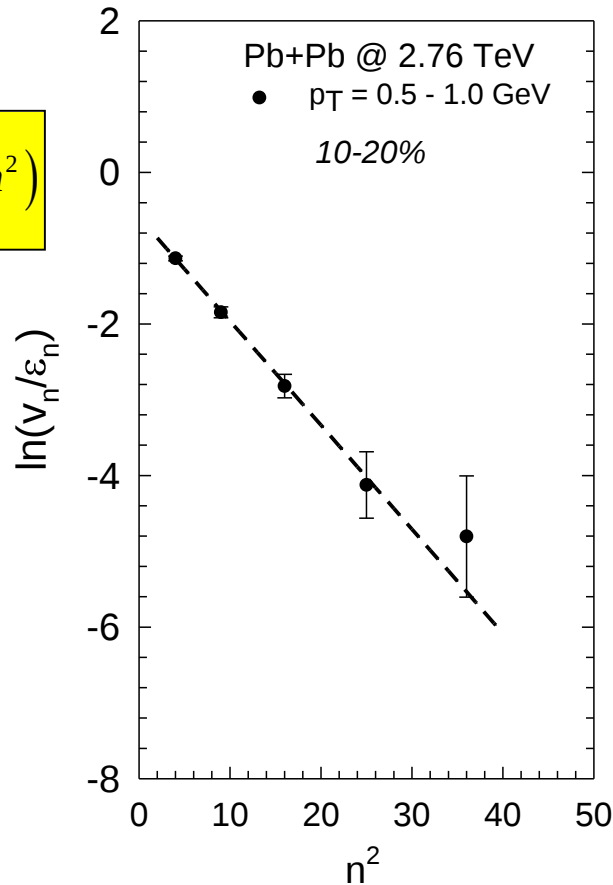
$$\ln\left(\frac{v_n}{\varepsilon_n}\right) \propto \frac{-\beta''}{RT}$$
$$RT \propto \left(\frac{dN_{chg}}{d\eta}\right)^{1/3}$$



- ✓ Characteristic $1/(RT)$ viscous damping validated
- ✓ Important constraint for η/s & ζ/s

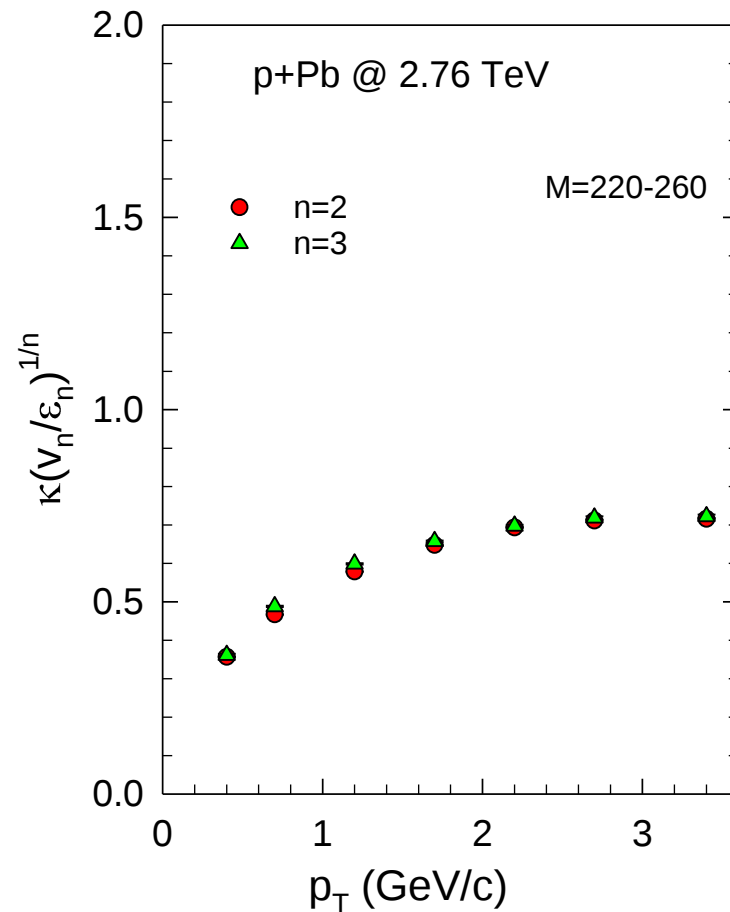
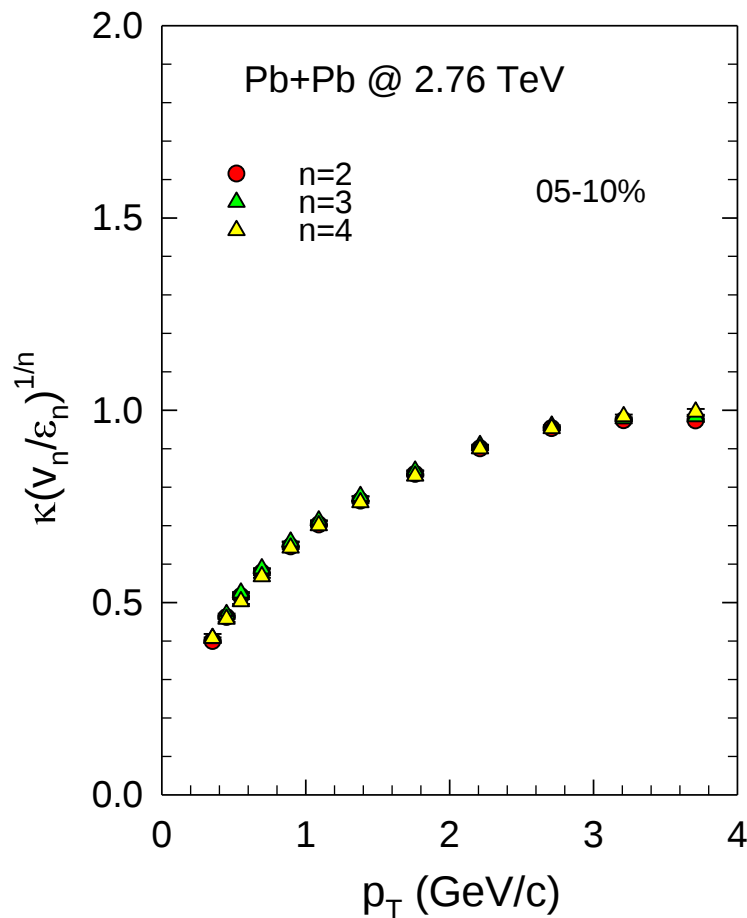
$$\left(\frac{v_n(p_T)}{\varepsilon_n} \right)^{1/n} \propto \exp(-\beta' n)$$

$$\left(\frac{v_n}{\varepsilon_n} \right) \propto \exp(-\beta' n^2)$$



- ✓ Characteristic n^2 viscous damping validated
- ✓ Similar patterns for other centrality selections
- ✓ Important constraint for η/s & ζ/s

System-size dependence

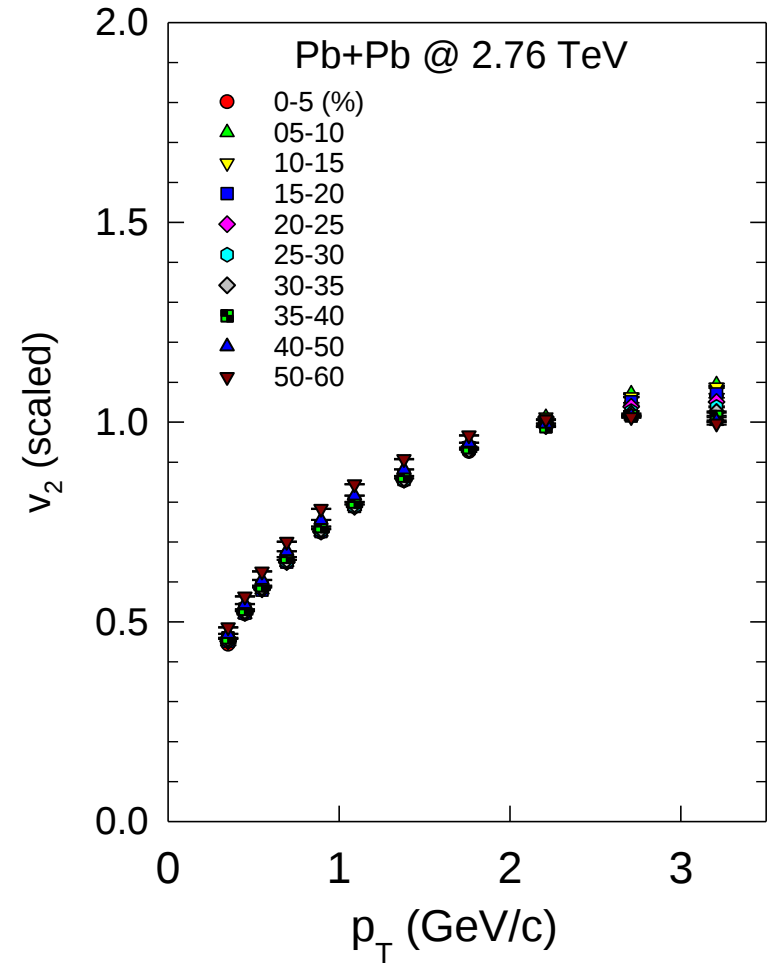


- ✓ **Similar acoustic patterns for p+Pb and Pb+Pb**
- ✓ **Similar results for other small systems**

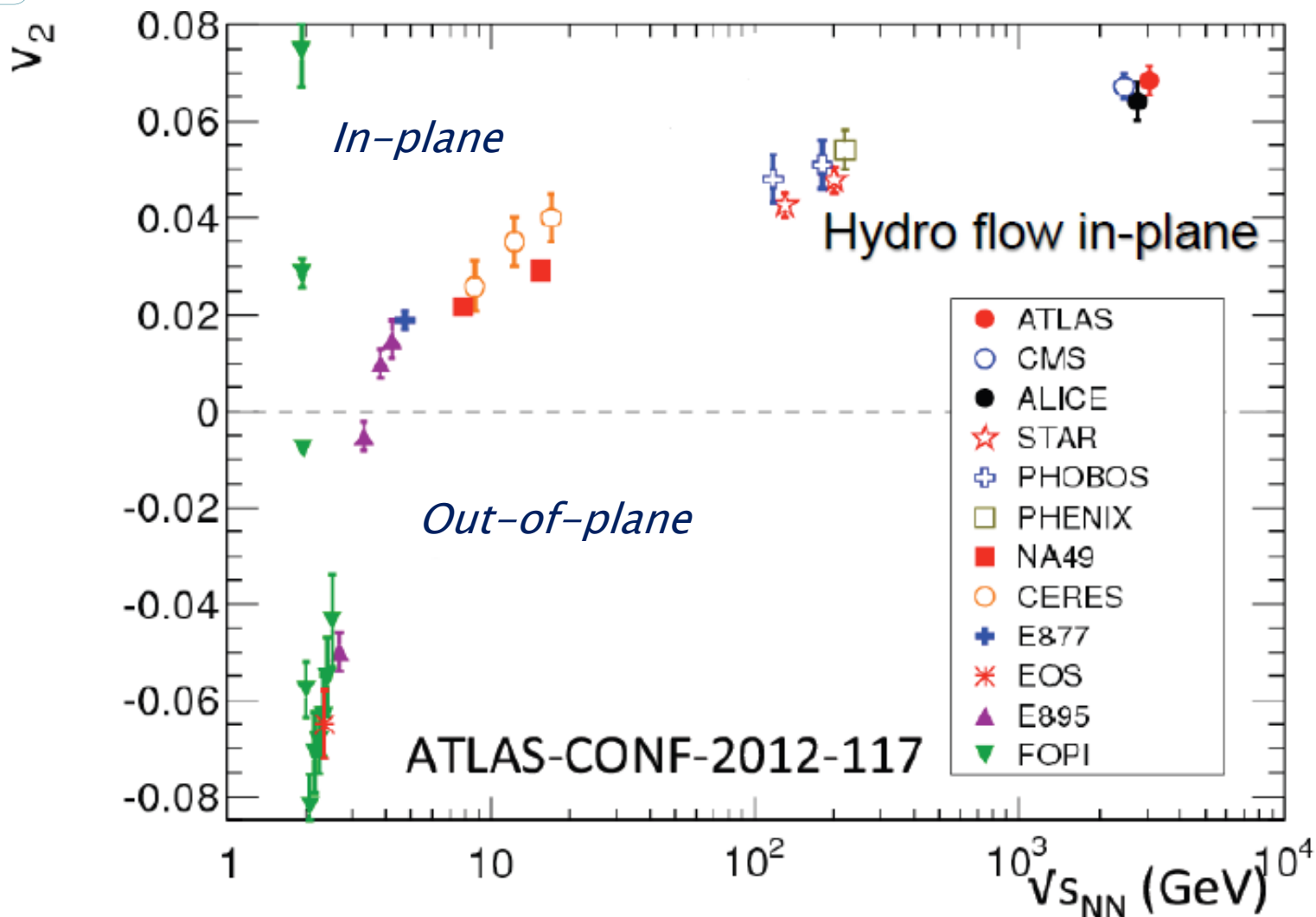
No fundamental change in the particle production mechanism and expansion dynamics, with reduced system size

- ***Similar particle production mechanism for large (A+A(B)) and small (p+p, p+A) system***
 - ✓ ***$\langle N_{chg} \rangle$ and $\frac{dN_{chg}}{d\eta}$ scaling over $\sim$ four orders of magnitude in $\sqrt{s_{NN}}$***
 - ✓ ***Important role for quark participants***
- ***Similar Acoustic dynamics validated in “large” and “small” systems***
 - ✓ ***Strong evidence for the important role of final-state interactions.***
 - ✓ ***Important constraints for transport coefficients***

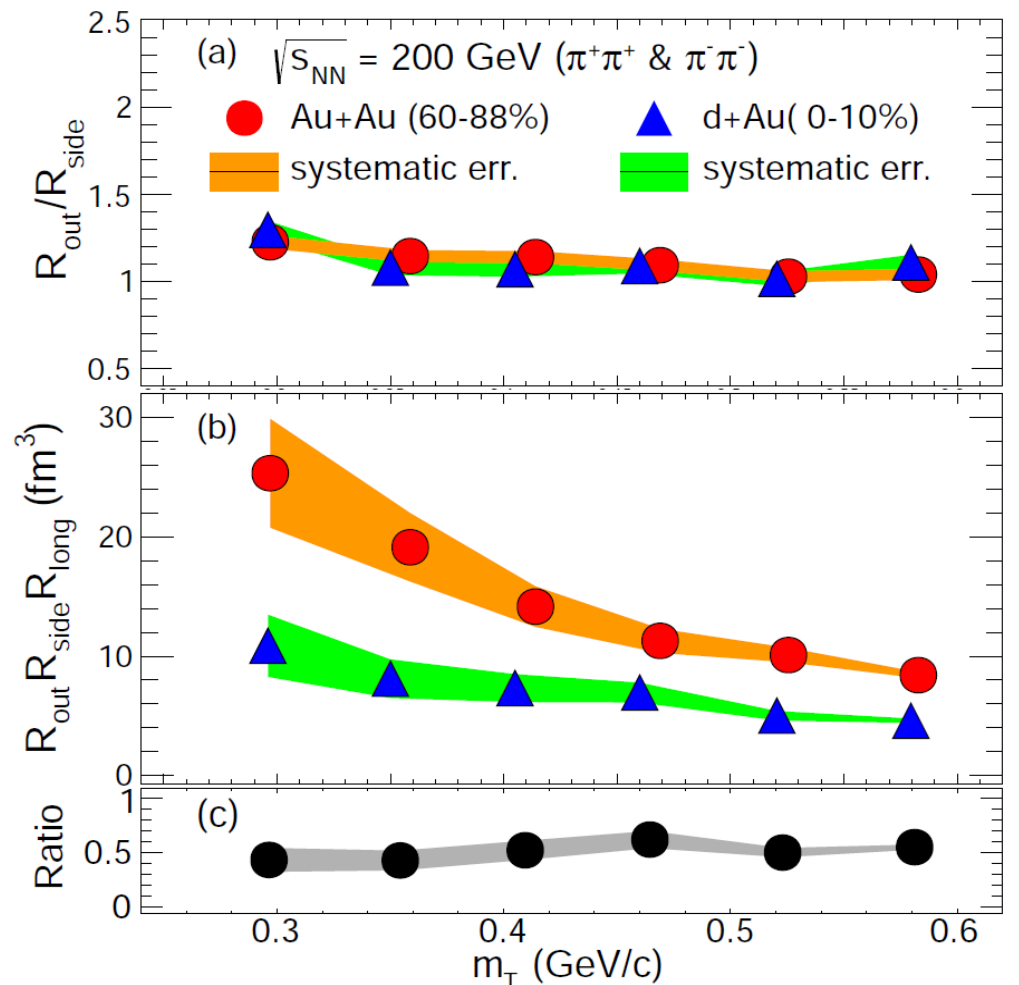
End



✓ *Combined scaling understood*



Comparison of Au+Au and d+Au collisions – m_T dependence



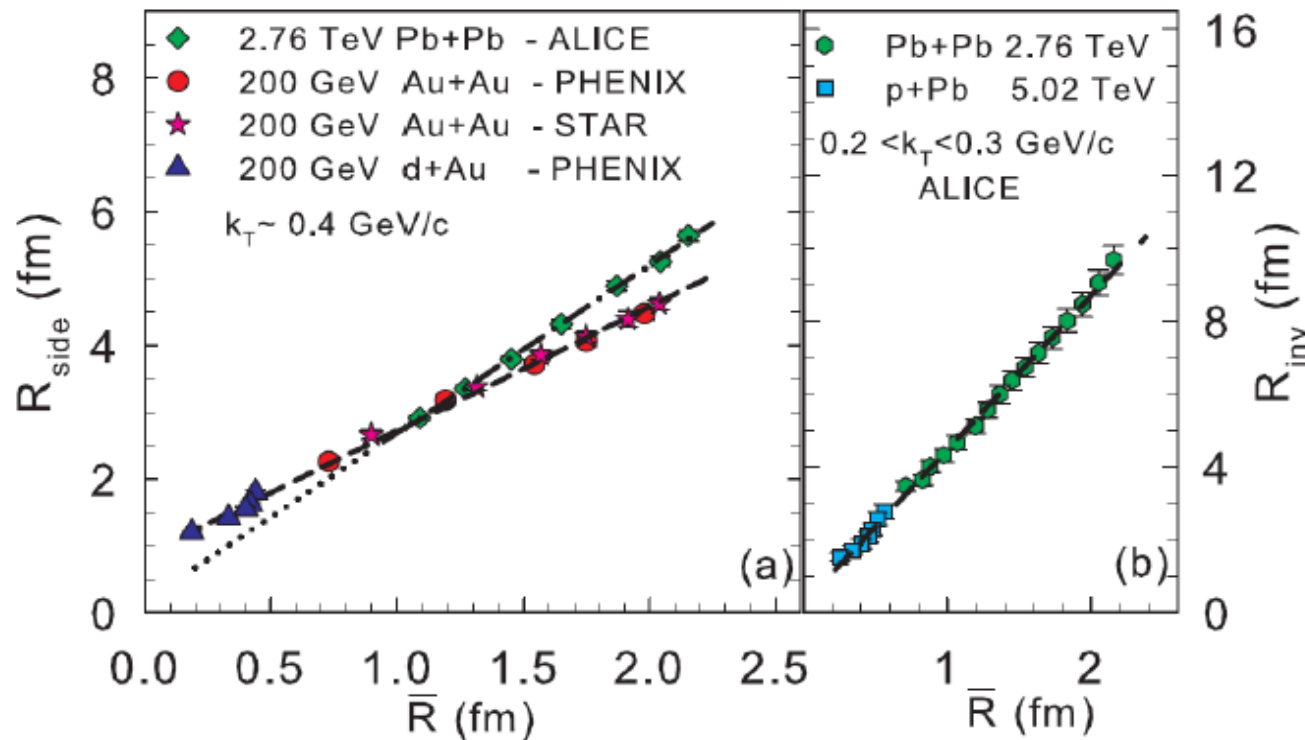
$$R_{out}^2 = \frac{R_{geom}^2}{1 + \frac{m_T}{T} v^2} + \frac{1}{2} \left(\frac{T}{m_T} \right)^2 \beta_T^2 \tau_0^2 \quad R_{side}^2 = \frac{R_{geom}^2}{1 + \frac{m_T}{T} v^2}$$

$$\frac{R_{out}}{R_{side}} \propto \Delta \tau$$

Similar m_T dependence for Both systems

d+Au indicates a smaller freeze-out volume!

Scaling of the transverse radii



d+Au, Cu+Cu and Au+Au radii scale for the same beam energy

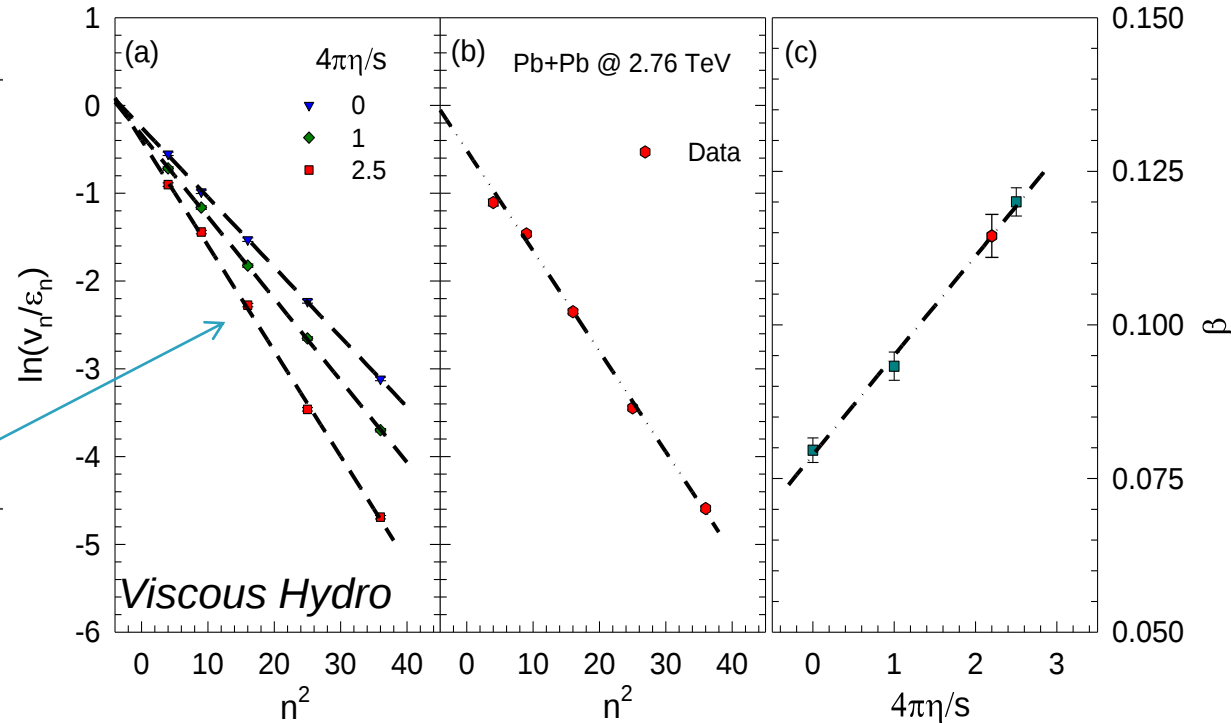
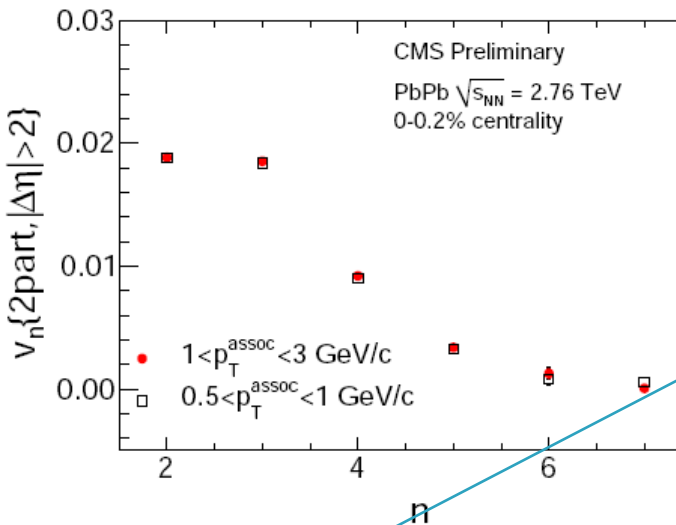
- Expansion dynamics of the d+Au system appears to be strongly influenced by final state effects
- Larger expansion rate at the LHC

Extraction of η/s

$$\frac{v_n(p_T)}{\varepsilon_n} \propto \exp(-\beta' n^2)$$

arXiv:1301.0165

& CMS PAS HIN-12-011



Slope sensitive
to η/s

Characteristic n^2 viscous damping validated in viscous hydrodynamics; calibration $\rightarrow 4\pi\eta/s \sim 2.2 \pm 0.2$
Extracted η/s value (LHC) insensitive to initial conditions